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**A FORTRAN PROGRAM TO CALCULATE AN  
ENGINEERING ESTIMATE OF THE THERMAL  
RADIATION TO THE BASE OF A MULTI-ENGINE  
SPACE VEHICLE AT HIGH ALTITUDES**

by E. R. HEATHERLY, M. J. DASH, G. R. DAVIDSON, AND C. A. RAFFERTY  
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ABSTRACT

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A method of estimating the radiant heat flux in a base of arbitrary shape from intersection regions caused by the interaction of hydrogen-oxygen engine exhaust jets is presented. An approximate method of generating the intersection region shape and temperature-pressure profiles is discussed. A computer program incorporating both of the above is described and instructions are given for its loading and use. The accuracy of this program is expected to yield within an order of magnitude of the true value of thermal radiation.

AUTHOR ↑

NASA - GEORGE C. MARSHALL SPACE FLIGHT CENTER

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## TECHNICAL MEMORANDUM X-53148

### A FORTRAN PROGRAM TO CALCULATE AN ENGINEERING ESTIMATE OF THE THERMAL RADIATION TO THE BASE OF A MULTI-ENGINE SPACE VEHICLE AT HIGH ALTITUDES

#### SUMMARY

A method of estimating the radiant heat flux in a base of arbitrary shape from intersection regions caused by the interaction of hydrogen-oxygen engine exhaust jets is presented. An approximate method of generating the intersection region shape and temperature-pressure profiles is discussed. A computer program incorporating both of the above is described and instructions are given for its loading and use. The accuracy of this program is expected to yield within an order of magnitude of the true value of thermal radiation.

#### I. INTRODUCTION

A contributing factor to the base heating rate on upper stage vehicles is radiation from the exhaust plumes. Limiting the discussion to upper stage vehicles makes it unnecessary to consider the afterburning problem. With this simplification, this radiant heating problem lends itself to division into three distinct radiating regions: the supersonic cores, the first order plume impingement regions, and the extremely complex flow field downstream from the base where the supersonic cores, first order regions, and higher order regions merge. The term "first order plume impingement region" is used to describe the region created by the shock formed when two exhaust plumes intersect. This region is an area of high temperature and pressure. A second order region is formed by the intersection of two first order regions. This terminology can be extended to describe any number of intersecting regions and will be used throughout this report.

Of the three types of radiating regions, the first two yield to analysis while the third, being virtually undefinable, does not. It was decided early in the analysis to consider the supersonic cores and first order regions as independent primary sources of radiation. To take account of the complex downstream flow field, it was decided to estimate a "lump sum" addition to the final overall radiative flux, this estimate being based on the numbers obtained for the primary radiation sources. Further analysis has revealed that of the two remaining regions, the supersonic cores are often insignificant; thus we have limited ourselves in the computer program described here to a calculation of the radiation from the first order intersection regions only.



The supersonic cores in general are at a considerably lower calculated temperature than the intersection region and, in addition, are located closer to the base. Because of this, radiation is less intense and more completely blocked by components in the base region. However, for the user who feels that the supersonic cores will contribute materially to his particular problem, a program has been developed to calculate the additional radiation from these regions using methods identical to those described in this report.

Proper use of the program discussed here will thus provide the user with an estimate of the incident radiation in a minimum of time and will show if a more detailed analysis is needed.

## II. CAPABILITIES AND LIMITATIONS

### A. Capabilities

The program will estimate the radiation incident on a base of arbitrary configuration from any number of first order regions and will predict how much of this radiation will be blocked by intervening structures in the base region. The user has the option of choosing the method of calculation of the temperature and pressure fields in the intersection region from the three methods programmed. In addition, the actual radiation is calculated by two different methods to allow comparison of two theoretical approaches to the problem. Of these methods, the average temperature and pressure method is more conservative since it assumes that the radiation passes through a transparent space from the radiating region to the base, when in fact it is passing through an absorbing medium. This method thus provides a probable upper limit to the heat flux rate. The other approach accounts for the absorption by an approximate method outlined by Hottel in Reference 1. Each method is presented with and without a blockage correction factor.

### B. Limitations and Assumptions

As mentioned earlier, this program computes only the radiation contribution from the first order intersection regions. These regions are assumed to have approximately elliptical cross sections and their temperature and pressure profiles are radially invariant. That is, temperature and pressure are assumed to vary in an axial direction only. These profiles and the geometry of the region are generated from input taken from a method of characteristics printout for a free jet expansion into quiescent air. The flow model for the first order regions is generated by assuming that this expanding plume impinges on a flat plate placed in the flow at a distance equal to one half the distance between nozzle centerlines. Oblique shock theory is then used to produce the geometry as described in Section IIIA of this report.

Both radiation methods use the emissivity data of Hottel given in Reference 1 without the correction for partial pressure. These data are used in the form of a polynomial curve fit with a maximum error in fit of 3 percent. Radiation from each intersection region is assumed to pass through a transparent medium until it impinges on the base or is blocked by one of the solid components in the base region (such as motors and heat shield).

Therefore, the program is restricted to use in cases where the only significant radiating species in the exhaust is water vapor. If the curves were fit to new emissivity data, the program could be changed to treat other radiating species.

### III. THEORETICAL BACKGROUND

The gas radiation is treated with a comparatively crude approximation. The emission and absorption coefficients, which actually vary in more or less unknown fashion through the emission spectrum of the gas are replaced by a lumped emissivity representing an integrated effect over the whole emission spectrum. This lumped or total emissivity was obtained from experiments on comparatively small samples of a homogeneous gas and extrapolated versus sample size, pressure, and temperature. The extrapolation becomes progressively more uncertain the further one moves away from the actual test conditions. Use of these data for estimating radiative heating of full scale rocket configurations should normally involve extrapolation of these data to larger beam lengths and lower pressures than those used in the basic experiments. Further, these measurements from homogeneous gas samples are used to estimate radiative emission from nonhomogeneous gas volumes. This may produce additional uncertainties.

Two methods are proposed for this estimate: the average temperature method and the absorption method. In both cases, the radiating gas volume is subdivided into conical pencil-like volume elements, extending along lines of sight from the base surface element in question. Temperature, density, and partial pressure of the radiating species vary along the gas pencil.

For the average temperature method, the properties of the gas, i.e.,  $T^4$  and partial pressure, are averaged over the length of the pencil. The "pencil" is then treated as a homogeneous gas sample, yielding a corresponding emissivity with a corresponding view factor. From these, the energy flux contribution that impinges on the base surface element under investigation is computed.

In the absorption method, the "gas pencil" is divided longitudinally into individual elements of different pressures and temperatures. The energy radiated from each longitudinal element toward the base surface element under investigation is subject to absorption losses in the pencil elements it has to pass through. This absorption loss is estimated by the assumption that the whole gas pencil between the radiating element and the surface of the intersection region has the same gas properties ( $T$ ,  $P_{H_2O}$ ) as the radiating element. While this model admittedly loses any effects of property variation on the absorption, it significantly reduces the complexity of the estimate by eliminating one integration.

To simplify the presentation, the following discussion will consider the program as though it were divided into four separate programs.

#### A. Geometry and Temperature-Pressure Profiles

From a method of characteristics analysis of a free plume expansion into quiescent air, one may obtain values for Mach number ( $M$ ) and flow direction angle ( $\theta$ ) at various points in the exhaust plume. Values of  $M$  and  $\theta$  along a line of constant radius are interpolated from this output (Figure 1). In addition, one obtains the plume expansion radius (radial distance from nozzle centerline to jet boundary streamline) as a function of axial distance. Using these input data, the initial region geometry and temperature-pressure profiles are generated using the following procedure.

##### 1. Geometry of the Intersection Region

In Figure 2, a representative cross section is drawn. The semi-major axis of the cross section,  $ADIS$ , was determined by connecting the overlap of circles whose diameters were established by the free plume boundaries from the method of characteristics. Determination of the semi-minor axis was more difficult. It was assumed that the flow field from two adjacent streams deflects by the same amount. This assumption preserves symmetry about the major axis of the region and is compatible with a hypothetical model consisting of a plane placed half way between two adjacent engines. This model is sketched in Figure 3. At points 0, 1, 2, 3, etc., the Mach number and flow angles are known. The flow impinging on the plate at point 0 produces an oblique shock at an angle  $\delta_0$  given by the equation

$$\cot \theta = \tan \delta_o \left( \frac{(\gamma + 1) M_1^2}{2 (M_1^2 \sin^2 \theta - 1)} - 1 \right) \quad (1)$$

where  $M_1$ , the Mach number before the shock, is the Mach number  $M_o$  which we have obtained from the method of characteristics analysis. This shock is shown as OB-1. It is clear that it is at an angle of  $(\delta - \theta)$  from the hypothetical flat plate. The mass flow between streamline SL-0 and SL-1 is now assumed to be turned at the shock so that it is flowing downstream parallel to the wall. Because of continuity, the flow occupies a certain distance from the plate to some streamline SL-1'. Next, the Mach number and flow angle known to exist at point 1 are transferred radially to point 1'. This transfer is justified on the grounds that the temperature and pressure are assumed constant in a radial direction and that thus the flow angle and Mach number must be constant also. At point 1' a new shock angle  $\delta_1$  is calculated as before and another section of the intersection region boundary is determined. The process is repeated until the entire region geometry is obtained. It is immediately obvious that this approach ignores mass flowing between point A and point 1'. This assumption should be reasonable if the value of  $(\delta - \theta)_o$  is small and the value of  $(\theta)_1$  is large. This case corresponds to the highly expanding plume, which is the case normally encountered in high altitude operation.

Equation (1) is limited in that it can only generate shock angles for values of flow angle less than a certain value. Figure 12 shows a parametric plot of this equation for a  $\gamma$  value of 1.23 and for Mach numbers ranging from 1.1 to 20. It is clear that since plume Mach numbers seldom exceed 10, flow angles of 55 degrees and above will not yield solutions to equation (1). In these cases, a shock angle of 65 degrees was assumed since this is approximately the maximum shock angle that can be produced by equation (1) for Mach numbers in the range of those encountered in jet plumes. (Note that there are two solutions to equation (1) for any flow angle. The highest, or "strong shock" solution, is not used in the analysis.)

The process outlined above is repeated until a complete geometrical profile of the region is developed. Figure 4 illustrates the application of the procedure for several increments. Referring to the Figure, we can see that the geometrical relation which links any one radial distance to the preceding radial distance is

$$(B/D)_n = (B/D)_{n-1} + \tan (\delta - \theta)_{n-1} (X/D)_n - (X/D)_{n-1}. \quad (2)$$

## 2. Pressure-Temperature Profiles

With the geometry of the intersection region computed, the program returns to the input data. The pressure-temperature profiles are generated using the same model as before. Postulating as before the information of an oblique shock whose angle is determined by the input flow angle for that particular axial distance, the program resolves itself into the determination of static temperatures and pressures behind a shock from the total conditions before the shock. Three methods of calculating these temperatures and pressures are programmed and may be selected by the user. In general, the oblique shock temperature and pressure equations should be used since they are more conservative than the other two models and because their use maintains consistency with the equations used to generate the region geometry.

Using the subscripts 1, 2, and 0 to denote, respectively, static conditions before the shock, static conditions after the shock, and total conditions, the following isentropic perfect gas relation holds:

$$\frac{P_1}{P_0} = \left(1 + \frac{\gamma - 1}{2} M^2\right)^{-\frac{\gamma}{\gamma - 1}} \quad (3)$$

Also the adiabatic perfect gas relation is

$$\frac{T_1}{T_0} = \left(1 + \frac{\gamma - 1}{2} M^2\right)^{-1} \quad (4)$$

The oblique shock relations used are taken from NACA Report 1135 as

$$\frac{T_2}{T_1} = \frac{[2\gamma M_1^2 \sin^2 \delta - (\gamma - 1)][(\gamma - 1) M_1^2 \sin^2 \delta + 2]}{(\gamma + 1)^2 M_1^2 \sin^2 \delta} \quad (5)$$

and

$$\frac{P_2}{P_1} = \frac{2\gamma M_1^2 \sin^2 \delta - (\gamma - 1)}{\gamma + 1} \quad (6)$$

As mentioned in the geometry section, cases exist where the shock angle  $\delta$  cannot be determined. In these situations, the program automatically switches to another method of calculation using the Rankine-Hugonot equation

$$T_2 = T_0 \left[ \frac{(1 + \beta)(1 + \alpha) + \alpha(\beta + \beta^2)}{(1 + \frac{\gamma - 1}{2} M_1^2)(1 + \alpha) + \beta + \frac{\gamma - 1}{2} M_1^2 \beta} \right], \quad (7a)$$

where

$$\alpha = \frac{\gamma - 1}{\gamma + 1} \quad \text{and} \quad \beta = \gamma M_1^2 \sin^2 \theta \quad (7b)$$

for the temperature calculation.

For the pressure calculation, the modified Newtonian Impact Theory equation

$$\frac{P_2}{P_1} = C_p (\gamma/2) M_1^2 + 1 \quad (8)$$

and

$$C_p = 2 \sin^2 \theta \quad (9)$$

is used. These equations may also be called for by the user if desired by inputting a control value as described in Section VIIIA of this report.

In addition, the isentropic flow equation

$$\frac{T_2}{T_1} = \left( C_p \frac{\gamma}{2} M_1^2 + 1 \right)^{\frac{\gamma - 1}{\gamma}} \quad (10)$$

is programmed and may be requested by use of the control variable. The pressure calculation is made using equation (8).

These calculations are repeated progressing in an axial direction until the entire profile has been generated. Due to the assumption that the static temperature before the shock is constant, it follows that the static temperature behind the shock does not vary from point 0 to point 1' in Figure 3 and thus also from 0 to 1. Then, at point 1, a step discontinuity will exist and the temperature from 1 to 2 will be the temperature calculated from the flow angle at point 1. If a plot of temperature vs axial distance were obtained, these discontinuities would cause the curve to resemble a "step" function. To smooth the curve, linear temperature gradients and not constant temperatures are assumed to exist between analyzed axial points.

### B. The Average Temperature Method

The Average Temperature Method is an analysis of the problem which uses the fundamental Stephan-Boltzman Law

$$Q = \sigma T^4. \quad (11)$$

Obviously, a sort of mean temperature and pressure for each radiating increment must be developed. The method of calculating these mean values is described below.

The intersection region was first divided into a number of increments. A line of sight from a point on the base to the lower edge of each increment was established and extended through to the rear face of the plume. A view factor, F, to account for the fact that the point on the base only "sees" one side of each radiating increment, was calculated following the analysis of Sparrow [2]. This derivation is performed in detail in Appendix A. This factor is calculated for each individual increment radiating to a point (Figure 5).

The mean temperature along the beam length itself is

$$T_{AV}^4 = \frac{\int_{x_1}^{x_2} (T(x))^4 dx}{x_2 - x_1}, \quad (12)$$

where  $x_1$  and  $x_2$  are the axial coordinates of the points where the beam enters and leaves the intersection region, respectively. A similar formula is applied for the evaluation of the average pressure along the beam length. Using this average pressure, the partial pressure of the water vapor in the exhaust is

$$P_{H_2O} = (FX1) P_{AV}, \quad (13)$$

where  $FX1$  is the mole fraction of  $H_2O$  vapor in the exhaust plume.

With the partial pressure, temperature, and beam length determined, the emissivity is obtained from the data of Hottel [1]. These emissivity data have been curve-fitted with a series of polynomial expressions such that the maximum error is  $\pm 3$  percent in fit. From this the emissivity may be determined and used in the final expression for  $Q$ , the heat flux

$$Q = \sigma F \epsilon T_{AV}^4. \quad (14)$$

### C. The Absorption Method

The absorption method employs the equation developed by Hottel [1] to account for the absorption in the intersection region. The equation employed is

$$Q = \frac{1}{\pi} \int_{\omega} \int_X \sigma T^4 (d\epsilon/dX) \cos \theta d\omega dX. \quad (15)$$

In this expression,  $X$  is the optical beam length and is evaluated as

$$X = P_{H_2O}(L), \quad (16)$$



and

$$\frac{1}{\pi} \int_{\omega} \cos \theta d\omega \quad (17)$$

is a solid angle shape factor previously called F. Then

$$Q = F_{\sigma} \int_{P_w L} T^4 \frac{d\epsilon}{d(PL)} d(PL). \quad (18)$$

The plume is divided as before into increments and a pencil ray (line of sight) erected to the lower edge of each increment. This line of sight is now the optical beam along which equation (18) must be evaluated. To do this, we must first evaluate the pressure and temperature at various points along the beam. This is done using a straight line interpolation method which is quite valid because of the smooth nature of the temperature and pressure profiles and to the small distance between points at which the evaluation is made.

The emissivity slope is easily evaluated since the curve fits mentioned in Section IIIB are functions of (PL) with T as a parameter. Thus, an explicit differentiation of these polynomial curve fits is possible without resorting to numerical techniques. Since all the variables are functions of the position variable L, we may now proceed to simplify equation (18).

$$Q = F_{\sigma} \int_{PL_1}^{PL_2} T_1^4 (1/P) \frac{d\epsilon}{dL} PdL, \quad (19)$$

since

$$d(PL) = PdL \quad (20)$$

by the assumption that temperature and pressure are constant in the particular increment of length under analysis. Then

$$Q = F\sigma \int_{PL_1}^{PL_2} T_1^4 \frac{d\epsilon}{dL} dL. \quad (21)$$

Equation (21) is evaluated using Simpson's rule and the value for F already computed in Section IIIB.

#### D. Blockage

In certain base configurations, a great deal of the radiation from the exhaust plumes will impinge upon the motors, heat shield, and other obstructions in the base, and will not therefore contribute to the heat flux rate to the base. To evaluate how much of the radiation is blocked, a section of the program generates a blockage factor and applies it to each intersection region. This blockage factor is not related to the form factor F computed in Section IIIB. The form factor expresses what portion of the intersection region the point "sees" assuming a transparent space between radiating region and point. The blockage factor increases the realism of the model by removing the "transparent space" assumption and substituting the actual base obstructions.

It was decided that the easiest method of generating a blockage factor was to determine if each individual beam was blocked and if it were to consider the radiation from the increment associated with that beam to be 0. Since the increments have widths which in some cases are appreciable, three lines of sight are erected to each increment, one to each side and one to the center. Each line is assumed to represent one-third of the radiation incident from the region. Thus, blockage of each beam reduces the incident radiation by one-third.

The obstructions are first represented as circles in a three-dimensional, Cartesian coordinate system located as follows.

1. The xy plane is located at the exit plane of the motors such that the z coordinates of all obstructions and the points to be analyzed are negative or zero.

2. The xz plane passes through the center of the heat shield and through the point being analyzed with the negative axis in the direction of the point being analyzed such that "x" and "z" coordinates of the point are negative and the "y" coordinate is always 0.

3. The yz plane is oriented as usual in a right-handed Cartesian coordinate system. See Figure 6 for a graphical illustration of this system.

The obstructions are assumed to be circles located in, or parallel to, the xy plane. In this way, a three-dimensional nozzle can be fairly well represented by, for example, three circles with radii equaling the radii of the nozzle at three different heights. The model expressing this nozzle would then become three circular areas in space given by the relations (in our coordinate system)

$$(x - h)^2 + (y - k)^2 \leq r_1^2 \quad z = z_1 \quad (22)$$

$$(x - h)^2 + (y - k)^2 \leq r_2^2 \quad z = z_2 \quad (23)$$

$$(x - h)^2 + (y - k)^2 \leq r_3^2 \quad z = z_3. \quad (24)$$

If the obstruction has its axis parallel to the axis of the vehicle (which is our z-axis) then "h" and "k" are constant for the three equations. The "h" and "k" coordinates are the "x" and "y" coordinates of the center of the obstruction. If the axis of the body is tilted with respect to the vehicle axis then "h" and "k" vary. They are then the coordinates of the center of the obstruction at that particular height. A slight error is thus introduced because of the assumption that the circles lie parallel to the xy plane when, in fact, they are tilted to be perpendicular to the obstruction axis; but this error will not be appreciable unless the tilt is considerable.

With equations (22), (23), and (24) defining three areas in space, it is clear that, for a line of sight to avoid intersecting one of these areas, yet in fact to be blocked by the nozzle, the line of sight must be almost parallel to the xy plane. Since in practice the intersection region must begin at some finite distance above the nozzle exit plane, and the point to be analyzed must be some distance below the nozzle exit plane, the line of sight angle should be sufficient to allow these three circles to adequately describe the blockage. In many cases, in fact, one circle suffices. (In theory, a large number of circles used as above could completely describe an axisymmetric obstruction. In practice, however, only forty equations may be used in the program

to describe the whole base or a portion of it if so desired. Therefore, one should not use more circles than are necessary on any one obstruction.)

Once the entire base picture has been presented in the simplified terms shown above, the coordinate system is shifted so that it is now centered at the point to be analyzed, the orientation of the axes being as before. Now it is clear that all the obstructions are at positive "z" coordinates and most are also at positive "x" coordinates.

To illustrate this transformation, assume a point P located at  $(x', 0, z')$  as shown in Figure 6 where  $z = 0$  is defined to exist at the nozzle exit plane. Assume also a point in an intersection region located at  $(x_i, y_i)$ . Its z coordinate is unimportant. Assume also a circular blockage located at  $(h, k, z_0)$  with a radius "r." The equations for this blockage region are

$$(x - h)^2 + (y - k)^2 \leq r^2. \quad z = z_0 \quad (25)$$

To transfer these equations to a coordinate system centered at P, the following transformation equations are needed. (The subscript 2 refers to the new system.)

$$x_2 = x - x' \quad y_2 = y \quad z_2 = z - z'. \quad (26)$$

Then, the transformed blockage equation is

$$(x_2 + x' - h)^2 + (y - k)^2 \leq r^2 \quad z_2 = z_0 - z'. \quad (27)$$

Given a line of sight with an angle,  $\beta$ , from the horizontal (the new xy plane) and knowing the z coordinate of the obstruction (Figure 7), we may calculate the distance (HYP) from P to the point where the line of sight passes through the plane of the obstruction ( $z_2 = z_0 - z'$ ).

$$HYP = \frac{z_2}{\tan(\beta)}. \quad (28)$$

Also, from the coordinates of the center of the intersection region which must be crossed by the beam, an angle  $\theta$  may be calculated as follows:

$$\theta = \tan^{-1} \frac{|y_i|}{x_i} . \quad (29)$$

With  $\theta$  and HYP, the coordinates of the point where the line of sight passes through the intersection region may be calculated.

$$x_o = (\cos \theta) \text{ HYP} \quad (30)$$

$$y_o = (\sin \theta) \text{ HYP} . \quad (31)$$

The sign of  $y_o$  is the same as the sign of  $y_i$  since P is on the x-axis.

Now, if the calculated values of  $x_o$  and  $y_o$  satisfy equation (25) the line of sight is blocked. If not, the process is repeated with new parameters. Finally, a new summation of all the unblocked radiation is made to give a better estimate of the environment.

#### IV. PROGRAM DESCRIPTION

The program is written in Chain Fortran for the GE 225 computer. The use of Chains was caused by the large number of subscripted variables and makes the program a compendium of four smaller programs. Each of these smaller programs contains the coding of the equations contained in one of the four sections just discussed.

This segmenting makes checkout and error investigation quite simple since one can immediately isolate a given section as the one in which the error occurred and restrict his investigation to it.

Each of the four sections follows closely the pattern laid down in the preceding portion of this report. Numerous interpolation, approximation, and averaging methods which are similar to techniques developed in the standard texts [3] are used as needed in the program. No unusual numerical differentiation and integration techniques are employed, and nothing other than simple geometry is used in the various form factor and beam length calculations. In short, the theory presented in the preceding portion of this report is followed closely with little modification.

Figure 8 contains a printout of the program as it is read into the machine. Notice the marginal notations separating the four sections of the program. If each of these sections is compared with the corresponding theory section of this report by a person familiar with Fortran II, there is no reason why he should not be able to follow the programming and to verify his results in any way he wishes.

Figure 9 contains a flow diagram to completely illustrate the flow of control throughout the program.

## V. NOTATION

<u>Program Symbol</u>	<u>Description and Units</u>
(J) (or a similar subscript)	Numerical subscript where J has a value from one number to another (i.e., 1 to L).
A(I, J) (J = 1 to 4)	Table of input from the method of characteristics.
A(I, 1)	Distance, nondimensionalized by DIA, measured along the nozzle axial line from the exit plane of that nozzle. The first value must be the initial intersection point.
A(I, 2)	} CHAIN I Mach number corresponding to A(I, 1) but located on the axial line of the intersecting region (not to be confused with critical condition Mach number, $M^*$ ).
A(I, 3)	
A(I, 4)	Flow direction angle corresponding to A(I, 1) but located on the axial line of the intersecting region, in radians.
A(I, 4)	Radius, nondimensionalized by DIA, of the circle formed by a plane drawn perpendicular to the nozzle axial line and cutting the exhaust plume for a corresponding A(I, 1).

Program SymbolDescription and Units

A(I, 1)		
A(I, 2)		
A(I, 3)	CHAIN IV	Center and radii of the blockage regions located in the (x, y, z) coordinate system illustrated in Figure 6, ft.
A(I, 4)		
ABSI		An increment length, nondimensionalized by DIA, that is 1/50 that of the beam length, FLE(J).
ADIS(J)		One-half the length, nondimensionalized by DIA, of the major axis of the elliptical plane for the intersecting region.
ANGLE(J)		The angle formed by the beam and its projection in the base plane, radians.
AVTEM(J)		Average temperature for the beam length, FLE(J), °R.
AVP(J)		Average pressure for the beam length, FLE(J), ATM.
BDIS(J)		One-half the length, nondimensionalized by DIA, of the minor axis of the elliptical plane for the intersecting region.
BLED(J)		Dimensional value for the beam length, ft.
C		The angular difference between the shock angle, DELTA, and a corresponding flow direction angle), radians.
DELI		Minimum shock angle for a given GAMMA and Mach number, FM(J) (zero flow direction angle), radians.
DELM		Maximum shock angle for a given GAMMA and Mach number, FM(J), radians.

<u>Program Symbol</u>	<u>Description and Units</u>
DELTA	Shock angle for a given GAMMA, Mach number, FM(J), and flow direction, T(J), radians.
DIA	Diameter of the nozzle exit, ft.
EMIS	Emissivity of the beam length, FLE(J).
F	Shape factor corresponding to a given beam. (F is the view factor associated with each beam length that radiates energy back to the viewpoint.)
FINTX	x-coordinate of intersection region center in coordinate system of Figure 6.
FINTY	y-coordinate of intersection region center in coordinate system of Figure 6.
FK	The distance, nondimensionalized by DIA, in the base plane from the point of view to the axial line for the intersecting region. (The value of FK is always negative.)
FLAG	Value, either +1 or 0, instructing computer on how to proceed.
FLE(J)	Length, nondimensionalized by DIA, of the beam within the bounds of the intersecting region.
FM(J)	Mach number on the axial line of the intersecting region corresponding to XD(J) (not to be confused with critical condition Mach number, M*).
FXI	Mole fraction of each of the gas components in the exhaust plume.
GAMMA	Ratio of specific heats for the exhaust components.
L	Number of desired data values for XD(J).
LL	Number of data values input for each A(I, 1), A(I, 2), A(I, 3), and A(I, 4) in Chain I.
LLLL	Number of blockage region circles.



Program SymbolDescription and Units

MCON	If +1: oblique shock theory temperature and pressure used. 0: Rankine-Hugiot temperature and Newtonian impact theory pressure used. -1: isentropic temperature and Newtonian impact theory used.
PBPX	Ratio of base pressure to exit pressure.
PHI	View angle formed by one-half the minor axis, BDIS(J), of the elliptical plane for the intersecting region and a corresponding projection of part of the beam into the same elliptical plane (Figure 6), radians.
PH20	Partial pressure for the beam length, FLE(J), ATM.
PO	Chamber pressure of the nozzle, ATM.
P(J) and PW	Static pressure for a location in the exhaust plume, ATM.
PX	x-coordinate of point being analyzed in coordinate system of Figure 5.
PY	y-coordinate of point being analyzed.
PZ	z-coordinate of point being analyzed.
QRAD	Radiant heat flux by the average temperature and pressure method for the beam length, FLE(J), BTU/ft <sup>2</sup> -sec.
QRADS	The total accumulated heat flux contribution by average temperature and pressure method for two or more beam lengths, BTU/ft <sup>2</sup> -sec.
QRDA	Radiant heat flux by absorption method for a single beam length, FLE(J), BTU/ft <sup>2</sup> -sec.
QRDAS	Total accumulated radiant heat flux by absorption method for two or more beam lengths, BTU/ft <sup>2</sup> -sec.
R	One-half the distance, nondimensionalized by DIA, between two adjacent nozzle center lines.

<u>Program Symbol</u>	<u>Description and Units</u>
RC(J)	One-half the length, nondimensionalized by DIA, of an axis in the elliptical plane for the intersecting region that is formed by a beam where it pierces this region and a point on the axial line of the same region.
RD(J)	Radius, nondimensionalized by DIA, measured in the same manner as that of A(1, 4) and corresponding to XD(J).
SABSIS	Total accumulated ABSIS increments to point in question.
SSF	The total accumulated shape factor for two or more beam lengths.
SXD	Perpendicular distance, nondimensionalized by DIA, between the base plane and the nozzle exit plane.
TAB	Table of flow direction angles, radians, obtained from a plot of flow direction angle, shock angle, and Mach number (Figure 13).
TABL	Table of Mach number values obtained from a plot of flow direction angle, shock angle, and Mach number (Figure 13).
TDIS(J)	One-half the length, nondimensionalized by DIA, of an axis perpendicular to RC(J) and in the same elliptical plane for the intersecting region.
TEMP(J) and TW	Static temperature for a location in the exhaust plume, °R.
THETA	Flow direction for a given GAMMA, Mach number, FM(J), and shock angle, DELTA, radians.
T(J)	Flow direction angle on the axial line of the intersecting region corresponding to XD(J), radians.
TO	Chamber temperature of the nozzle, °R.

Program SymbolDescription and Units

XD(J)	Arbitrary distance, nondimensionalized by DIA, that is measured in the same manner as is A(I, 1). (Simply numbered values for XD(J) make it easier for the user to plot the results. XD(J) can be set equal to A(I, 1) if so desired.)
XD(L + 1)	Selected value, nondimensionalized by DIA, that is slightly larger than the last input value for XD(J). (The value, XD(L + 1), is necessary so that the solution of shape factor can be completed for the last increment.)
XO	x-coordinate of point at which line of sight to I.R. pierces plane of obstruction.
YO	y-coordinate of point at which line of sight to I.R. pierces plane of obstruction.
ZO	z-coordinate of point at which line of sight pierces plane of obstruction.

## VI. INPUT

The program requires as input certain characteristics of the rocket engines on the missile in question, the base geometry and a flow field. Since the input required is quite extensive, it will be treated as three separate topics. In addition, the discussion will be restricted to the input and how it is obtained leaving the actual load format for a separate section.

A. Flow Field Description

The program requires extensive input data to describe the downstream flow field. This input is received in the form of tables of the free exhaust plume properties, Mach number,  $M$ , flow angle,  $\theta$ , and plume radius,  $R$ , as functions of axial distance. The axial distance and the plume radius are nondimensionalized by the exit diameter and will hereafter be referred to by their symbolic names  $X/D$  and  $R/D$ . The Mach number is not the characteristic Mach number  $M^*$  but is related to it by

$$M = \sqrt{\frac{2M^{*2}}{(\gamma + 1) - (\gamma - 1) M^{*2}}} \quad (32)$$

The angle  $\theta$  is expressed in radians. These tables are obtained from a method of characteristics analysis as follows.

In Figure 1 it may be seen that by a two-way interpolation into the method of characteristics output, values of  $M$  and  $\theta$  may be found along a line of given radial distance from the nozzle centerline. In addition, at the specific  $X/D$  location at which the  $M$  and  $\theta$ 's are found, the free plume radius must also be input as shown in the figure. The first  $X/D$  chosen must be at the initial intersection point and additional  $X/D$ 's down the plume may be chosen arbitrarily; however, the bottom number must not exceed 60.

Given now this set of tables of  $M$ ,  $\theta$ , and  $R/D$  as functions of  $X/D$ , the user next inputs the  $X/D$  distances at which he wants his lines of sight to pierce the intersection region. The input fixes the number of increments into which the intersection region will be divided; thus, it will generally be advantageous to input as many as practical. The number of these points is in no way related to the number of points in the above tables except that no more than 60 may be input, and the highest and lowest value must be within the range of the previously input tables.

A review of the oblique shock equations will show that the equation relating the shock angle  $\delta$  to the flow direction angle  $\theta$  does not allow a  $\delta$  to exist for all  $\theta$  values. In particular, for a given specific heat ratio and Mach number, there exists a maximum  $\theta$  beyond which a corresponding shock angle does not exist. The program is made aware of these limits by inputting a table of Mach numbers and the corresponding maximum  $\theta$  values so that it will not try to solve for a nonexistent angle. This table consists of ten values and must be obtained for the correct specific heat ratio as it varies strongly with that parameter.

#### B. Rocket Motor Input

The given rocket motor must be characterized for the program by inputting its total temperature, total pressure, its exit diameter, the specific heat ratio of its exhaust gases and the pressure ratio (exit pressure to ambient pressure) at which the method of characteristics analysis was run.

#### C. Base Geometry

Referring to Figure 10, the program needs the distances  $SXD$  and  $FK$ , both in the nondimensionalized (divided by the exit diameter) mode. In addition, the location of the blockage regions and intersection

regions in a coordinate system oriented as described in Section IIID are needed. The dimensions of this coordinate system must be in feet.

In addition to the above input, a number of constants which effect control of the execution cycle are needed and are described later in the load format section.

## VII. OUTPUT

The output is limited since execution time is already quite long and excessive print statements only make it longer. As may be seen in Figure 11, the output is arranged in the same logical order as was followed in Section III. The first section is devoted to the temperature and pressure profiles; the second to one radiation method; the third to the absorption method; and the fourth to the blockage correction factors. As may be seen, the total cumulative radiation, as well as the radiation from the individual increments, is summed in each case.

Note that in the blockage correction section each increment is divided into left, middle and right sides. The coordinates at which the line of sight to each of these three points pierces the planes of the various obstructions ( $x_0$ ,  $y_0$ ) are printed out. If the line of sight is blocked, the last set of  $x_0$ ,  $y_0$  coordinates printed out are within a blockage circle. This is shown on the output in Figure 11.

Figure 11 contains the complete output for the sample problem in Section VIIIB.

## VIII. LOAD FORMAT AND SAMPLE PROBLEM

### A. Load Format

A few basic rules for writing a load format for the GE 225 Fortran are as follows:

1. Fixed point numbers must have an X before the number and must be immediately followed by a comma (i.e., X31,). "X31 ;" will be misinterpreted.
2. Each value must be separated by a comma (i.e., .21, .2646, ...).
3. Every data card must end with an asterisk (i.e., .28, .29, .30\*).

4. Floating point numbers can be written either in decimal form without exponent or with exponent (i.e., .000539 or 5.39E-4).
5. Any one data card cannot contain values listed on more than one read statement (RCD).
6. Data must be set up in the same order as it is listed in the read statement (RCD).
7. All floating point numbers must have decimal points (i.e., the expression 31 is not permitted).

These rules must be followed explicitly.

In the following discussion the input will be separated into blocks. Each block of data must go on one or more cards. The first item in each new block must be the first item on a new card; i.e., no card may contain data from two blocks.

a. Block 1

(1) A fixed point number expressing the number of values in the input table of M vs X/D. This number is of course also the number of values in the  $\theta$  vs X/D table and the R/D vs X/D table and must not exceed 60.

(2) A fixed point number giving the number of X/D locations at which the user desires to increment his intersection region.

(3) A fixed point number with its value determined from the following.

- (a)  $X + 1$  if oblique shock relations are desired in the solution of the temperature and pressure profiles.
- (b)  $X + 0$  if Rankine-Hugonot relations are desired.
- (c)  $X - 1$  if isentropic flow relations are needed.

(4) A floating point number giving one-half the distance between the centerlines of the two motors which are generating the intersection region. This number is the actual distance nondimensionalized by the exit diameter of the motor.

(5) The value of the chamber total pressure; atmospheres ~ floating point.

(6) The value of the chamber total temperature; °R ~ floating point.

(7) The exhaust gas specific heat ratio; floating point.

b. Block 2

A floating point number expressing the base pressure to exit pressure ratio for which the method of characteristics run was made.

c. Block 3

A set of floating point numbers in ascending order expressing the X/D coordinates of the points at which the M and  $\theta$  will be given.

d. Block 4

A set of floating point numbers expressing the Mach numbers corresponding to the X/D locations given in Block 3.

e. Block 5

A set of floating point numbers giving the corresponding  $\theta$  values; radians.

f. Block 6

A set of floating point numbers giving the corresponding R/D's. (Note: Together Blocks 3, 4, 5, and 6 give the columns of a table into which the machine may go to interpolate the value of any parameter (M,  $\theta$ , R/D) at any given X/D value during later execution stages. As a result, extreme care must be taken to assure that proper correspondence is maintained between the elements in the columns.)

g. Block 7

A series of floating point numbers giving the X/D locations at which the plume is desired to be incremented. The number of these points is given in Block 1, part 2.

h. Block 8 and Block 9

These two blocks contain the maximum values of M and  $\theta$ , respectively, which are used to prevent the program from solving for a nonexistent shock angle. Referring to Figure 12, notice that for a Mach number 4.0 and a flow angle  $\theta$  of 55 degrees no shock angle  $\delta$  exists. Thus, to prevent the program from attempting to solve for shock angles

in cases like this, a table of Mach numbers and the maximum corresponding  $\theta$  angles is input. Figure 12 shows such a table for Figure 12. This table must have ten values.

i. Block 10

- (1) Exit diameter of the rocket engines used on the base being considered. A floating point number ~ feet.
- (2) The percent water vapor in the exhaust plumes. Floating point ~ dimensionless.
- (3) A selected X/D location equal to the last X/D location in Block 7 plus .1. Floating point ~ nondimensionalized.

j. Block 11

- (1) The distance in the plane of the point being analyzed from the point of view to the axial line of the intersecting region. This value is always given a negative sign. A floating point number ~ nondimensionalized (see Figure 10).
- (2) The angle formed by the semi-major axis, BDIS(J), of the elliptical plane for the intersection region and a corresponding projection of part of the beam into the same elliptical plane. A floating point number ~ radians (see Figure 14).
- (3) The perpendicular distance between the plane of the point being analyzed and the nozzle exit plane. A floating point number ~ nondimensionalized (see Figure 10).

k. Block 12

- (1) The number of blockage circles being considered. Must not exceed 40. A fixed point number ~ dimensionless.
- (2) The x-coordinate of the center of the intersection region being considered. A floating point number (including sign) ~ feet.
- (3) The y-coordinate of the center of the intersection region being considered. A floating point signed number ~ feet.



l. Block 13

A series of numbers expressing the x-coordinates of the blockage circle centers. Floating point signed numbers ~ feet.

m. Block 14

A series of numbers expressing the y-coordinate of the blockage circle centers. Floating point signed numbers ~ feet.

n. Block 15

A series of numbers expressing the z-coordinate of the blockage circle centers. Floating point signed number ~ feet.

o. Block 16

A series of numbers expressing the radius of each of the blockage circles. A floating point number ~ feet.

p. Block 17

- (1) A value, either +1.0 or 0.0 depending upon whether a new intersection region is to be analyzed next or just a new point. This number is a command to the machine.

+1.0 if a new point is to be analyzed or  
if this is the last piece of data.

0.0 if a new intersection region is to be  
considered.

- (2) This value is +1.0 if the intersection region being analyzed has an x-coordinate greater than the x-coordinate of the point being considered. If the intersection region has an x-coordinate less than the point being considered, then the value in this position is the x-coordinate. A floating point negative (all x-coordinates are negative according to the defined coordinate system in Section IIID) number ~ feet. As clarification, a case where the x-coordinate must be input in this manner is illustrated in Figure 15.

## B. Sample Problem

As a sample problem an analysis of the radiation incident on a point on the thrust structure of the S-II stage from two of the eight I.R.'s will be made. Figure 16 shows the base with some of the necessary geometrical input. Figure 17 shows the same base drawn in the necessary coordinate system to input the coordinates of the intersection regions and blockage regions. Other necessary input data concerning the engine and other features of the base are:

Chamber Total Pressure: 43.004899 atmospheres.

Chamber Total Temperature: 5760 °R

Exit Diameter: 6.6666 feet

Distance between Engine Centerlines: 12.37 feet

Specific Heat Ratio of Exhaust Gases: 1.23

Percent Water Vapor in Exhaust Gases: 63% = .63.

Now a method of characteristics analysis of a J-2 engine free plume expansion into quiescent air must be obtained. From this we develop the following table.

TABLE I

(Note that the axial distance and radius have already been divided through by the exit diameter, 6.6666 ft.)

<u>A</u> X/D	<u>B</u> M	<u>C</u> Theta - $\theta$	<u>D</u> Free Plume Expansion Radius - R/D
.55300	5.55	.59932	.932
.60577	5.678	.61166	.971
.68793	6.121	.69823	1.022
.75513	6.027	.65766	1.062
.82400	6.01	.63600	1.103
.87308	5.89	.60129	1.131
.91254	5.874	.58471	1.456

<u>A</u>	<u>B</u>	<u>C</u>	<u>D</u>
X/D	M	Theta - $\theta$	Free Plume Expansion Radius (R/D)
.96408	5.840	.56404	1.182
1.05794	5.80	.53164	1.242
1.09118	5.78	.51986	1.260
1.14699	5.75	.50391	1.292
1.20885	5.723	.48549	1.323
1.27162	5.715	.46950	1.355
1.33487	5.710	.45436	1.388
1.43185	5.69	.43380	1.437
1.52983	5.69	.41471	1.488
1.68460	5.69	.38945	1.561
1.79133	5.70	.37429	1.609
1.90591	5.705	.36038	1.660
2.00453	5.705	.34923	1.710
2.10755	5.715	.33942	1.743
2.20516	5.718	.33107	1.783
2.31099	5.718	.32418	1.825
2.39077	5.716	.32047	1.851
2.40765	5.701	.32655	1.862
2.51795	5.705	.32794	1.902
2.6743	5.717	.31689	1.955
2.82225	5.72	.30810	2.005
2.96077	5.722	.30217	2.050
3.08055	5.725	.29927	2.086
3.19207	5.719	.29961	2.117
3.35044	5.685	.31006	2.165

It has been decided to break up the plume into increments at the following X/D locations:

.56, .60, .7, .8, .9, 1.0, 1.1, 1.2, 1.3, 1.4, 1.5,  
1.6, 1.7, 1.8, 1.9, 2.0, 2.1, 2.2, 2.3, 2.4, 2.6,  
2.8, 3.0, 3.2, and 3.3.

In addition, the graph shown in Figure 12 has been made and the values shown in Figure 13 have been chosen as the maximum Thetas and Mach numbers. With this data, the first part of the program may be loaded.

1. Block 1

- a. There are 32 figures in each column of Table I. The value loaded here is X32.
- b. According to the X/D locations shown above, the region is to be incremented at 25 X/D's. Value loaded is X25.
- c. Oblique shock theory is desired.  $X + 1$ .
- d. One half the distance between rocket engine centerlines divided by the exit diameter is .92773.
- e. Value is 43.004899.
- f. Value is 5760.0.
- g. Value is 1.23.

2. Block 2

The pressure ratio for this run was .0185.

3. Block 3

Load here column A of Table I in order going down, taking as many cards as needed.

4. Block 4

Load here column B.

5. Block 5

Load here column C.

6. Block 6

Load here column D.

7. Block 7

Load here the 25 values of X/D locations listed on page 28.

8. Block 8

Load here column A of Figure 13.

9. Block 9

Load here column B of Figure 13.

10. Block 10

a. The exit diameter of the engine is 6.666 feet.

b. Value is .63.

c. Since the last value in column A of the input table is 3.35044, the value loaded here is 3.45044.

11. Block 11

a. Referring to Figure 16 and remembering to non-dimensionalize by division by the exit diameter, the value loaded here is - .81404.

b. From the same figure, the value (in radians) loaded is 1.57079.

c. Value here is 2.09559.

Now another table is made. Referring to Figure 17, locate the blockage regions (which are the heat shield and the five motors) and prepare the following table.

TABLE II

<u>Blockage</u>	<u>x-coordinate</u>	<u>y-coordinate</u>	<u>z-coordinate</u>	<u>Radius</u>
	<u>A</u>	<u>B</u>	<u>C</u>	<u>D</u>
Heat Shield	0.0	0.0	-3.4	10.25
Engine I	-6.19	6.19	0.0	3.33
Engine II	6.19	6.19	0.0	3.33
Engine III	6.19	-6.19	0.0	3.33
Engine IV	-6.19	-6.19	0.0	3.33
Engine V	0.0	0.0	0.0	3.33

Also it is noted that the intersection region is located at  $X = -6.19$ ,  $y = 0.0$ . Now this new data is loaded.

12. Block 12

- a. There are six blockage regions so X6 is loaded here.
- b. -6.19 is the value as noted above.
- c. 0.0 is loaded here.

13. Block 13

Load here column A of Table II.

14. Block 14

Load here column B of Table II.

15. Block 15

Load here column C of Table II.

16. Block 16

Load here column D of Table II.

17. Block 17

- a. Since a new intersection region is to be analyzed the first tendency would be to load 0.0 in this place.

However, it is apparent that actually the new intersection region is formed by two motors separated by the same distance as before and formed by engines with the same characteristics as before. Thus, in effect the same intersection region is being analyzed but from a different point. 1.0 is input here. This tells the machine that it need not calculate new temperature and pressure profiles and that it may start execution with Chain II instead of Chain I.

- b. 1.0 is input here because clearly the intersection region is at a larger x-coordinate than is the point.

The input for the first intersection region analysis is now complete. Directly behind it the data for the second intersection region is loaded. Of course, since the machine already has in memory the necessary intersection region data, Blocks 1 through 9 need not be input again. Starting with Block 10 and proceeding in the same manner as before the following is loaded:

18. Block 10

- a. 6.6667
- b. .63
- c. 3.35044.

19. Block 11

- a. - 1.97363
- b. .4895
- c. 2.09559.

20. Block 12

- a. X6
- b. 0.0
- c. +6.19.

21. Block 13

Column A, Table II.

22. Block 14

Column B, Table II.

23. Block 15

Column C, Table II.

24. Block 16

Column D, Table II.

25. Block 17

a. Load here now 1.0. The machine will continue to execute, will try to read data for Block 10 and finding none, will stop.

b. 1.0.

Figure 18 presents the input for this problem as it appears on the input cards.

## IX. CONCLUSIONS AND RECOMMENDATIONS

1. This program may be used to estimate radiant heat flux rates to various missile bases from intersection regions produced by  $H_2-O_2$  engines.

2. Possible inaccuracies can exist in the calculated intersection region properties, the emissivity data, or in the application of equation (15).

3. Other inaccuracies arise because of the fact that second and higher order intersections are ignored, radiation from plume to plume is ignored, and blockage by intervening gas masses is ignored.

4. Further work is needed in all the areas mentioned in 2 and 3 above. In particular, an accurate method to calculate the region properties and an accurate method of accounting for second order regions is essential before accurate estimates can be made.



5. Measurements, preferably inflight, must be made before these analytical approaches can be completely trusted. Instrumentation must be developed that will measure these low transient heat flux rates.

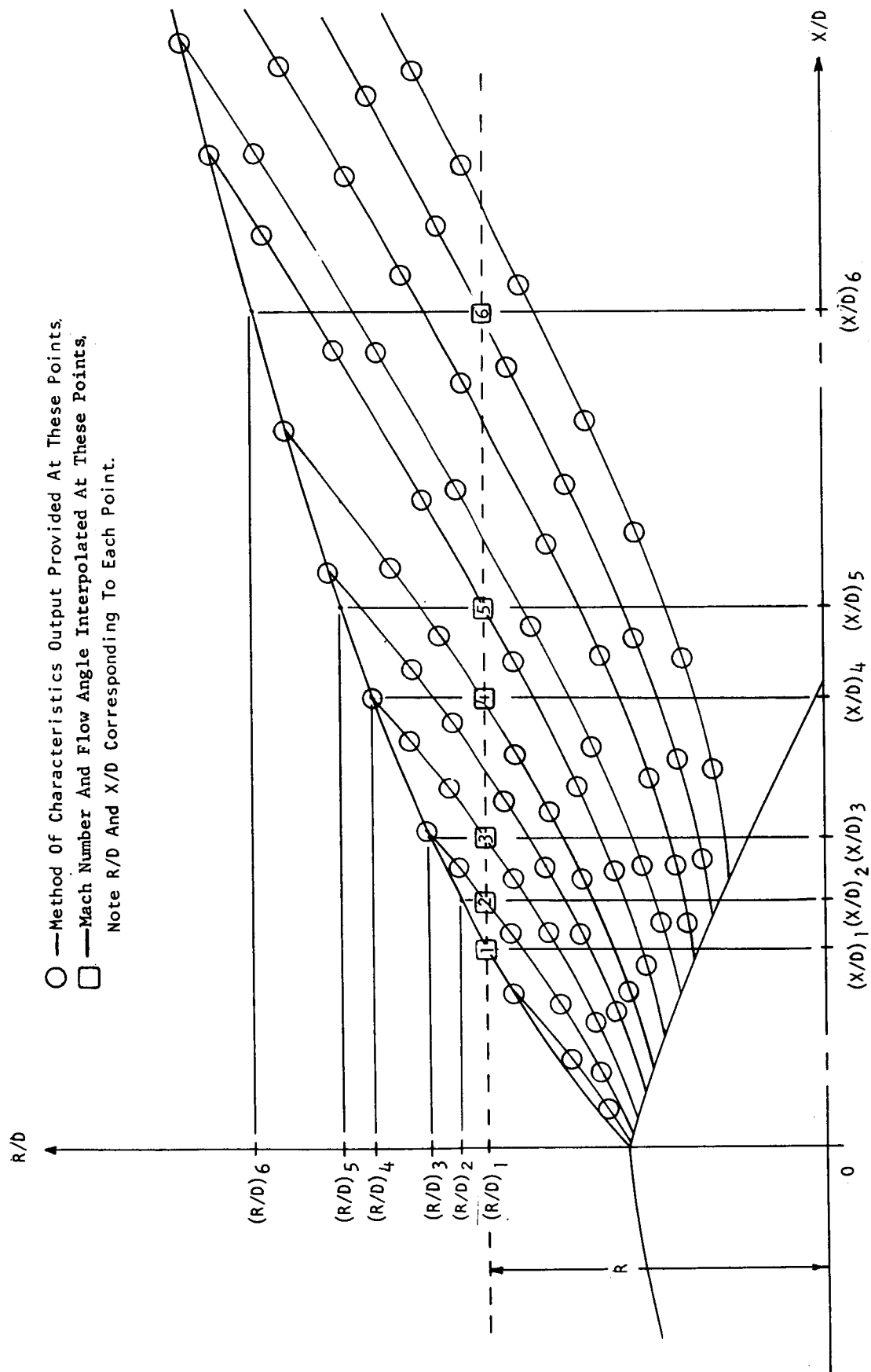


FIGURE 1. INTERPOLATED MACH NUMBER ( $M$ ) AND FLOW DIRECTION ANGLE ( $\theta$ ) ALONG A LINE OF CONSTANT RADIUS WITHIN THE EXHAUST PLUME

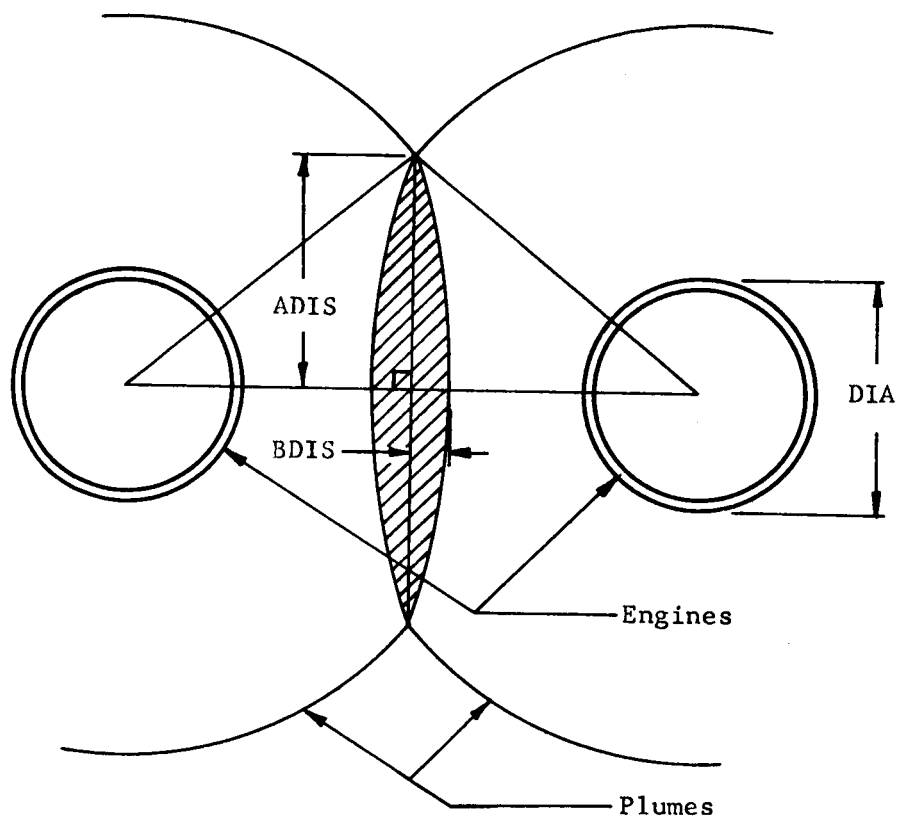
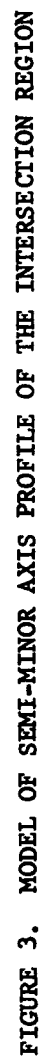


FIGURE 2. GEOMETRY OF THE CROSS SECTION OF THE INTERSECTION REGION





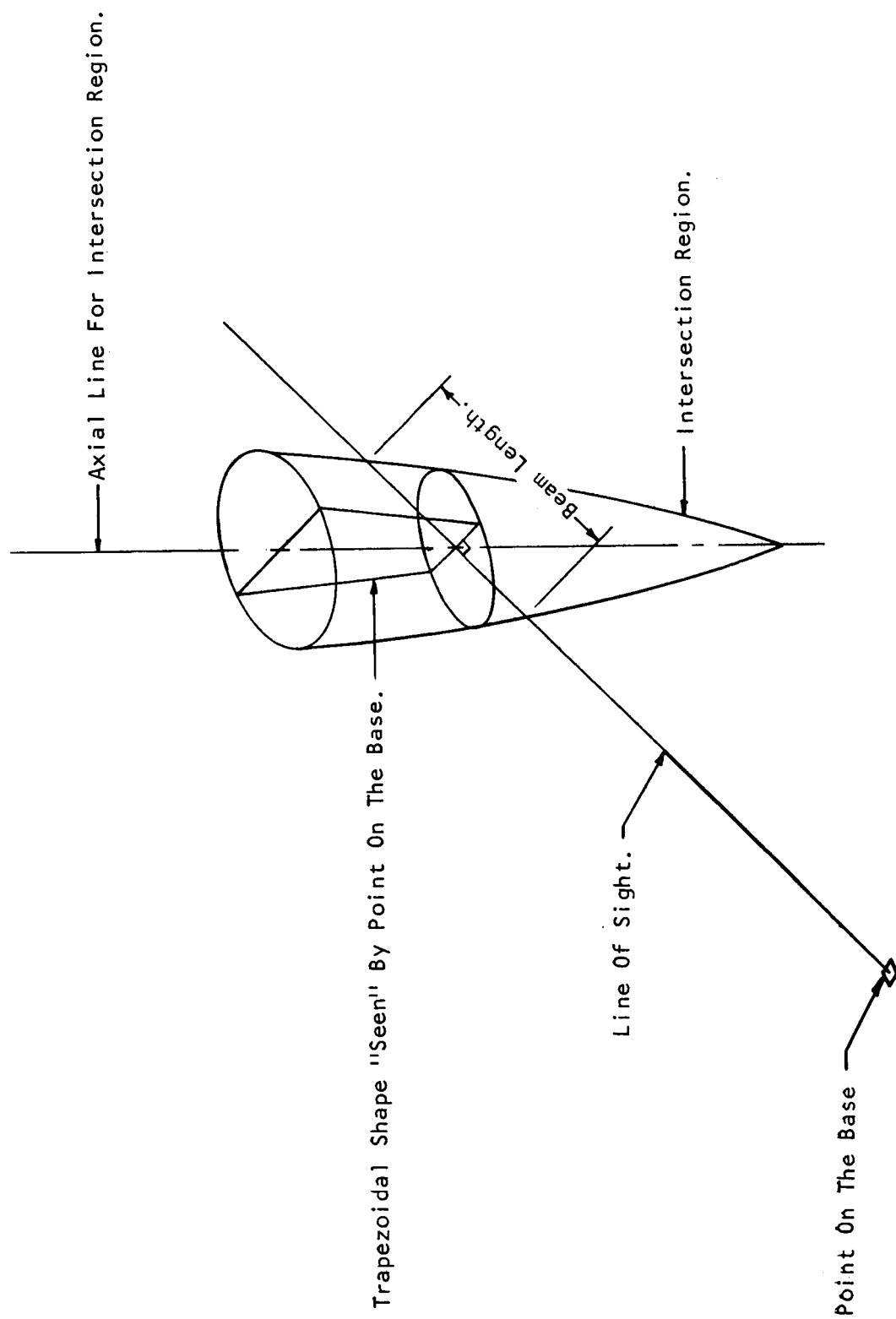


FIGURE 5. SKETCH OF TYPICAL INCREMENT RADIATING TO A POINT ON THE BASE

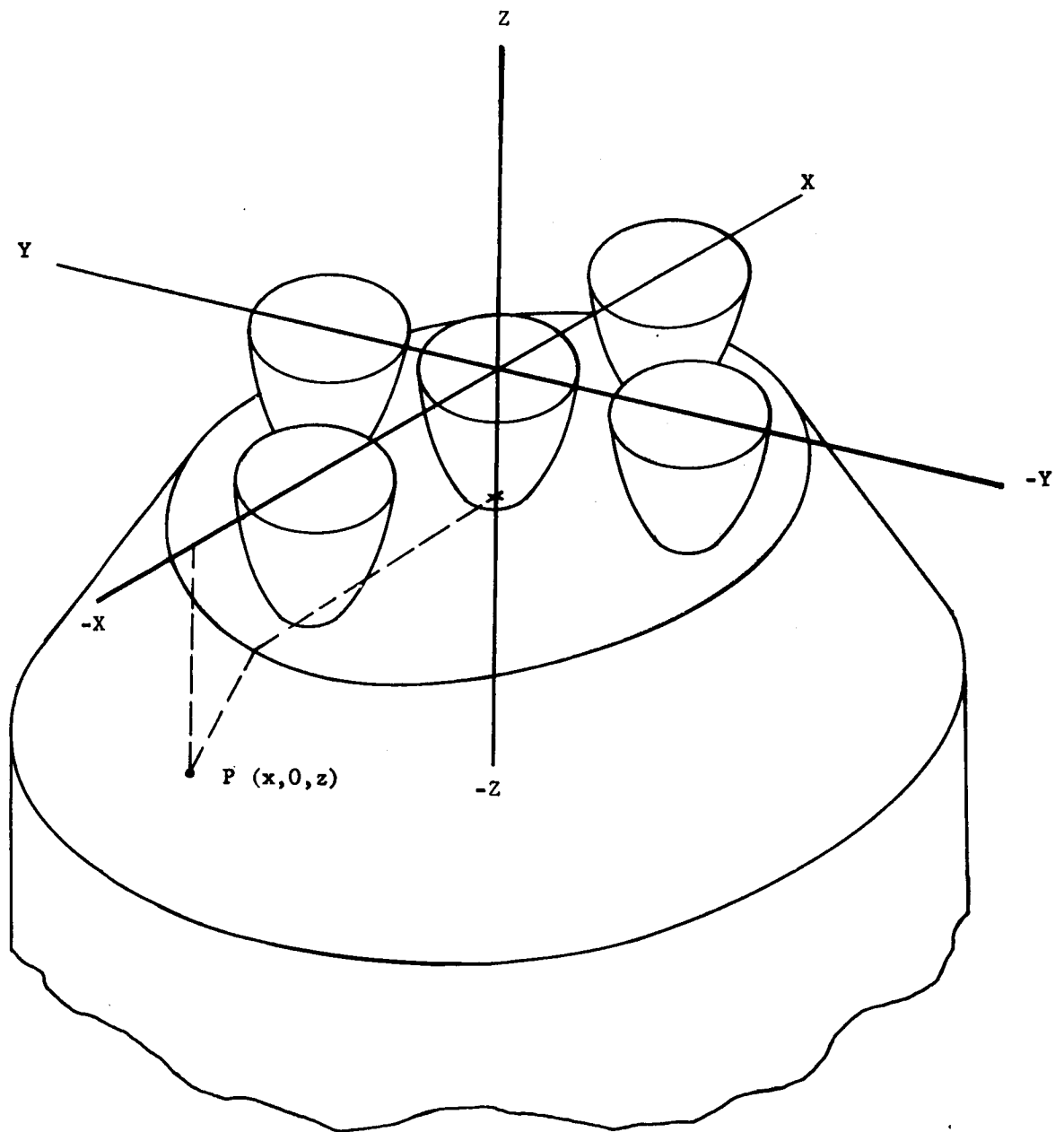


FIGURE 6. RIGHT-HANDED CARTESIAN COORDINATE SYSTEM USED TO LOCATE POINTS ON BASE

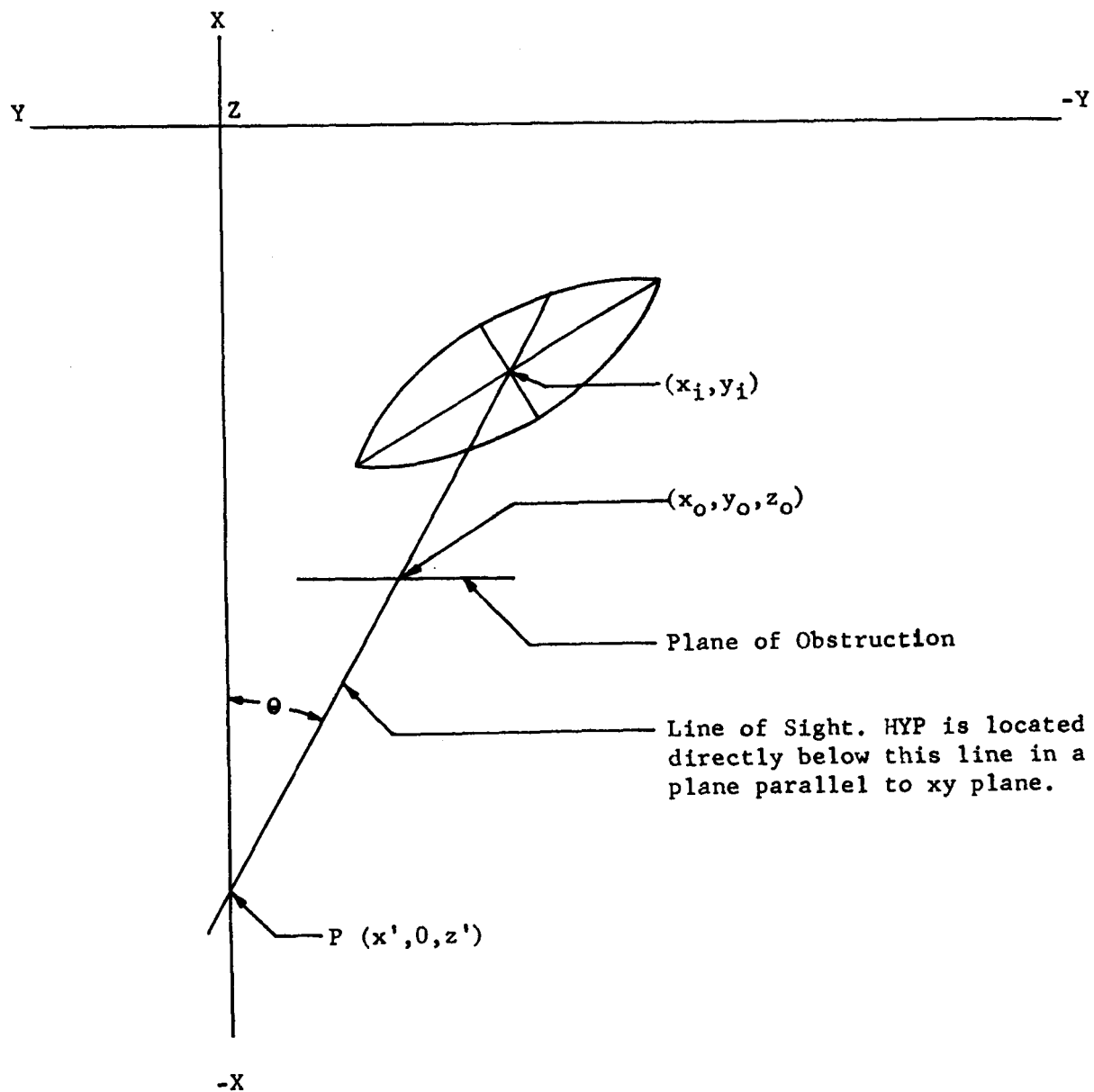


FIGURE 7. PLANE OF OBSTRUCTION GEOMETRY



START	CHAIN	*	SLEM	DASH	550110	13	FORTAN	04011
1			COMMON L,GAMMA, XD(60),FM(60),T(60),RU(60)					
			COMMON P(60),TEMP(60),BVIS(60),ADIS(60)					
			DIMENSION A(60,4),TABL(10),TAB(10),C(60)					
3			RCD,LL,L,MCON,R,PU,TU,GAMMA					
			RCD,PBPX					
			RCD,((A(I,J),I=1,LL),J=1,4)					006
			RCD,(XD(J),J=1,L)					007
			RCD,TABL					008
			RCD,TAB					009
			Q=2.					010
			PRINT 1					011
1			FORMAT(1H1,25X17HRADIATION PROGRAM//)					012
			PRINT 2					
2			FORMAT(27X9HCHAIN (1)///)					
			PRINT 1002,PBPX					013
1002			FORMAT(23X5HBPX=,F13.5//)					
			DO 204 J=1,L					015
			ARG=XD(J)					016
			DO 16 I=1,LL					017
			DATA=A(I,1)					018
			IF (DATA-ARG) 16,49,19					019
16			CONTINUE					020
			PRINT 216,ARG					021
			GO TO 204					022
19			IF (DATA-A(1,1)) 20,20,22					023
20			PRINT 218,ARG					024
			GO TO 204					025
22			DATAP=A(I-1,1)					026
			FUNC=(ARG-DATAP)/(DATA-DATAP)					027
			FMH=A(I,2)					028
			FML=A(I-1,2)					029
			IF (FMH-FML) 30,30,27					030
27			FMC=FUNC*(FMH-FML)					031
			FML(J)=FML+FMC					032
			GO TO 32					033
30			FMC=FUNC*(FML-FMH)					034
			FM(J)=FML-FMC					035
32			TH=A(I,3)					036
			TL=A(I-1,3)					037
			IF (TH-TL) 38,38,35					038
35			TC=FUNC*(TH-TL)					039
			T(J)=TL+TC					040
			GO TO 40					041
38			TC=FUNC*(TL-TH)					042
			T(J)=TL-TC					043
40			RDH=A(I,4)					044
			RDL=A(I-1,4)					045
			IF (RDH-RDL) 46,46,43					046
43			RDC=FUNC*(RDH-RDL)					047
			RD(J)=RDL+RDC					048
			GO TO 48					049
46			RDC=FUNC*(RDL-RDH)					050
			RD(J)=RDL-RDC					051
48			GO TO 52					052

FIGURE 8. RADIATION PROGRAM PRINTOUT

49	FM(J)=A(I,2)	053
	T(J)=A(I,3)	054
	RD(J)=A(I,4)	055
52	IF(1.6-GAMMA) 61,63,63	063
61	PRINT 220,GAMMA	064
	GO TO 71	066
63	DO 70 K=1,10	
	IF(TABL(K)-FM(J)) 70,7001,7001	068
70	CONTINUE	071
	PRINT 221	072
	GO TO 72	073
7001	IF(TAB(K)-T(J)) 71,76,76	074
71	PRINT 222	075
	PRINT 224	076
	IF(J-1) 78,78,72	
78	T(J)=A(1,3)	
72	IF (MCON) 74,74,73	077
73	MCON=0	078
74	DELTA=1.1344	079
	GO TO 145	080
76	AA=GAMMA+1.	081
	AC=FM(J)/Q	082
	AAA=GAMMA-1.	083
	BB=FM(J)**Q/Q	084
	CC=1./(GAMMA*FM(J)**Q)	085
	DELI=ASINF(1./FM(J))	086
	DLM=CC*(AA*AC**Q-1.+(AA*(1.+AAA*BB+AA*AC**4.))**.5)	087
	DELM=ASINF(DLM**.5)	088
	DDEL=DELM-DELI	089
	GO TO 100	090
99	DDEL=T(J)/THETA*DDEL	091
100	DELTA=DELI+DDEL	092
	THET=TANF(DELTA)*((AA*BB)/((FM(J)*SINF(DELTA))**Q-1.)-1.)	093
	THETA=ATANF(1./THET)	094
	IF(ABSF(THETA-T(J))-.0001) 145,145,120	095
120	GO TO 99	096
145	IF (MCON) 146,157,174	097
146	IF (J-1) 147,147,148	098
147	PRINT 207	099
148	CP=2.*SINF(T(J))**Q	100
	OPP=(CP*(GAMMA/Q)*FM**2.)+1.	101
	OPC=(GAMMA-1.)/Q	102
	OPD=1.+OPC*FM**Q	103
	OPE=OPD**((GAMMA/(GAMMA-1.))	104
	SAV=OPP/OPE	105
	P(J)=PO*SAV	106
	TEMP(J)=TO*SAV**((GAMMA-1.)/GAMMA)	107
	PRINT 208,XD(J),FM(J),T(J),P(J),TEMP(J)	
	GO TO 190	110
157	IF (J-1) 158,158,159	111
158	PRINT 210	112
159	CP=2.*SINF(T(J))**Q	113
	OPP=(CP*(GAMMA/Q)*FM**2.)+1.	114
	OPC=(GAMMA-1.)/Q	115
	OPD=1.+OPC*FM**Q	116

FIGURE 8. RADIATION PROGRAM PRINTOUT (Continued)

OPE=OPD**((GAMMA/(GAMMA-1.))	117
SAV=OPP/OPE	118
P(J)=PO*SAV	119
ALPHA=(GAMMA-1.)/(GAMMA+1.)	120
BETA=GAMMA*FM**Q*(SINF(T(J))**Q	121
VA=1.+ALPHA	122
VB=(GAMMA-1.)*FM**Q/Q	123
TEMP(J)=TO*((1.+BETA)*VA+ALPHA*(BETA+BETA**Q))/((1.+VB)*VA+BETA+VB	124
9*BETA)	125
PRINT 208,XD(J),FM(J),T(J),P(J),TEMP(J)	
GO TO 190	128
174 IF (J-1) 175,175,176	129
175 PRINT 212	130
176 X=(FM**Q)*((SINF(DELTA))**Q)	131
Y=Q*GAMMA	132
Z=GAMMA-1.	133
ZZ=GAMMA+1.	134
ZZZ=ZZ**Q	135
T2T1=(X*Y-Z)*(Z*X+Q)/(ZZZ*X)	136
XX=1.+(Z/Q)*(FM**2.)	137
T2TC=T2T1/XX	138
TEMP(J)=T2TC*TO	139
P2P1=(X*Y-Z)/ZZ	140
P2PC=P2P1/(XX**((GAMMA/Z))	141
P(J)=PO*P2PC	142
PRINT 208,XD(J),FM(J),T(J),P(J),TEMP(J)	
190 C(J)=DELTA-T(J)	
IF (J-1) 192,192,194	146
192 BDIS(J)=(TANF(C(J)))*(XD(J)-A(1,1))	
GO TO 195	148
194 BDIS(J)=BDIS(J-1)+ TANF(C(J-1))*(XD(J)-XD(J-1))	
195 ADIS(J)=SQRTF(RD(J)**Q-R**Q)	150
204 CONTINUE	152
205 PRINT 206	153
206 FORMAT(1H1)	154
207 FORMAT(10X50HISENTROPIC RELATIONS USED FOR TEMP AND P CALCULAT.//)	
208 FORMAT(23X8HXD(J)=,E13.5/,2X8HFM(J) =,E13.5,2X8HT(J) =,E13.5,	
92X8HP(J) =,E13.5,2X8HTEMP(J)=,E13.5///)	
210 FORMAT(10X46HRANKINE-HUGONIOT RELATIONS USED FOR TEMP AND P/	158
211 911HCALCULATION///)	159
212 FORMAT(10X49HOBLIQUE SHOCK RELATION USED FOR TEMP AND PRESSURE/	160
213 911HCALCULATION///)	161
216 FORMAT(25HXD VALUE EXCEEDS XD TABLE/	164
217 96HXD(J)=,E16.8///)	165
218 FORMAT(41HXD VALUE IS LOWER THAN LOWEST IN XD TABLE/	166
219 96HXD(J)=,E16.8///)	167
220 FORMAT(40HGAMMA EXCEEDS OBLIQUE SHOCK CAPABILITIES/	168
220196HGAMMA=,E16.8///)	169
221 FORMAT(33HFM(J) EXCEEDS OBLIQUE SHOCK TABLE///)	170
222 FORMAT(28HOBLIQUE SHOCK CANNOT BE USED/	171
223 926H SWITCH TO RANKINE-HUGONIOT///)	172
224 FORMAT(16HDELTA=65 DEGREES///)	173
225 CALL CHAIN (2)	174
226 END	175
* FORTRAN	

FIGURE 8. RADIATION PROGRAM PRINTOUT (Continued)

START	COMMON L,GAMMA, XD(60),FM(60),T(60),RU(60)	
CHAIN	COMMON P(60),TEMP(60),BDIS(60),ADIS(60)	
2	COMMON F(60),ANGLE(60),FLE(60),PH2U(60),FMISC,DIA,PHI,FXI	
	COMMON FK,SXD,QRAD(60)	
	DIMENSION RC(60),TUIS(60),AVIFM(60),FMIS(60),BLEU(60),AVP(60)	
	DIMENSION XDQ(60),FNRC(60)	
	RCD,DIA,FXI,XD(L+1)	
	RCD,FK,PHI,SXD	
	Q=2.	185
	VG=SINF(PHI)**Q	187
	VGG=COSE(PHI)**Q	188
	DO 2559 J=1,L	189
	VC=ADIS(J)*BDIS(J)	190
	VD=ADIS(J)**Q	191
	VE=BDIS(J)**Q	192
	RC(J)=VC*(SQRTF(1./((VE*VG+VD*VGG)))	193
	TDIS(J)=VC*(SQRTF(1./((VE*VGG+VD*VG)))	194
2559	CONTINUE	195
	PRINT 252	
	PRINT 426	
252	FORMAT(31X9HCHAIN (2)///)	
262	PRINT 263,FK,PHI	202
263	FORMAT(30X3HEK=,E12.5, /30X4HPHI=,E12.5//)	203
	DO 440 J=1,L	205
	PRINT 267,J	207
267	FORMAT(35X2HJ=,I3//)	208
	PRINT 269,XD(J)	209
269	FORMAT(30X6HXD(J)=,E13.5//)	
	IF (ABS(FK)-RC(J)) 285,271,275	
271	FLE(J)=50.0	213
	ANGLE(J)=1.570796327	214
	GO TO 297	215
275	UA=ABS(FK)-RC(J)	216
	UB=XD(J)+SXD	
	ANGLE(J)=ATANF(UB/UA)	218
	XDQ(J)=XD(J)+TANF(ANGLE(J))*RC(J)	219
	DO 281 I=J,L	220
	IF (XD(I)-XDQ(J)) 281,291,291	221
281	CONTINUE	222
	FLE(J)=(RC(J)+RC(L))/(COSE(ANGLE(J)))	224
	GO TO 294	225
285	FLE(J)=25.	227
	UB=XD(J)+SXD	
	UC=RC(J)-ABS(FK)	229
	ANGLE(J)=ATANF(UB/UC)	230
	GO TO 297	231
291	FNXD=XD(I)	232
	FNRC(J)=RC(I)	233
	FLE(J)=(RC(J)+FNRC(J))/(COSE(ANGLE(J)))	234
294	IF (FLE(J)-50.) 297,297,295	235
295	FLE(J)=50.	237
297	XDI=(SINF(ANGLE(J))*FLE(J)	238
	XDS=XD(J)+XDI	239
	DO 301 I=1,L	240
	IF (XD(I)-XDS) 301,314,314	241

FIGURE 8. RADIATION PROGRAM PRINTOUT (Continued)

301	CONTINUE	242
	CAREA=(TEMP(L)**4)*(XDS-XD(L))	
	N=L-1	243
	DO 310 KW=J,N	246
	IF (KW-J) 310,309,310	247
309	AREAC=0.	248
310	AREAC=AREAC+(TEMP(KW)**4)*(XD(KW+1)-XD(KW))	
	TOTA=AREAC+CAREA	250
	AVTEM(J)=TOTA/(XDS-XD(J))	251
	AVTEM(J)=AVTEM(J)**.25	
	GO TO 321	252
314	M=I-1	253
	DO 318 K=J,M	254
	IF (K-J) 318,317,318	255
317	AREAC=0.	256
318	AREAC=AREAC+(TEMP(K)**4)*(XD(K+1)-XD(K))	
	TOTA=AREAC	258
	AVTEM(J)=TOTA/(XD(I)-XD(J))	259
	AVTEM(J)=AVTEM(J)**.25	
321	IF (XD(L)-XDS) 322,331,331	260
322	CPRES=(P(L))*(XDS-XD(L))	261
	N=L-1	262
	DO 327 KW=J,N	263
	IF (KW-J) 327,326,327	264
326	AREAP=0.	265
327	AREAP=AREAP+(P(KW))*(XD(KW+1)-XD(KW))	266
	TOTP=AREAP+CPRES	267
	AVP(J)=TOTP/(XDS-XD(J))	268
	GO TO 338	269
331	MN=I-1	270
	DO 335 K=J,MN	271
	IF (K-J) 335,334,335	272
334	AREAP=0.	273
335	AREAP=AREAP+(P(K))*(XD(K+1)-XD(K))	274
	TOTP=AREAP	275
	AVP(J)=TOTP/(XD(I)-XD(J))	276
338	BLED(J)=(FLE(J))*DIA	277
	SIG2=1./SQRTF(FK**Q+(SXD+XD(J))**Q)	
	SIG3=1./SQRTF(FK**Q+(SXD+XD(J+1))**Q)	
	XXX=SIG2*(-Q*ATANF(TDIS(J)*SIG2))	280
	YYY=SIG3*(Q*ATANF(TDIS(J)*SIG3))	281
	F(J)=(FK/6.283185)*(XXX+YYY)	
	PH20(J)=FXI*AVP(J)	
	PL=PH20(J)*BLED(J)	
	IF (PL-.001) 3407,3390,3390	
3390	IF (PL-.02) 3391,3394,3394	
3391	IF (AVTEM(J)-2200.) 3392,3392,3393	
3392	A0=.6918E-2-.1035E-4*AVTEM(J)+.5908E-8*AVTEM(J)**2	
	9-.1221E-11*AVTEM(J)**3	
	A1=4.1462-.3099E-2*AVTEM(J)+.9596E-6*AVTEM(J)**2	
	9-.121E-9*AVTEM(J)**3	
	A2=-41.808+.2765E-1*AVTEM(J)-.243E-5*AVTEM(J)**2	
	9-.1E-8*AVTEM(J)**3	
	A3=175.61-.8474E-1*AVTEM(J)-.2372E-4*AVTEM(J)**2	
	9+.1303E-7*AVTEM(J)**3	

FIGURE 8. RADIATION PROGRAM PRINTOUT (Continued)

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      EMIS(J)=A0+A1*PL+A2*PL**2+A3*PL**3
      GO TO 3406
3393  A0=.1042E-2-.9582E-6*AVTEM(J)+.1574E-9*AVTEM(J)**2
      A1=2.524-.1088E-2*AVTEM(J)+.1197E-6*AVTEM(J)**2
      A2=-28.96+.1552E-1*AVTEM(J)-.1945E-5*AVTEM(J)**2
      EMIS(J)=A0+A1*PL+A2*PL**2
      GO TO 3406
3394  IF(PL-.1)3395,3395,3400
3395  IF(AVTEM(J)-2200.) 3396,3396,3397
3396  GO TO 3392
3397  IF(AVTEM(J)-3400.) 3398,3399,3399
3398  A0=.569E-2-.2627E-5*AVTEM(J)-.1168E-9*AVTEM(J)**2
      9+.8381E-13*AVTEM(J)**3
      A1=2.594-.1468E-2*AVTEM(J)+.3207E-6*AVTEM(J)**2
      9-.2583E-10*AVTEM(J)**3
      A2=-.7873-.2297E-2*AVTEM(J)+.9238E-6*AVTEM(J)**2
      9-.7605E-10*AVTEM(J)**3
      A3=-.8534E+2+.8458E-1*AVTEM(J)-.2441E-4*AVTEM(J)**2
      9+.2119E-8*AVTEM(J)**3
      EMIS(J)=A0+A1*PL+A2*PL**2+A3*PL**3
      GO TO 3406
3399  A0=.1052-.7318E-4*AVTEM(J)+.1645E-7*AVTEM(J)**2
      9-.1208E-11*AVTEM(J)**3
      A1=-2.299+.2014E-2*AVTEM(J)-.4971E-6*AVTEM(J)**2
      9+.3741E-10*AVTEM(J)**3
      A2=66.19-.4732E-1*AVTEM(J)+.1086E-4*AVTEM(J)**2
      9-.7985E-9*AVTEM(J)**3
      A3=-405.9+.2897*AVTEM(J)-.6701E-4*AVTEM(J)**2
      9+.5014E-8*AVTEM(J)**3
      EMIS(J)=A0+A1*PL+A2*PL**2+A3*PL**3
      GO TO 3406
3400  IF(PL-1.0) 3401,3401,3402
3401  A0=.1006-.1014E-3*AVTEM(J)+.4390E-7*AVTEM(J)**2
      9-.9089E-11*AVTEM(J)**3+.7098E-15*AVTEM(J)**4
      A1=.7705+.1016E-3*AVTEM(J)-.2288E-6*AVTEM(J)**2
      9+.6294E-10*AVTEM(J)**3-.5309E-14*AVTEM(J)**4
      A2=-1.1784-.3062E-3*AVTEM(J)+.5419E-6*AVTEM(J)**2
      9-.1516E-9*AVTEM(J)**3+.1289E-13*AVTEM(J)**4
      A3=.9306+.5489E-3*AVTEM(J)-.6685E-6*AVTEM(J)**2
      9+.1773E-9*AVTEM(J)**3-.1454E-13*AVTEM(J)**4
      A4=-.2717-.2979E-3*AVTEM(J)+.2938E-6*AVTEM(J)**2
      9-.7382E-10*AVTEM(J)**3+.5799E-14*AVTEM(J)**4
      EMIS(J)=A0+A1*PL+A2*PL**2+A3*PL**3+A4*PL**4
      GO TO 3406
3402  IF(PL-10.) 3403,3403,3404
3403  A0=.2814-.6083E-4*AVTEM(J)-.998E-8*AVTEM(J)**2
      9+.2684E-11*AVTEM(J)**3
      A1=+.9226E-1-.3216E-5*AVTEM(J)+.1709E-8*AVTEM(J)**2
      9-.8164E-12*AVTEM(J)**3
      A2=-.1176E-1+.3054E-5*AVTEM(J)-.1514E-8*AVTEM(J)**2
      9+.2766E-12*AVTEM(J)**3
      A3=.5398E-3-.1976E-6*AVTEM(J)+.9794E-10*AVTEM(J)**2
      9-.1646E-13*AVTEM(J)**3
      EMIS(J)=A0+A1*PL+A2*PL**2+A3*PL**3
      GO TO 3406

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FIGURE 8. RADIATION PROGRAM PRINTOUT (Continued)

3404	IF (PL-100.) 3405,3405,3408	
3405	A0=.61295-.1101E-3*AVTEM(J)+.4088E-8*AVTEM(J)**2	
	A1=.5569E-2-.8151E-8*AVTEM(J)-.9138E-10*AVTEM(J)**2	
	A2=-.2578E-4-.8615E-9*AVTEM(J)+.5913E-12*AVTEM(J)**2	
	EMIS(J)=A0+A1*PL+A2*PL**2	
	GO TO 3406	
3407	PRINT 430	
	GO TO 440	
3408	PRINT 431	
	GO TO 440	
3406	SAVE=F(J)*(4.7611E-13)*EMIS(J)*AVTEM(J)**4.	285
	IF (J-1) 350,348,350	286
348	GRADS=0.	287
	SSF=0.	288
350	GRADS=SAVE+GRADS	
	SSF=F(J)+SSF	
	PRINT 425,BLED(J),AVTEM(J),PH20(J),SSF,EMIS(J)	
	QRAD(J)=SAVE	
	PRINT 427,QRAD(J),QRADS	
425	FORMAT(5H BLED=,E13.5,2X6H AVTEM=,E13.5,2X5H PH20=,E13.5,	
	92X4H SSF=,E13.5,2X5H EMIS=,E13.5//)	
427	FORMAT(15X5H QRAD=,E13.5,4X6H QRADS=,E13.5//)	
440	CONTINUE	
	PRINT 426	
426	FORMAT(1H ,20X21H Q BY AVT + AVP METHOD//)	
	PRINT 4083,GRADS	
4083	FORMAT(127H TOTAL RADIANT HEAT FLUX IS E16.8,2X13H BTU/SEC=SQ FT//)	
414	PRINT 415	353
415	FORMAT(1H )	354
430	FORMAT(10X50H PL IS LESS THAN .001 FT-ATM - PROGRAM WILL DISCARD//)	
431	FORMAT(10X49H PL GREATER THAN 100 FT-ATM - PROGRAM WILL DISCARD//)	
	CALL CHAIN (3)	
START	END	368
CHAIN	* FORTRAN	
3	COMMON L,GAMMA, XD(60),FM(60),T(60),RU(60)	
	COMMON P(60),TEMP(60),BDIS(60),ADIS(60)	
	COMMON F(60),ANGLE(60),FLE(60),PH20(60),EMISC,DIA,PH1,FX1	
	COMMON FK,SXD,QRAD(60),QRDA(60)	
	DIMENSION VAL(51)	
	DO 416 J=1,L	
	IF (J-1) 350,351,350	
351	PRINT 352	
352	FORMAT(27X9H CHAIN (3)//)	
	PRINT 4082	
350	ABSI=(FLE(J))/50.	296
	CN=ABSI*SINF(ANGLE(J))	297
	DO 3960 I=1,51	
	IF (I-1) 361,361,365	299
361	CR=XD(J)	300
	CI=I	301
	SABSI=ABSI*CI*DIA	302
	GO TO 369	303
365	CI=I	304
	AI=CI-1.	305
	SABSI=ABSI*CI*DIA	

FIGURE 8. RADIATION PROGRAM PRINTOUT (Continued)

	CR=CN*AI+XD(J)	307
369	DO 392 K=1,L	308
	IF(CR-XD(K)) 374,371,392	309
371	TW=TEMP(K)	310
	PW=P(K)	311
	GO TO 395	312
374	FUNT=(CR-XD(K-1))/(ABS(XD(K)-XD(K-1)))	313
	QTH=TEMP(K)	314
	QTL=TEMP(K-1)	315
	IF(QTH-QTL) 381,381,378	316
378	TE=FUNT*(QTH-QTL)	317
	TW=QTL+TE	318
	GO TO 383	319
381	TE=FUNT*(QTL-QTH)	320
	TW=QTL-TE	321
383	QPH=P(K)	322
	QPL=P(K-1)	323
	IF(QPH-QPL) 389,389,386	324
386	PC=FUNT*(QPH-QPL)	325
	PW=QPL+PC	326
	GO TO 395	327
389	PC=FUNT*(QPL-QPH)	328
	PW=QPL-PC	329
	GO TO 395	330
392	CONTINUE	331
	TW=TEMP(L)	332
	PW=P(L)	333
395	POW=FXI*PW	
	POWL=POW*SABSI	
3950	IF(POWL-.02) 3953,3954,3954	
3953	IF(TW-2200.) 3956,3956,3957	
3956	A1=4.1462-.3099E-2*TW+.9596E-6*TW**2-.121E-9*TW**3	
	A2=-41.808+.2765E-1*TW-.243E-5*TW**2-.10E-8*TW**3	
	A3=175.61-.8474E-1*TW-.2372E-4*TW**2+.1303E-7*TW**3	
	VAL(I)=A1*POW+2.*A2*(POW**2)*SABSI+3.*A3*(POW**3)*(SABSI**2)	
	GO TO 3960	
3957	A1=2.524-.1088E-2*TW+.1197E-6*TW**2	
	A2=-28.96+.1552E-1*TW-.1945E-5*TW**2	
	VAL(I)=A1*POW+2.*A2*(POW**2)*SABSI	
	GO TO 3960	
3954	IF(POWL-.1) 3959,3959,3961	
3959	IF(TW-2200.) 3962,3962,3963	
3962	GO TO 3956	
3963	IF(TW-3400.) 3964,3965,3965	
3964	A1=2.294-.1468E-2*TW+.3207E-6*TW**2-.2582E-10*TW**3	
	A2=-.7073+.2297E-2*TW+.9258E-6*TW**2-.7605E-10*TW**3	
	A3=-.8534E+2+.8458E-1*TW-.2441E-4*TW**2+.2119E-8*TW**3	
	VAL(I)=A1*POW+2.*A2*(POW**2)*SABSI+3.*A3*(POW**3)*(SABSI**2)	
	GO TO 3960	
3965	A1=-2.299+.2014E-2*TW-.4971E-6*TW**2+.3741E-10*TW**3	
	A2=66.19-.4732E-1*TW+.1086E-4*TW**2-.7985E-9*TW**3	
	A3=-405.9+.2897*TW-.0701E-4*TW**2+.5014E-8*TW**3	
	VAL(I)=A1*POW+2.*A2*(POW**2)*SABSI+3.*A3*(POW**3)*(SABSI**2)	
	GO TO 3960	
3961	IF(POWL-1.0) 3966,3966,3967	

FIGURE 8. RADIATION PROGRAM PRINTOUT (Continued)



```

3966 A1=.7705+.1016E-3*TW-.2288E-6*TW**2+.6294E-10*TW**3
9-.5309E-14*TW**4
A2=-.1.1784-.3062E-3*TW+.5419E-6*TW**2-.1516E-9*TW**3
9+.1289E-13*TW**4
A3=.9306+.5489E-3*TW-.6685E-6*TW**2+.1775E-9*TW**3
9-.1454E-13*TW**4
A4=-.2717-.2979E-3*TW+.2938E-6*TW**2-.7302E-10*TW**3
9+.5799E-14*TW**4
VAL(I)=A1*POW+2.*A2*(POW**2)*SABSI5+3.*(POW**3)*(SABSI5**2)
9+4.*A4*(POW**4)*(SABSI5**3)
GO TO 3960
3967 IF(POWL-10.) 3968,3968,3969
3968 A1+.9226E-1-.3210E-3*TW+.1709E-8*TW**2-.6164E-12*TW**3
A2=-.1176E-1+.3054E-3*TW-.1514E-6*TW**2+.2766E-12*TW**3
A3=.5398E-3-.1976E-6*TW+.9794E-10*TW**2-.1646E-13*TW**3
VAL(I)=A1*POW+2.*A2*(POW**2)*SABSI5+3.*A3*(POW**3)*(SABSI5**2)
GO TO 3960
3969 A1=.5569E-2-.8151E-6*TW-.9136E-10*TW**2
A2=-.2578E-4-.8615E-9*TW+.5913E-12*TW**2
VAL(I)=A1*POW+2.*A2*(POW**2)*SABSI5
3960 VAL(I)=VAL(I)*TW**4
DO 400 M=2,50,2
IF(M-2) 399,399,400
399 WE=0.
400 WE=WE+VAL(M)
DO 404 M=1,51,2
IF(M-1) 401,403,404
403 YOU=0.
404 YOU=YOU+VAL(M)
F=F(J)
SAVE=ABSIS*4.7611E-13*F* (-VAL(I)+4.*WE+2.*YOU-VAL(51))/3.
IF(J-1) 408,407,408
407 QRDAS=0.
408 QRDAS=SAVE+QRDAS
PRINT 426,J,XD(J)
426 FORMAT(30X2HJ=,I3/,22X6HXD(J)=,E15.5//)
QRDA(J)=SAVE
PRINT 427, QRDA(J),QRDAS
427 FORMAT(15X5HQRDA=,E12.5,4X6HQRDAS=,E12.5//)
416 CONTINUE
PRINT 4082
4082 FORMAT(20X30HHEAT FLUX BY ABSORPTION METHOD/)
PRINT 4083, QRDAS
4083 FORMAT(27HTOTAL RADIANT HEAT FLUX IS E16.8,2X13HBTU/SEC-SQ FT//)
PRINT 415
415 FORMAT(1H1)
CALL CHAIN(4)
421 CONTINUE
END
*
FORTRAN
DIMENSION A(40,4),TDIS(60)
COMMON L,GAMMA,XD(60),FM(60),T(60),RD(60)
COMMON P(60),TEMP(60),DUI5(60),ADIS(60)
COMMON F(60),ANGLE(60),FLE(60),PH20(60),EMISC,DIA,PHI,FXI
COMMON FX,SXD,QRAD(60),QRDA(60)

```

FIGURE 8. RADIATION PROGRAM PRINTOUT (Continued)

```

RCD,LLLL,FINTX,FINTY
RCD,((A(I,J),I=1,LLLL),J=1,4)
RCD,FLAG,PX
PRINT 252
PRINT 253
252 FORMAT (27X9HCHAIN (4)//)
253 FORMAT (17X27HBLOCKAGE CORRECTION FACTORS//)
IF (PX) 32,32,100
100 SI=ASINF(ABSF(FINTY/(FK*DIA)))
XP=(COSF(SI))*(ABSF(FK))*DIA
IF(XP-FINTX)30,31,31
31 PX=(XP-FINTX)*(-1.)
GO TO 32
30 PX=(XP+FINTX)*(-1.)
32 PY=0.
PZ=(-1.)*SXD*DIA
DO 69 J=1,L
Q=2.
VG=SINF(PHI)**Q
VGG=COSF(PHI)**Q
VC=ADIS(J)*BDIS(J)
VD=ADIS(J)**Q
VE=BDIS(J)**Q
TDIS =VC*(SQRTF(1./((VE*VGG+VD*VG)))
RC=VC*(SQRTF(1./((VE*VG+VD*VGG)))
XCOR=TDIS*(SINF(SI))*DIA
YCOR=TDIS*(COSE(SI))*DIA
PRINT 999,J
999 FORMAT (24X2HJ=,I3//)
YR=FINTY-YCOR
YL=FINTY+YCOR
IF(FINTY)26,27,27
26 XR=FINTX-XCOR
XL=FINTX+XCOR
GO TO 28
27 XR=FINTX+XCOR
XL=FINTX-XCOR
28 CONTINUE
DO 49 K=1,3
IF(K-1)21,21,22
22 IF(K-2)21,23,24
24 IF(K-3)21,25,25
21 PRINT 29
29 FORMAT(19HLEFT SIDE OF REGION//)
998 FLY=0.0
AINTX=XL-PX
AINTY=YI
GO TO 40
23 PRINT 41
41 FORMAT(16HMIDDLE OF REGION//)
AINTX=FINTX-PX
AINTY=FINTY
GO TO 40
25 PRINT 42
42 FORMAT(20HRIGHT SIDE OF REGION//)

```

FIGURE 8. RADIATION PROGRAM PRINTOUT (Continued)

```

      AINIX=XR-PX
      AINTY=YR
40    THETA=ATANF(ABSF(AINTY)/(AINIX-PX))
      DO 79 LI=1,LLLL
      ZO=A(LI,3)*PZ
      IF (K-2) 70,71,70
70    FFF=(SQRT(FFK**2.+IDIS**2.))
      HYP=ZO*(FFF/(SXD+XD(J)))
      GO TO 72
71    HYP=ZO*((ABSF(FK)-RC)/(SXD+XD(J)))
72    XO=(COSE(THETA))*HYP
      YO=(SINF(THETA))*HYP
      IF (AINIX) 50,50,51
50    XO=-1.*XO
51    IF (AINTY) 10,10,11
      10 YO=-1.*YO
      11 H=A(LI,1)
      PRINT 1002,XO,YO
1002  FORMAT (3HXO=,E16.8,2X3HYO=,E16.8//)
      FFK=A(LI,2)
      RADIUS=A(LI,4)
      EQN=(XO+PX-H)**2.+(YO-FFK)**2.
      SADIUS=RADIUS**2.
      IF (SADIUS-EQN) 79,49,49
79    CONTINUE
      1 FLY=1.+FLY
49    CONTINUE
      QRAD(J)=QRAD(J)*FLY/3.
      QRDA(J)=QRDA(J)*FLY/3.
      5 QRADS=QRADS+QRAD(J)
      QRDAS=QRDAS+QRDA(J)
      PRINT 1005,QRAD(J),QRADS
      PRINT 1006,QRDA(J),QRDAS
1005  FORMAT (5HQRAD=,E16.8,2X6HQRADS=,E16.8//)
1006  FORMAT (5HQRDA=,E16.8,2X6HQRDAS=,E16.8//)
      69 CONTINUE
      PRINT 4038,QRADS,QRDAS
4038  FORMAT (29HWITH BLOCKAGE CORRECTION,THE
      946HRADIATIVE FLUX BY THE AVT. AND AVP. METHOD IS E16.8,2X3HBTU
      910H/SEC-SQ FT/
      932HBY THE ABSORPTION METHOD, IT IS E16.8///)
      PRINT 5000
5000  FORMAT (1H1)
      IF (FLAG) 419,420,419
420  CALL CHAIN (1)
      GO TO 421
419  CALL CHAIN (2)
421  CONTINUE
      END

```

FIGURE 8. RADIATION PROGRAM PRINTOUT (Concluded)

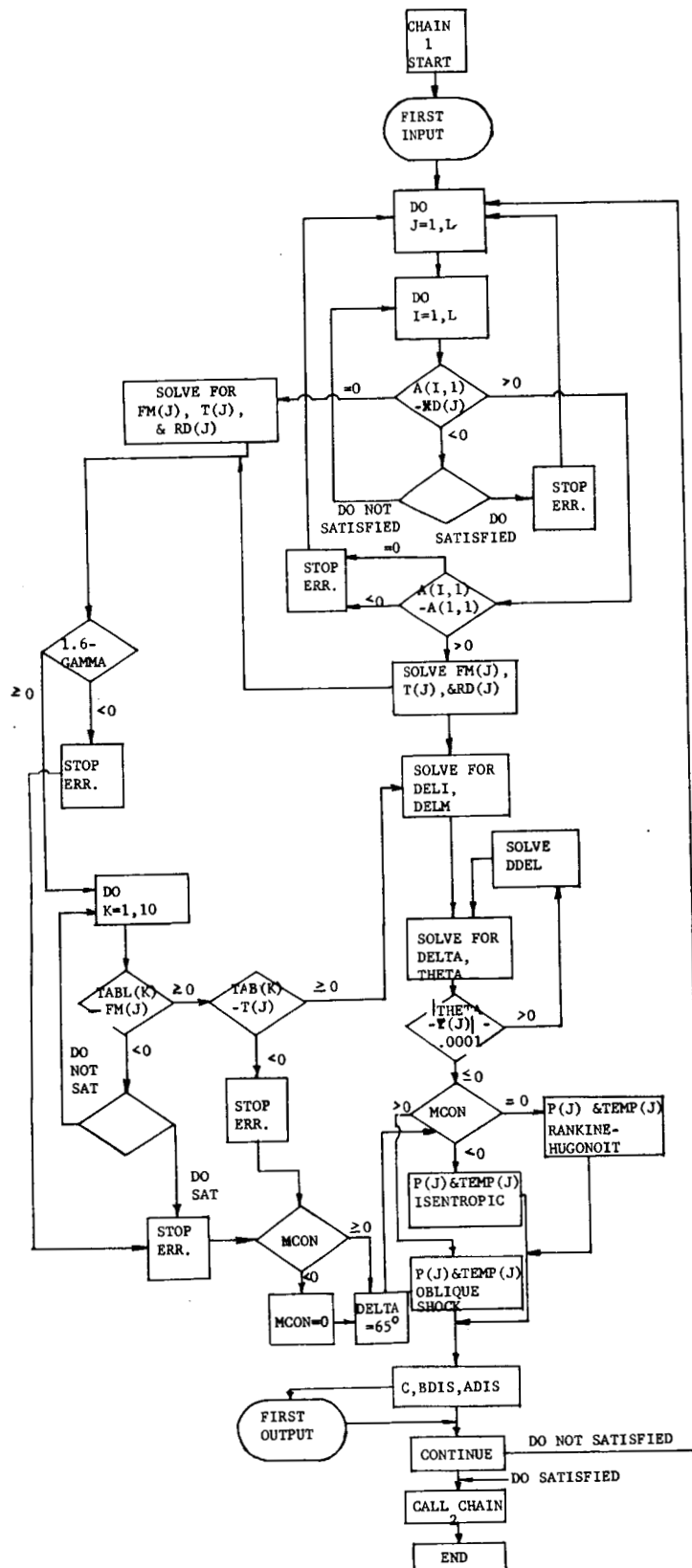


FIGURE 9. FLOW DIAGRAM

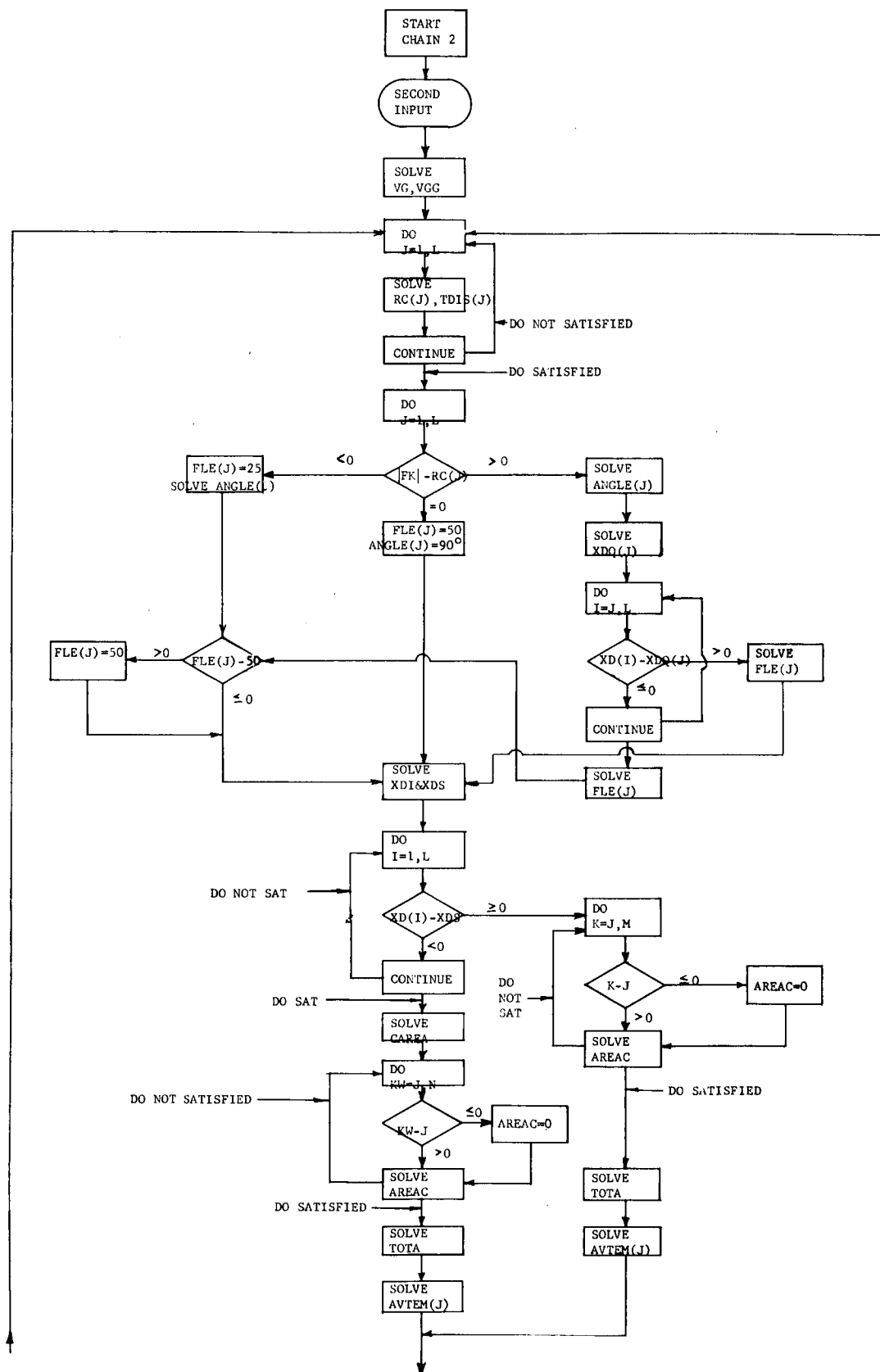


FIGURE 9. FLOW DIAGRAM (Continued)

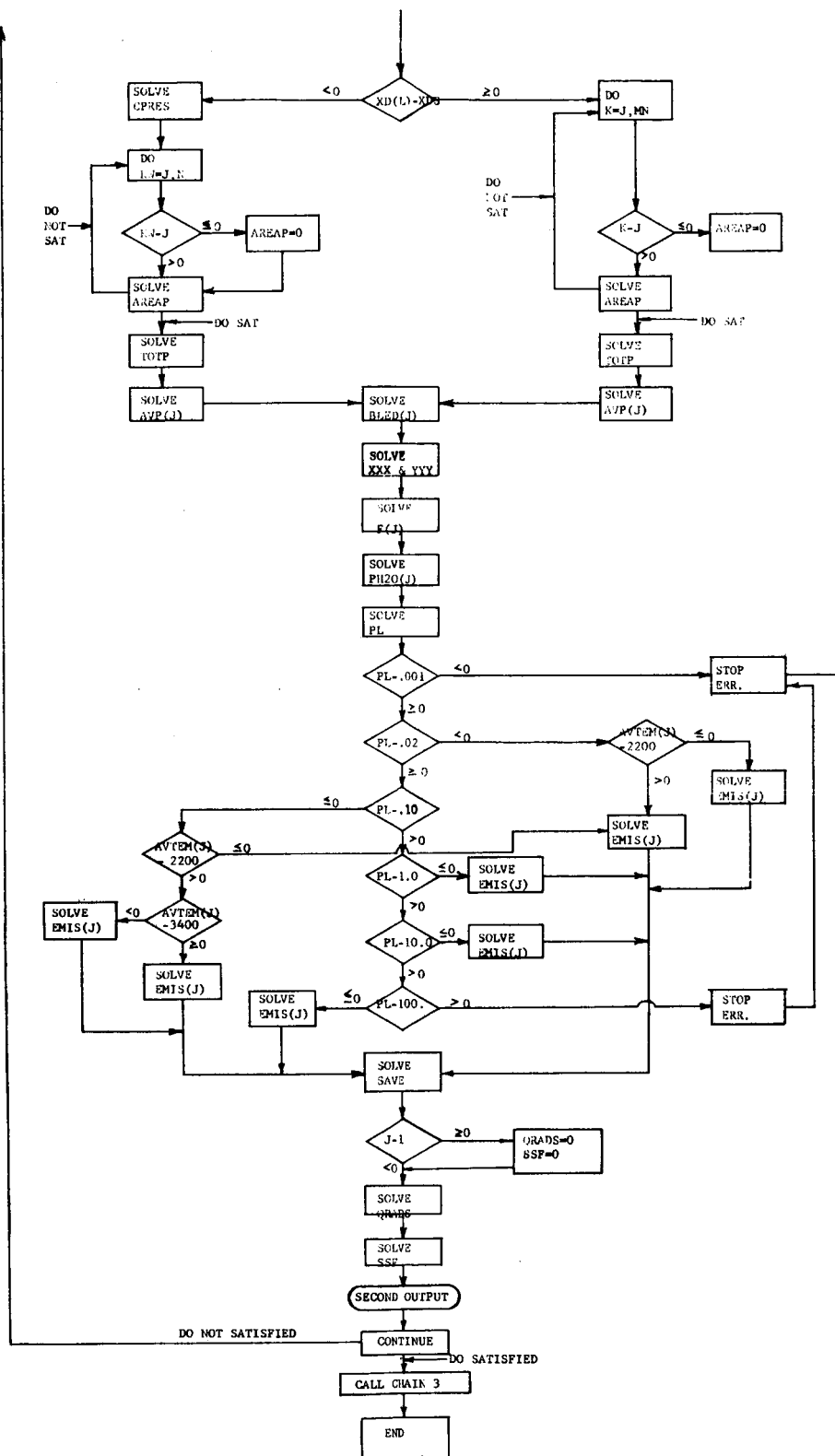


FIGURE 9. FLOW DIAGRAM (Continued)

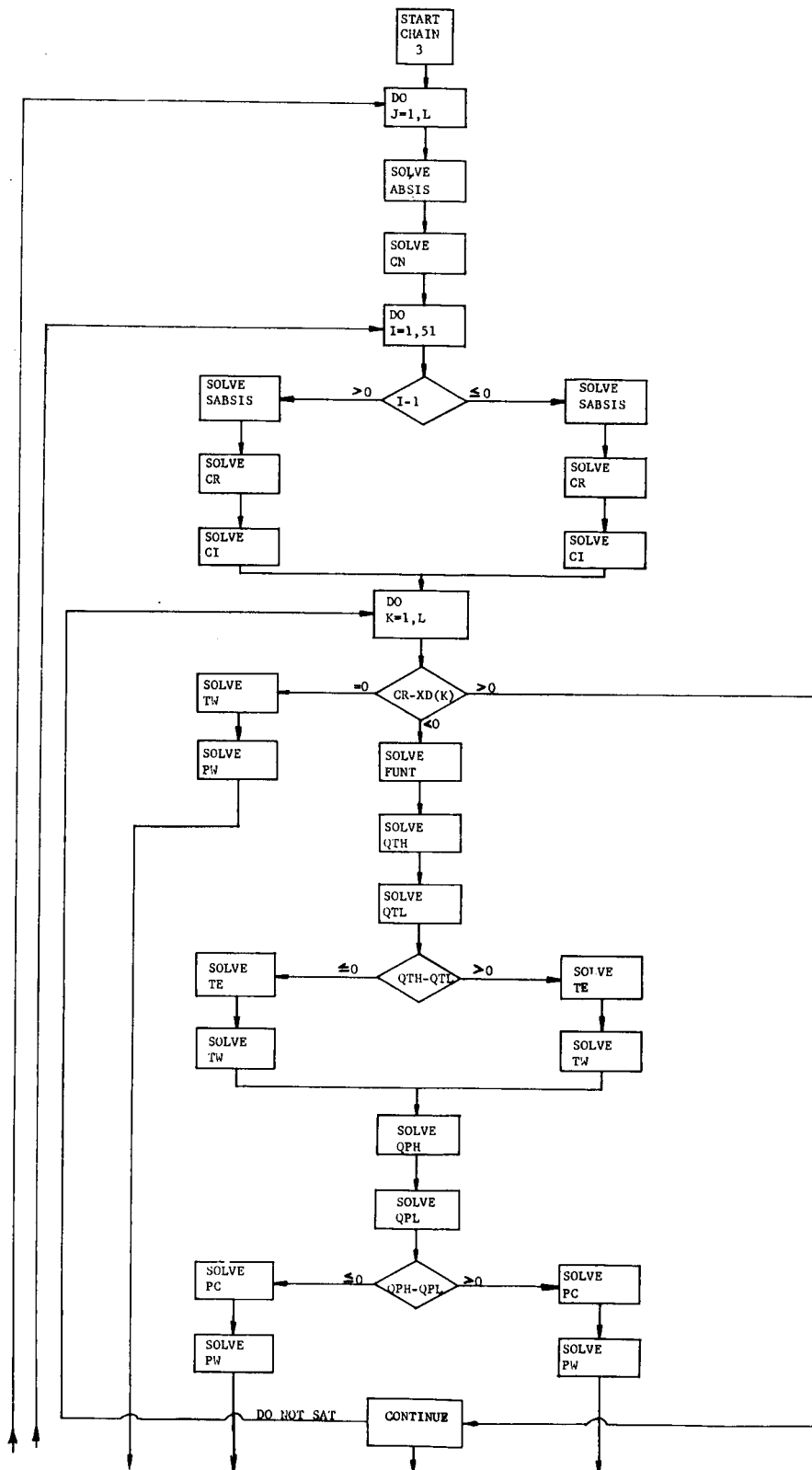


FIGURE 9. FLOW DIAGRAM (Continued)

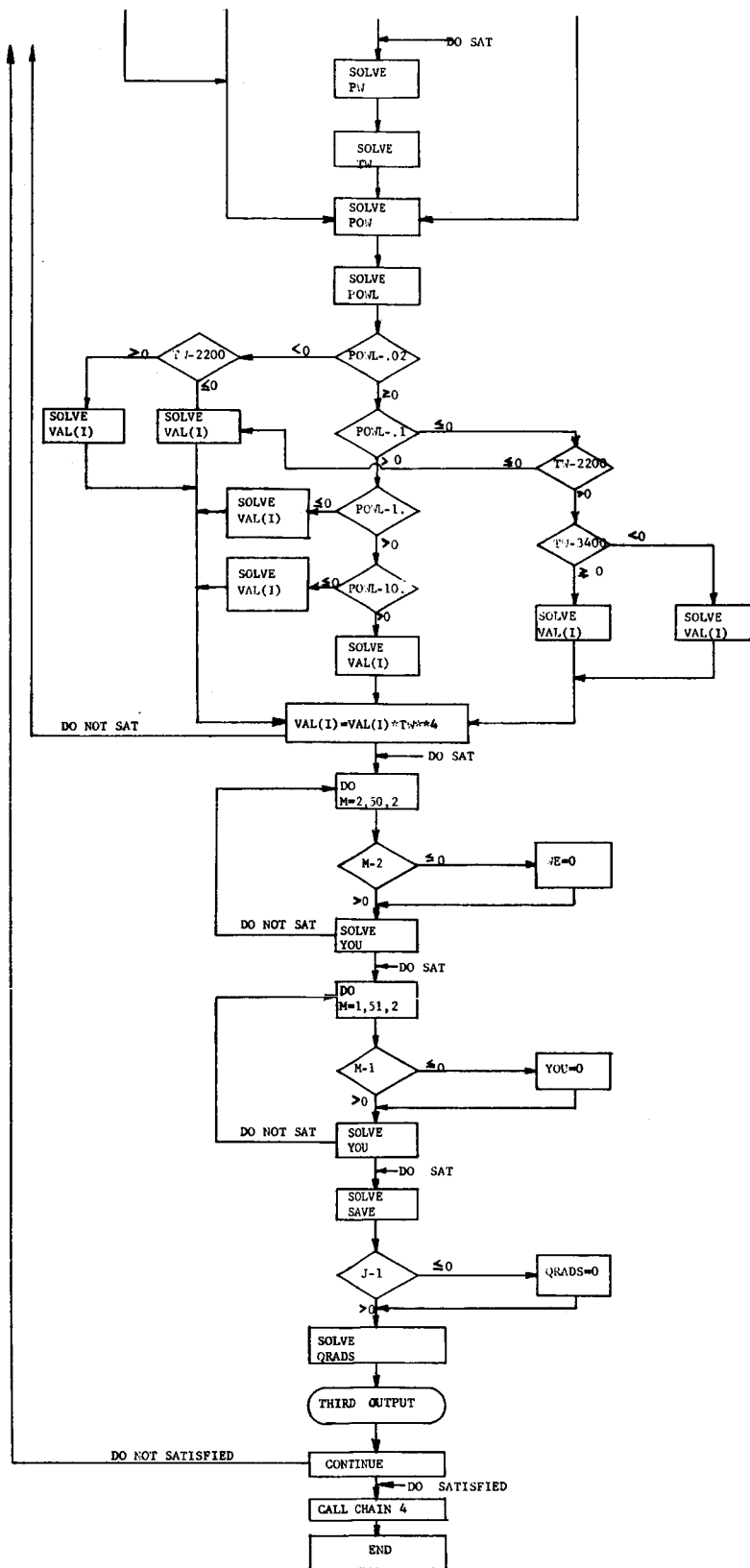


FIGURE 9. FLOW DIAGRAM (Continued)



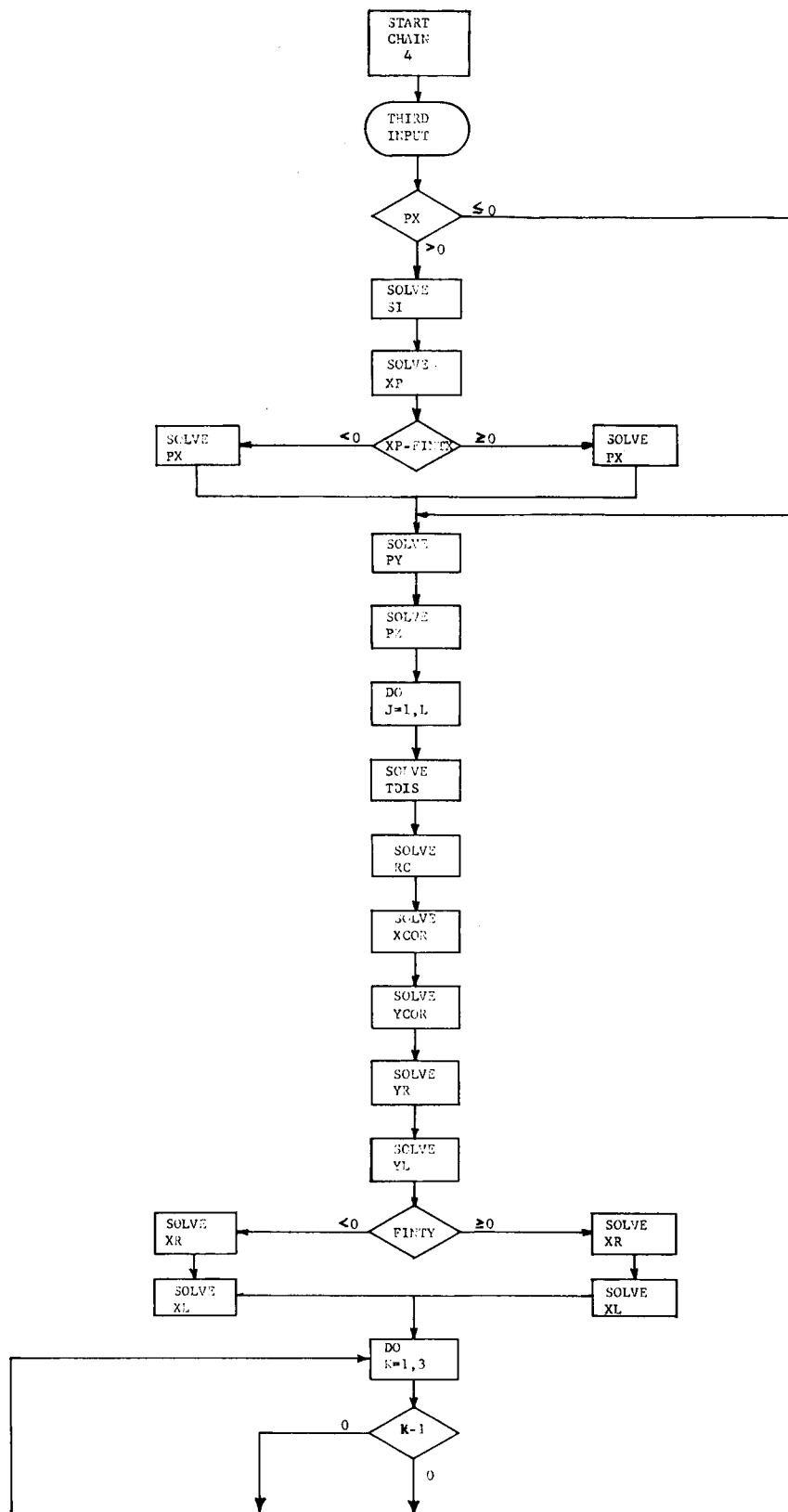


FIGURE 9. FLOW DIAGRAM (Continued)

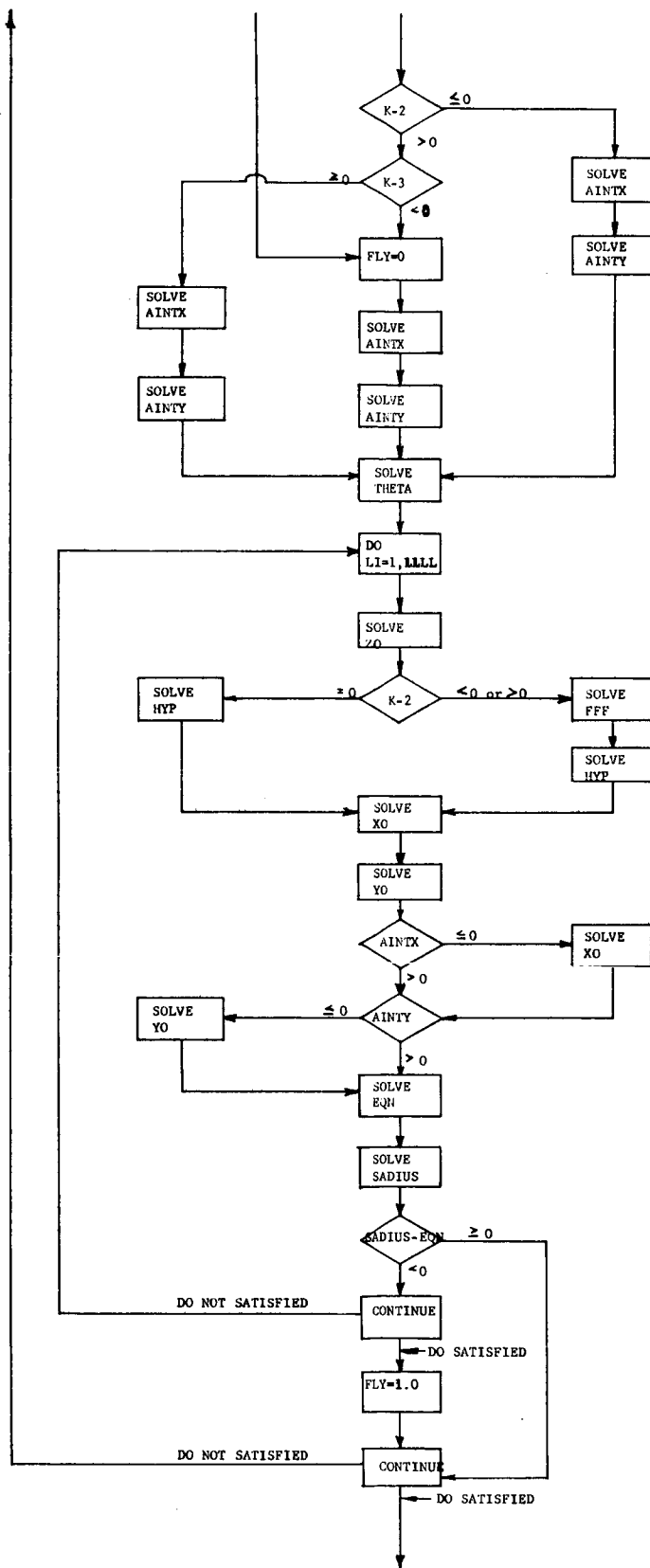


FIGURE 9. FLOW DIAGRAM (Concluded)

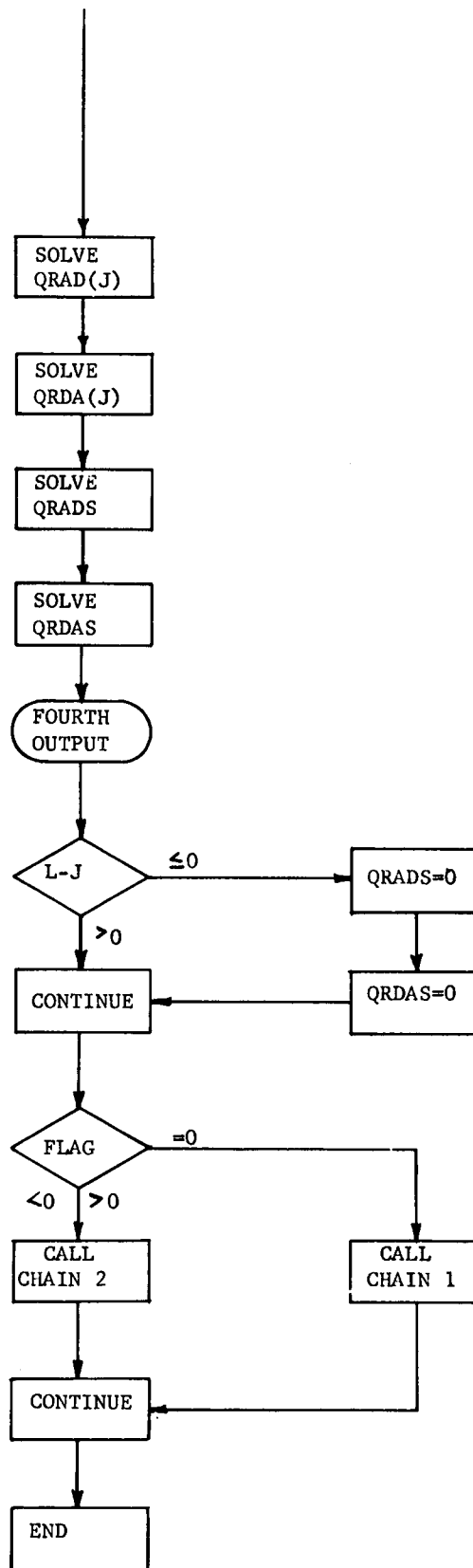


FIGURE 9. FLOW DIAGRAM (Continued)

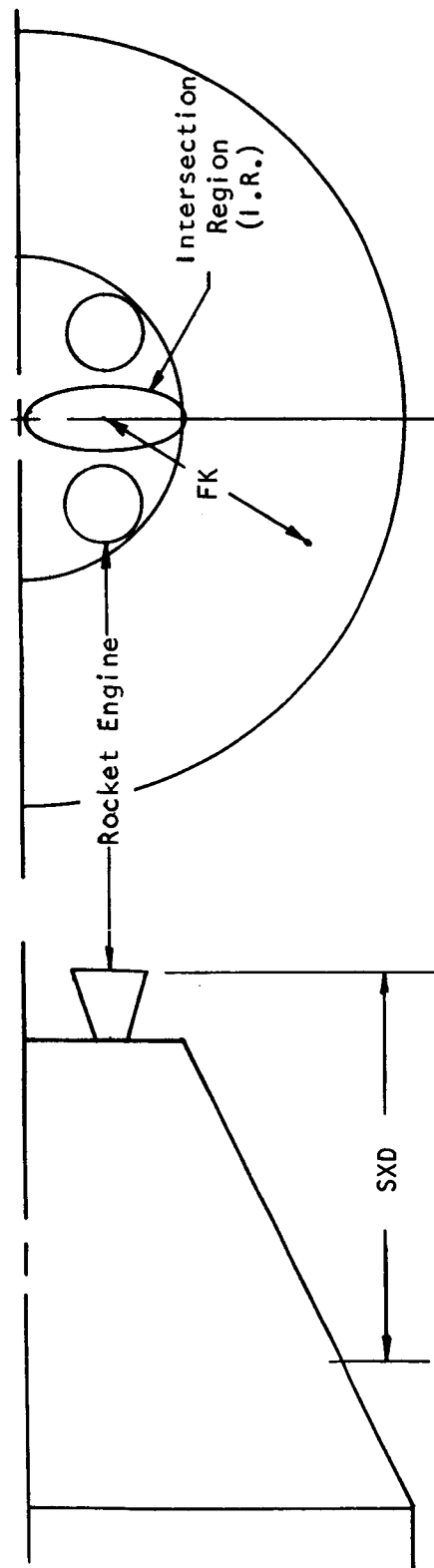


FIGURE 10. BASE GEOMETRY

## RADIATION PROGRAM

CHAIN (1)

PBPX= 0.18500E-01

OBLIQUE SHOCK RELATION USED FOR TEMP AND PRESSURE  
CALCULATION

FM(I) = 0.5567E 01	XD(I) = 0.56000E 00	TI(I) = 0.60096E 00	PI(I) = 0.20421E-00	TEMP(I) = 0.33161E 04
FM(I) = 0.5664E 01	XD(I) = 0.60000E 00	TI(I) = 0.61031E 00	PI(I) = 0.20820E-00	TEMP(I) = 0.33569E 04
FM(I) = 0.41041E 01	XD(I) = 0.70000E 00	TI(I) = 0.69094E 00	PI(I) = 0.24993E-00	TEMP(I) = 0.37720E 04
FM(I) = 0.40154E 01	XD(I) = 0.80000E 00	TI(I) = 0.64355E 00	PI(I) = 0.22298E-00	TEMP(I) = 0.35075E 04
FM(I) = 0.58791E 01	XD(I) = 0.90000E 00	TI(I) = 0.58994E 00	PI(I) = 0.19527E-00	TEMP(I) = 0.32248E 04
FM(I) = 0.58247E 01	XD(I) = 0.10000E 01	TI(I) = 0.55144E 00	PI(I) = 0.17597E-00	TEMP(I) = 0.30278E 04
FM(I) = 0.57751E 01	XD(I) = 0.11000E 01	TI(I) = 0.51744E 00	PI(I) = 0.15943E-00	TEMP(I) = 0.29887E 04
FM(I) = 0.57264E 01	XD(I) = 0.12000E 01	TI(I) = 0.48813E 00	PI(I) = 0.14597E-00	TEMP(I) = 0.27210E 04
FM(I) = 0.5712E 01	XD(I) = 0.13000E 01	TI(I) = 0.46271E 00	PI(I) = 0.13445E-00	TEMP(I) = 0.26030E 04
FM(I) = 0.56964E 01	XD(I) = 0.14000E 01	TI(I) = 0.44055E 00	PI(I) = 0.12481E-00	TEMP(I) = 0.25041E 04
FM(I) = 0.56900E 01	XD(I) = 0.15000E 01	TI(I) = 0.42092E 00	PI(I) = 0.11632E-00	TEMP(I) = 0.24168E 04
FM(I) = 0.56901E 01	XD(I) = 0.16000E 01	TI(I) = 0.40324E 00	PI(I) = 0.10919E-00	TEMP(I) = 0.23435E 04
FM(I) = 0.56914E 01	XD(I) = 0.17000E 01	TI(I) = 0.38724E 00	PI(I) = 0.10277E-00	TEMP(I) = 0.22773E 04
FM(I) = 0.57004E 01	XD(I) = 0.18000E 01	TI(I) = 0.37374E 00	PI(I) = 0.97241E-01	TEMP(I) = 0.22202E 04
FM(I) = 0.57047E 01	XD(I) = 0.19000E 01	TI(I) = 0.36110E 00	PI(I) = 0.92610E-01	TEMP(I) = 0.21723E 04
FM(I) = 0.57051E 01	XD(I) = 0.20000E 01	TI(I) = 0.34974E 00	PI(I) = 0.88419E-01	TEMP(I) = 0.21289E 04
FM(I) = 0.57143E 01	XD(I) = 0.21000E 01	TI(I) = 0.34014E 00	PI(I) = 0.84880E-01	TEMP(I) = 0.20922E 04
FM(I) = 0.5717E 01	XD(I) = 0.22000E 01	TI(I) = 0.33151E 00	PI(I) = 0.81806E-01	TEMP(I) = 0.20602E 04
FM(I) = 0.5718E 01	XD(I) = 0.23000E 01	TI(I) = 0.32490E 00	PI(I) = 0.79513E-01	TEMP(I) = 0.20364E 04
FM(I) = 0.5707E 01	XD(I) = 0.24000E 01	TI(I) = 0.32379E 00	PI(I) = 0.79221E-01	TEMP(I) = 0.20333E 04
FM(I) = 0.5711E 01	XD(I) = 0.25000E 01	TI(I) = 0.32214E 00	PI(I) = 0.78626E-01	TEMP(I) = 0.20271E 04
FM(I) = 0.57195E 01	XD(I) = 0.26000E 01	TI(I) = 0.30942E 00	PI(I) = 0.74282E-01	TEMP(I) = 0.19818E 04
FM(I) = 0.5723E 01	XD(I) = 0.30000E 01	TI(I) = 0.30122E 00	PI(I) = 0.71570E-01	TEMP(I) = 0.19534E 04
FM(I) = 0.5717E 01	XD(I) = 0.37000E 01	TI(I) = 0.30013E 00	PI(I) = 0.71266E-01	TEMP(I) = 0.19502E 04
FM(I) = 0.5695E 01	XD(I) = 0.33000E 01	TI(I) = 0.30673E 00	PI(I) = 0.73593E-01	TEMP(I) = 0.19746E 04

FIGURE 11. RADIATION PROGRAM, SAMPLE PRINT OUT

```

CHAIN (2)
Q BY AVT • AVP METHOD
FK=-0.81404E 00
PHI= 0.15708F 01
J= 1
XDI(J)= 0.56000E 00
BLED= 0.26629F 02 AVTEM= 0.24763E 04 PH20= 0.66107E-01 SSF= 0.99420E-06 EMIS= 0.22877E-00
GRAD= 0.40307E-05 GRADS= 0.40307E-05
J= 2
XDI(J)= 0.60000E 00
BLED= 0.57655E 02 AVTEM= 0.22344E 04 PH20= 0.54985E-01 SSF= 0.16411E-04 EMIS= 0.31177E-00
GRAD= 0.57074E-04 GRADS= 0.61105E-04
J= 3
XDI(J)= 0.70000E 00
BLED= 0.92166E 03 AVTEM= 0.20916E 04 PH20= 0.49935E-01 SSF= 0.60190E-04 EMIS= 0.39607E-00
GRAD= 0.15801E-03 GRADS= 0.21912E-03
J= 4
XDI(J)= 0.80000E 00
BLED= 0.99894E 03 AVTEM= 0.20296E 04 PH20= 0.48165E-01 SSF= 0.12944E-03 EMIS= 0.44783E-00
GRAD= 0.25052E-03 GRADS= 0.46964E-03
J= 5
XDI(J)= 0.90000E 00
BLED= 0.93330E 03 AVTEM= 0.19994E 04 PH20= 0.47248E-01 SSF= 0.21748E-03 EMIS= 0.48461E-00
GRAD= 0.32466E-03 GRADS= 0.79430E-03
J= 6
XDI(J)= 0.10000E 01
BLED= 0.93330E 03 AVTEM= 0.19935E 04 PH20= 0.47093E-01 SSF= 0.31932E-03 EMIS= 0.48497E-00
GRAD= 0.37137E-03 GRADS= 0.11657E-02
J= 7
XDI(J)= 0.11000E 01
BLED= 0.96665E 03 AVTEM= 0.20035E 04 PH20= 0.47566E-01 SSF= 0.43137E-03 EMIS= 0.42864E-00
GRAD= 0.36843E-03 GRADS= 0.15341E-02
J= 8
XDI(J)= 0.12000E 01
BLED= 0.96665E 03 AVTEM= 0.19970E 04 PH20= 0.47350E-01 SSF= 0.55094E-03 EMIS= 0.42895E-00
GRAD= 0.38834E-03 GRADS= 0.19224E-02
J= 9
XDI(J)= 0.13000E 01
BLED= 0.96665E 03 AVTEM= 0.19921E 04 PH20= 0.47168E-01 SSF= 0.67602E-03 EMIS= 0.42899E-00
GRAD= 0.40229E-03 GRADS= 0.23247E-02
J= 10
XDI(J)= 0.14000E 01
BLED= 0.96665E 03 AVTEM= 0.19882E 04 PH20= 0.47015E-01 SSF= 0.80496E-03 EMIS= 0.42907E-00
GRAD= 0.41156E-03 GRADS= 0.27363E-02
J= 11
XDI(J)= 0.15000E 01
BLED= 0.96665E 03 AVTEM= 0.19851E 04 PH20= 0.46886E-01 SSF= 0.93649E-03 EMIS= 0.42912E-00
GRAD= 0.41729E-03 GRADS= 0.31536E-02
J= 12
XDI(J)= 0.16000E 01
BLED= 0.96665E 03 AVTEM= 0.19827E 04 PH20= 0.46779E-01 SSF= 0.10696E-02 EMIS= 0.42914E-00
GRAD= 0.42025E-03 GRADS= 0.35738E-02
J= 13
XDI(J)= 0.17000E 01
BLED= 0.96665E 03 AVTEM= 0.19808E 04 PH20= 0.46689E-01 SSF= 0.12035E-02 EMIS= 0.42915E-00
GRAD= 0.42102E-03 GRADS= 0.39949E-02
J= 14
XDI(J)= 0.18000E 01

```

FIGURE 11. RADIATION PROGRAM, SAMPLE PRINT OUT (Continued)

```

BLED= 0.16665E 03 AVTEM= 0.19793E 04 PH20= 0.46615E-01 SSF= 0.13374E-02 FMIS= 0.42916E-00
      GRAD= 0.42008E-03 GRADS= 0.44149E-02
              J= 15
      XDIJ= 0.19000E 01

BLED= 0.16665E 03 AVTEM= 0.19781E 04 PH20= 0.46556E-01 SSF= 0.14710E-02 FMIS= 0.42915E-00
      GRAD= 0.41776E-03 GRADS= 0.48327E-02
              J= 16
      XDIJ= 0.20000E 01

BLED= 0.16665E 03 AVTEM= 0.19772E 04 PH20= 0.46507E-01 SSF= 0.16037E-02 FMIS= 0.42915E-00
      GRAD= 0.41438E-03 GRADS= 0.52471E-02
              J= 17
      XDIJ= 0.21000E 01

BLED= 0.16665E 03 AVTEM= 0.19765E 04 PH20= 0.46470E-01 SSF= 0.17353E-02 FMIS= 0.42914E-00
      GRAD= 0.41020E-03 GRADS= 0.56573E-02
              J= 18
      XDIJ= 0.22000E 01

BLED= 0.16665E 03 AVTEM= 0.19759E 04 PH20= 0.46441E-01 SSF= 0.18654E-02 FMIS= 0.42914E-00
      GRAD= 0.40534E-03 GRADS= 0.60626E-02
              J= 19
      XDIJ= 0.23000E 01

BLED= 0.16665E 03 AVTEM= 0.19756E 04 PH20= 0.46420E-01 SSF= 0.19939E-02 FMIS= 0.42913E-00
      GRAD= 0.39998E-03 GRADS= 0.64626E-02
              J= 20
      XDIJ= 0.24000E 01

BLED= 0.16665E 03 AVTEM= 0.19753E 04 PH20= 0.46405E-01 SSF= 0.22397E-02 FMIS= 0.42913E-00
      GRAD= 0.76458E-03 GRADS= 0.72272E-02
              J= 21
      XDIJ= 0.26000E 01

BLED= 0.16665E 03 AVTEM= 0.19748E 04 PH20= 0.46376E-01 SSF= 0.24783E-02 FMIS= 0.42912E-00
      GRAD= 0.74149E-03 GRADS= 0.79687E-02
              J= 22
      XDIJ= 0.28000E 01

BLED= 0.16665E 03 AVTEM= 0.19744E 04 PH20= 0.46350E-01 SSF= 0.27092E-02 FMIS= 0.42911E-00
      GRAD= 0.71673E-03 GRADS= 0.86854E-02
              J= 23
      XDIJ= 0.30000E 01

BLED= 0.16665E 03 AVTEM= 0.19743E 04 PH20= 0.46347E-01 SSF= 0.29320E-02 FMIS= 0.42911E-00
      GRAD= 0.69159E-03 GRADS= 0.93770E-02
              J= 24
      XDIJ= 0.32000E 01

BLED= 0.16665E 03 AVTEM= 0.19745E 04 PH20= 0.46357E-01 SSF= 0.30422E-02 FMIS= 0.42911E-00
      GRAD= 0.34223E-03 GRADS= 0.97192E-02
              J= 25
      XDIJ= 0.33000E 01

BLED= 0.16665E 03 AVTEM= 0.19776E 04 PH20= 0.46648E-01 SSF= 0.32027E-02 FMIS= 0.42938E-00
      GRAD= 0.50173E-03 GRADS= 0.10221E-01
      Q BY AVT + AVP METHOD

TOTAL RADIANT HEAT FLUX IS 0.10220942E-01 BTU/SEC-SQ FT

```

FIGURE 11. RADIATION PROGRAM, SAMPLE PRINT OUT (Continued)

```

CHAIN (3)
HEAT FLUX BY ABSORPTION METHOD
J= 1
XD(J)= 0.56000E 00
ORD= 0.29731E-03 ORDA= 0.29731E-05
J= 2
XD(J)= 0.60000E 00
ORD= 0.51711E-04 ORDA= 0.54685E-04
J= 3
XD(J)= 0.70000E 00
ORD= 0.15404E-03 ORDA= 0.20872E-03
J= 4
XD(J)= 0.80000E 00
ORD= 0.27009E-03 ORDA= 0.47972E-03
J= 5
XD(J)= 0.90000E 00
ORD= 0.47332E-03 ORDA= 0.95304E-03
J= 6
XD(J)= 0.10000E 01
ORD= 0.34710E-03 ORDA= 0.13001E-02
J= 7
XD(J)= 0.11000E 01
ORD= 0.16509E-03 ORDA= 0.14652E-02
J= 8
XD(J)= 0.12000E 01
ORD= 0.15263E-03 ORDA= 0.16179E-02
J= 9
XD(J)= 0.13000E 01
ORD= 0.14497E-03 ORDA= 0.17628E-02
J= 10
XD(J)= 0.14000E 01
ORD= 0.13931E-03 ORDA= 0.19021E-02
J= 11
XD(J)= 0.15000E 01
ORD= 0.13430E-03 ORDA= 0.20364E-02
J= 12
XD(J)= 0.16000E 01
ORD= 0.13116E-03 ORDA= 0.21676E-02
J= 13
XD(J)= 0.17000E 01
ORD= 0.12753E-03 ORDA= 0.22951E-02
J= 14
XD(J)= 0.18000E 01
ORD= 0.12678E-03 ORDA= 0.24219E-02
J= 15
XD(J)= 0.19000E 01
ORD= 0.12536E-03 ORDA= 0.25472E-02
J= 16
XD(J)= 0.20000E 01
ORD= 0.12344E-03 ORDA= 0.26707E-02
J= 17
XD(J)= 0.21000E 01
ORD= 0.12173E-03 ORDA= 0.27924E-02
J= 18
XD(J)= 0.22000E 01
ORD= 0.11904E-03 ORDA= 0.29115E-02
J= 19
XD(J)= 0.23000E 01
ORD= 0.11703E-03 ORDA= 0.30285E-02
J= 20
XD(J)= 0.24000E 01
ORD= 0.22288E-03 ORDA= 0.32514E-02
J= 21
XD(J)= 0.26000E 01
ORD= 0.21511E-03 ORDA= 0.34665E-02
J= 22
XD(J)= 0.28000E 01
ORD= 0.20886E-03 ORDA= 0.36753E-02
J= 23
XD(J)= 0.30000E 01
ORD= 0.20136E-03 ORDA= 0.38767E-02
J= 24
XD(J)= 0.32000E 01
ORD= 0.99599E-04 ORDA= 0.39763E-02
J= 25
XD(J)= 0.33000E 01
ORD= 0.14521E-03 ORDA= 0.41215E-02
HEAT FLUX BY ABSORPTION METHOD
TOTAL RADIANT HEAT FLUX IS 0.41214981E-02 BTU/SEC-SQ FT

CHAIN (4)
BLOCKAGE CORRECTION FACTORS
J= 1
LEFT SIDE OF REGIO-
XD= 0.32498470E 01 YD= 0.13755273E-02
MIDDLE OF REGION
XD= 0.27116950E 01 YD= -0.13271311E-05
RIGHT SIDE OF REGION
XD= 0.32498470E 01 YD= -0.13755273E-02
ORD= 0. GRAD= 0.
ORD= 0. GRAD= 0.
J= 2
LEFT SIDE OF REGIO-
XD= 0.31019037E 01 YD= 0.90989337E-02
MIDDLE OF REGION
XD= 0.21259402E 01 YD= -0.10404544E-05
RIGHT SIDE OF REGION
XD= 0.31019037E 01 YD= -0.90989337E-02
ORD= 0. GRAD= 0.
ORD= 0. GRAD= 0.
J= 3
LEFT SIDE OF REGIO-
XD= 0.30786983E 01 YD= 0.27421047E-01
MIDDLE OF REGION
XD= 0.13030417E 01 YD= -0.68176835E-06
RIGHT SIDE OF REGION
XD= 0.30786983E 01 YD= -0.27421047E-01
ORD= 0. GRAD= 0.
ORD= 0. GRAD= 0.
J= 4
LEFT SIDE OF REGIO-
XD= 0.29744792E 01 YD= 0.46014039E-01
MIDDLE OF REGION
XD= 0.89169564E 01 YD= -0.43640478E-06
XD= 0.11785444E 01 YD= -0.57679154E-06
XD= 0.11785444E 01 YD= -0.57679154E-06
XD= 0.11785444E 01 YD= -0.57679154E-06
XD= 0.11785444E 01 YD= -0.57679154E-06
XD= 0.11785444E 01 YD= -0.57679154E-06
RIGHT SIDE OF REGION
XD= 0.29744792E 01 YD= 0.46014039E-01
ORD= 0.83507117E-04 GRAD= 0.83507113E-04
ORD= 0.00331561E-04 GRAD= 0.90331561E-04
J= 5
LEFT SIDE OF REGIO-
XD= 0.28788407E 01 YD= 0.62010342E-01
MIDDLE OF REGION
XD= 0.44206982E-01 YD= -0.23788743E-06
XD= 0.64243330E 01 YD= -0.31441329E-06
XD= 0.64243330E 01 YD= -0.31441329E-06
XD= 0.64243330E 01 YD= -0.31441329E-06
XD= 0.64243330E 01 YD= -0.31441329E-06
XD= 0.64243330E 01 YD= -0.31441329E-06
RIGHT SIDE OF REGION
XD= 0.28788407E 01 YD= 0.62010342E-01
ORD= 0.10821874E-03 GRAD= 0.19172589E-03
ORD= 0.15777324E-03 GRAD= 0.24810482E-03

```

FIGURE 11. RADIATION PROGRAM, SAMPLE PRINT OUT (Continued)



LEFT SIDE OF REGION	J= 10	J= 14
X0= 0.27884704E-01 Y0= 0.75930348E-01	LEFT SIDE OF REGION	LEFT SIDE OF REGION
MIDDLE OF REGION	X0= 0.24863580E-01 Y0= 0.11956636E-00	X0= 0.22526391E-01 Y0= 0.15221333E-00
X0= 0.15402514E-01 Y0= -0.75381445E-07	MIDDLE OF REGION	MIDDLE OF REGION
X0= 0.20157344E-01 Y0= -0.99630800E-07	X0= -0.79278693E-01 Y0= 0.38799746E-06	X0= -0.13709121E-01 Y0= 0.67093810E-06
X0= 0.20157344E-01 Y0= -0.99630800E-07	X0= -0.10478180E-01 Y0= 0.51281244E-06	X0= -0.19119199E-01 Y0= 0.88677174E-06
X0= 0.20157344E-01 Y0= -0.99630800E-07	X0= -0.10478180E-01 Y0= 0.51281244E-06	X0= -0.19119199E-01 Y0= 0.88677174E-06
X0= 0.20157344E-01 Y0= -0.99630800E-07	X0= -0.10478180E-01 Y0= 0.51281244E-06	X0= -0.19119199E-01 Y0= 0.88677174E-06
X0= 0.20157344E-01 Y0= -0.99630800E-07	X0= -0.10478180E-01 Y0= 0.51281244E-06	X0= -0.19119199E-01 Y0= 0.88677174E-06
RIGHT SIDE OF REGION	RIGHT SIDE OF REGION	RIGHT SIDE OF REGION
X0= 0.27884704E-01 Y0= -0.75930348E-01	X0= 0.24863580E-01 Y0= 0.11956636E-00	X0= 0.22526391E-01 Y0= -0.15221333E-00
QRAD= 0.12379024E-03 QRADS= 0.31551411E-03	QRAD= 0.13718144E-03 QRADS= 0.87905440E-03	QRAD= 0.14002769E-03 QRADS= 0.17996067E-02
QRDA= 0.11569077E-03 QRDA= 0.34380459E-03	QRDA= 0.46436753E-04 QRDA= 0.56446927E-03	QRDA= 0.42259484E-04 QRDA= 0.71772300E-03
J= 7	J= 11	J= 15
LEFT SIDE OF REGION	LEFT SIDE OF REGION	LEFT SIDE OF REGION
X0= 0.27850731E-01 Y0= 0.88363512E-01	X0= 0.24224355E-01 Y0= 0.12949395E-00	X0= 0.22824230E-01 Y0= 0.15930393E-00
MIDDLE OF REGION	MIDDLE OF REGION	MIDDLE OF REGION
X0= -0.19217634E-01 Y0= 0.74476623E-07	X0= -0.96831827E-01 Y0= 0.47390433E-06	X0= -0.14795929E-01 Y0= 0.72412740E-06
X0= -0.20112944E-01 Y0= 0.98434990E-07	X0= -0.12798159E-01 Y0= 0.62635470E-06	X0= -0.19555622E-01 Y0= 0.95707173E-06
X0= -0.20112944E-01 Y0= 0.98434990E-07	X0= -0.12798159E-01 Y0= 0.62635470E-06	X0= -0.19555622E-01 Y0= 0.95707173E-06
X0= -0.20112944E-01 Y0= 0.98434990E-07	X0= -0.12798159E-01 Y0= 0.62635470E-06	X0= -0.19555622E-01 Y0= 0.95707173E-06
X0= -0.20112944E-01 Y0= 0.98434990E-07	X0= -0.12798159E-01 Y0= 0.62635470E-06	X0= -0.19555622E-01 Y0= 0.95707173E-06
RIGHT SIDE OF REGION	RIGHT SIDE OF REGION	RIGHT SIDE OF REGION
X0= 0.27850731E-01 Y0= -0.88363512E-01	X0= 0.24224355E-01 Y0= -0.12949395E-00	X0= 0.22824230E-01 Y0= -0.15930393E-00
QRAD= 0.12280921E-03 QRADS= 0.43812534E-03	QRAD= 0.13909787E-03 QRADS= 0.97819227E-03	QRAD= 0.13925469E-03 QRADS= 0.15378604E-02
QRDA= 0.15029724E-04 QRDA= 0.41883391E-03	QRDA= 0.44766031E-04 QRDA= 0.60023532E-03	QRDA= 0.41780250E-04 QRDA= 0.77950825E-03
J= 8	J= 12	J= 16
LEFT SIDE OF REGION	LEFT SIDE OF REGION	LEFT SIDE OF REGION
X0= 0.26272500E-01 Y0= 0.99630207E-01	X0= 0.23623774E-01 Y0= 0.13686175E-00	X0= 0.21850063E-01 Y0= 0.16607836E-00
MIDDLE OF REGION	MIDDLE OF REGION	MIDDLE OF REGION
X0= -0.30427631E-01 Y0= 0.19296277E-06	X0= -0.11193457E-01 Y0= 0.54781807E-06	X0= -0.15991780E-01 Y0= 0.78265373E-06
X0= -0.52111080E-01 Y0= 0.25503644E-06	X0= -0.14794272E-01 Y0= 0.72404650E-06	X0= -0.21136165E-01 Y0= 0.10344251E-05
X0= -0.52111080E-01 Y0= 0.25503644E-06	X0= -0.14794272E-01 Y0= 0.72404650E-06	X0= -0.21136165E-01 Y0= 0.10344251E-05
X0= -0.52111080E-01 Y0= 0.25503644E-06	X0= -0.14794272E-01 Y0= 0.72404650E-06	X0= -0.21136165E-01 Y0= 0.10344251E-05
X0= -0.52111080E-01 Y0= 0.25503644E-06	X0= -0.14794272E-01 Y0= 0.72404650E-06	X0= -0.21136165E-01 Y0= 0.10344251E-05
RIGHT SIDE OF REGION	RIGHT SIDE OF REGION	RIGHT SIDE OF REGION
X0= 0.26272500E-01 Y0= -0.99630207E-01	X0= 0.23623774E-01 Y0= -0.13686175E-00	X0= 0.21850063E-01 Y0= -0.16607836E-00
QRAD= 0.12944746E-03 QRADS= 0.56777211E-03	QRAD= 0.14008454E-03 QRADS= 0.11182368E-02	QRAD= 0.13812814E-03 QRADS= 0.16759889E-02
QRDA= 0.10876244E-04 QRDA= 0.44971014E-03	QRDA= 0.43719080E-04 QRDA= 0.65295439E-03	QRDA= 0.41147268E-04 QRDA= 0.82045551E-03
J= 9	J= 13	J= 17
LEFT SIDE OF REGION	LEFT SIDE OF REGION	LEFT SIDE OF REGION
X0= 0.25545007E-01 Y0= 0.10999485E-00	X0= 0.23587190E-01 Y0= 0.14474706E-00	X0= 0.21101912E-01 Y0= 0.17258302E-00
MIDDLE OF REGION	MIDDLE OF REGION	MIDDLE OF REGION
X0= -0.60314469E-01 Y0= 0.29518505E-06	X0= -0.12529729E-01 Y0= 0.61321744E-06	X0= -0.16993264E-01 Y0= 0.81209117E-06
X0= -0.79716991E-01 Y0= 0.39014204E-06	X0= -0.16460409E-01 Y0= 0.81048301E-06	X0= -0.21031144E-01 Y0= 0.10733323E-05
X0= -0.79716991E-01 Y0= 0.39014204E-06	X0= -0.16460409E-01 Y0= 0.81048301E-06	X0= -0.21031144E-01 Y0= 0.10733323E-05
X0= -0.79716991E-01 Y0= 0.39014204E-06	X0= -0.16460409E-01 Y0= 0.81048301E-06	X0= -0.21031144E-01 Y0= 0.10733323E-05
X0= -0.79716991E-01 Y0= 0.39014204E-06	X0= -0.16460409E-01 Y0= 0.81048301E-06	X0= -0.21031144E-01 Y0= 0.10733323E-05
RIGHT SIDE OF REGION	RIGHT SIDE OF REGION	RIGHT SIDE OF REGION
X0= 0.25545007E-01 Y0= -0.10999485E-00	X0= 0.23587190E-01 Y0= -0.14474706E-00	X0= 0.21101912E-01 Y0= -0.17258302E-00
QRAD= 0.13409615E-03 QRADS= 0.70186824E-03	QRAD= 0.14034149E-03 QRADS= 0.12959781E-02	QRAD= 0.13673197E-03 QRADS= 0.19127204E-02
QRDA= 0.14832277E-04 QRDA= 0.51803293E-03	QRDA= 0.42509919E-04 QRDA= 0.69546351E-03	QRDA= 0.40577153E-04 QRDA= 0.86193267E-03

FIGURE 11. RADIATION PROGRAM, SAMPLE PRINT OUT (Continued)

```

J# 18
LEFT SIDE OF REGION
X# 0.20A7782AE 01 Y# 0.17883314E-00
MIDDLE OF REGION
X# -0.17A73792E 01 Y# 0.85029078E-06
X# -0.2296275AE 01 Y# 0.11238203E-05
X# -0.2296275AE 01 Y# 0.11238203E-05
X# -0.2296275AE 01 Y# 0.11238203E-05
X# -0.2296275AE 01 Y# 0.11238203E-05
X# -0.2296275AE 01 Y# 0.11238203E-05
X# -0.2296275AE 01 Y# 0.11238203E-05
RIGHT SIDE OF REGION
X# 0.20A7782AE 01 Y# -0.17883314E-00
QRAD= 0.13511220E-03 QRADS= 0.19478314E-02
QRDA= 0.19679094E-04 QRDAS= 0.90001174E-01

J# 19
LEFT SIDE OF REGION
X# 0.20P76205E 01 Y# 0.18486849E-00
MIDDLE OF REGION
X# -0.14A93824E 01 Y# 0.88553015E-06
X# -0.23014419E 01 Y# 0.11703946E-05
X# -0.23014419E 01 Y# 0.11703946E-05
X# -0.23014419E 01 Y# 0.11703946E-05
X# -0.23014419E 01 Y# 0.11703946E-05
X# -0.23014419E 01 Y# 0.11703946E-05
X# -0.23014419E 01 Y# 0.11703946E-05
RIGHT SIDE OF REGION
X# 0.20P76205E 01 Y# -0.18486849E-00
QRAD= 0.1333247AE-03 QRADS= 0.20811594E-02
QRDA= 0.19008957E-04 QRDAS= 0.90902072E-01

J# 20
LEFT SIDE OF REGION
X# 0.19A9557AE 01 Y# 0.19072049E-00
MIDDLE OF REGION
X# -0.14A91899E 01 Y# 0.91431041E-06
X# -0.24A91659E 01 Y# 0.12084343E-05
X# -0.24A91659E 01 Y# 0.12084343E-05
X# -0.24A91659E 01 Y# 0.12084343E-05
X# -0.24A91659E 01 Y# 0.12084343E-05
X# -0.24A91659E 01 Y# 0.12084343E-05
X# -0.24A91659E 01 Y# 0.12084343E-05
RIGHT SIDE OF REGION
X# 0.19A9557AE 01 Y# -0.19072049E-00
QRAD= 0.254A5491E-03 QRADS= 0.273A0184E-02
QRDA= 0.7420149AE-04 QRDAS= 0.10142124E-02

J# 21
LEFT SIDE OF REGION
X# 0.19A92202E 01 Y# 0.202000A1E-00
MIDDLE OF REGION
X# -0.197A607AE 01 Y# 0.98736911E-06
X# -0.26A2454AE 01 Y# 0.12785614E-05
X# -0.26A2454AE 01 Y# 0.12785614E-05
X# -0.26A2454AE 01 Y# 0.12785614E-05
X# -0.26A2454AE 01 Y# 0.12785614E-05
X# -0.26A2454AE 01 Y# 0.12785614E-05
X# -0.26A2454AE 01 Y# 0.12785614E-05
RIGHT SIDE OF REGION
X# 0.19A92202E 01 Y# -0.202000A1E-00
QRAD= 0.254716284E-03 QRADS= 0.28871414E-02
QRDA= 0.71704770E-04 QRDAS= 0.10899174E-02

J# 22
LEFT SIDE OF REGION
X# 0.1A457304E 01 Y# 0.21272917E-00
MIDDLE OF REGION
X# -0.20A16159E 01 Y# 0.10089758E-05
X# -0.27A48144E 01 Y# 0.13335515E-05
X# -0.27A48144E 01 Y# 0.13335515E-05
X# -0.27A48144E 01 Y# 0.13335515E-05
X# -0.27A48144E 01 Y# 0.13335515E-05
X# -0.27A48144E 01 Y# 0.13335515E-05
X# -0.27A48144E 01 Y# 0.13335515E-05
RIGHT SIDE OF REGION
X# 0.1A457304E 01 Y# -0.21272917E-00
QRAD= 0.25389108E-03 QRADS= 0.20220225E-02
QRDA= 0.49621027E-04 QRDAS= 0.11555384E-02

J# 23
LEFT SIDE OF REGION
X# 0.170A2185E 01 Y# 0.22297117E-00
MIDDLE OF REGION
X# -0.213A6799E 01 Y# 0.10427746E-05
X# -0.24A1A095E 01 Y# 0.137A2255E-05
X# -0.24A1A095E 01 Y# 0.137A2255E-05
X# -0.24A1A095E 01 Y# 0.137A2255E-05
X# -0.24A1A095E 01 Y# 0.137A2255E-05
X# -0.24A1A095E 01 Y# 0.137A2255E-05
X# -0.24A1A095E 01 Y# 0.137A2255E-05
RIGHT SIDE OF REGION
X# 0.170A2185E 01 Y# -0.22297117E-00
QRAD= 0.23052040E-03 QRADS= 0.30526219E-02
QRDA= 0.47121440E-04 QRDAS= 0.12226499E-02

J# 24
LEFT SIDE OF REGION
X# 0.17A59845E 01 Y# 0.2328337E-00
MIDDLE OF REGION
X# -0.217A5295E 01 Y# 0.106A1922E-05
X# -0.24A93339E 01 Y# 0.14091749E-05
X# -0.24A93339E 01 Y# 0.14091749E-05
X# -0.24A93339E 01 Y# 0.14091749E-05
X# -0.24A93339E 01 Y# 0.14091749E-05
X# -0.24A93339E 01 Y# 0.14091749E-05
X# -0.24A93339E 01 Y# 0.14091749E-05
RIGHT SIDE OF REGION
X# 0.17A59845E 01 Y# -0.2328337E-00
QRAD= 0.11407430E-03 QRADS= 0.316A6972E-02
QRDA= 0.33196430E-04 QRDAS= 0.12558501E-02

J# 25
LEFT SIDE OF REGION
X# 0.1721672AE 01 Y# 0.23765675E-00
MIDDLE OF REGION
X# -0.20A40725E 01 Y# 0.1078A991E-05
X# -0.29A30991E 01 Y# 0.1425A999E-05
X# -0.29A30991E 01 Y# 0.1425A999E-05
X# -0.29A30991E 01 Y# 0.1425A999E-05
X# -0.29A30991E 01 Y# 0.1425A999E-05
X# -0.29A30991E 01 Y# 0.1425A999E-05
X# -0.29A30991E 01 Y# 0.1425A999E-05
RIGHT SIDE OF REGION
X# 0.1721672AE 01 Y# -0.23765675E-00
QRAD= 0.15A724175E-03 QRADS= 0.33319400E-02
QRDA= 0.44A02450E-04 QRDAS= 0.13042584E-02

WITH BLOCKAGE CORRECTION, THE RADIATIVE FLUX BY THE AVT. AND AVP. METHOD IS 0.33339409E-02 BTU/SEC-SQ FT
BY THE ABSORPTION METHOD, IT IS 0.13042584E-02

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FIGURE 11. RADIATION PROGRAM, SAMPLE PRINT OUT (Continued)

```

CHAIN (2)
G BY AVT + AVF METHOD
FK=-0.19735E-01
PHI= 0.48930E-00
J= 1
XD(J)= 0.56000E-00
RLFD= 1.10606E-00 AVTEM= 0.33161E-04 PH20= 0.12865E-00 SSF= 1.25403E-05 FMIS= 0.29740E-02
QPA= 1.43498E-06 QPADS= 0.43498E-06
J= 2
XD(J)= 0.60000E-00
RLFD= 1.38526E-00 AVTEM= 0.33569E-04 PH20= 0.13117E-00 SSF= 1.43398E-04 FMIS= 0.12041E-01
QPA= 1.29743E-04 QPADS= 0.30178E-04
J= 3
XD(J)= 0.70000E-00
RLFD= 1.82293E-00 AVTEM= 0.36470E-04 PH20= 0.14865E-00 SSF= 1.16325E-03 FMIS= 0.22903E-01
QPA= 0.23209E-03 QPADS= 0.26227E-03
J= 4
XD(J)= 0.80000E-00
RLFD= 1.12882E-01 AVTEM= 0.33750E-04 PH20= 0.13175E-00 SSF= 1.35853E-03 FMIS= 0.36357E-01
QPA= 1.43860E-03 QPADS= 0.70047E-03
J= 5
XD(J)= 0.90000E-00
RLFD= 1.17493E-01 AVTEM= 0.30482E-04 PH20= 0.11144E-00 SSF= 1.61387E-03 FMIS= 0.48903E-01
QPA= 0.51123E-03 QPADS= 0.12141E-02
J= 6
XD(J)= 0.10000E-01
RLFD= 0.24966E-01 AVTEM= 0.24161E-04 PH20= 0.96092E-01 SSF= 1.91699E-03 FMIS= 0.63385E-01
QPA= 1.57529E-03 QPADS= 0.17894E-02
J= 7
XD(J)= 0.11000E-01
RLFD= 0.26804E-01 AVTEM= 0.26811E-04 PH20= 0.88034E-01 SSF= 1.12588E-02 FMIS= 0.72568E-01
QPA= 1.61061E-03 QPADS= 0.24000E-02
J= 8
XD(J)= 0.12000E-01
RLFD= 0.33680E-01 AVTEM= 0.25283E-04 PH20= 0.79473E-01 SSF= 1.16320E-02 FMIS= 0.80710E-01
QPA= 0.58595E-03 QPADS= 0.29860E-02
J= 9
XD(J)= 0.13000E-01
RLFD= 0.40699E-01 AVTEM= 0.24040E-04 PH20= 0.71002E-01 SSF= 0.20306E-02 FMIS= 0.90920E-01
QPA= 0.57715E-03 QPADS= 0.35631E-02
J= 10
XD(J)= 0.14000E-01
RLFD= 0.45971E-01 AVTEM= 0.23050E-04 PH20= 0.65823E-01 SSF= 1.24496E-02 FMIS= 0.97302E-01
QPA= 0.54849E-03 QPADS= 0.41116E-02
J= 11
XD(J)= 0.15000E-01
RLFD= 0.53477E-01 AVTEM= 0.22233E-04 PH20= 0.60893E-01 SSF= 1.28850E-02 FMIS= 0.10500E-00
QPA= 0.53633E-03 QPADS= 0.46479E-02
J= 12
XD(J)= 0.16000E-01
RLFD= 0.59225E-01 AVTEM= 0.21735E-04 PH20= 0.57094E-01 SSF= 1.33331E-02 FMIS= 0.11189E-00
QPA= 0.53274E-03 QPADS= 0.51807E-02

```

FIGURE 11. RADIATION PROGRAM, SAMPLE PRINT OUT (Continued)

```

      J= 13
      XDI(J)= 0.17000E 01
      BLEB= 0.65208E 01 AVTEM= 0.21222E 04 PH20= 0.54998E-01 SSF= 0.37910E-02 EMIS= 0.11745E-00
      GRAD= 0.51934E-03 GRADS= 0.57000E-02
      J= 14
      XDI(J)= 0.18000E 01
      BLEB= 0.73608E 01 AVTEM= 0.20699E 04 PH20= 0.51008E-01 SSF= 0.42560E-02 EMIS= 0.12466E-00
      GRAD= 0.50665E-03 GRADS= 0.62866E-02
      J= 15
      XDI(J)= 0.19000E 01
      BLEB= 0.80154E 01 AVTEM= 0.20545E 04 PH20= 0.51058E-01 SSF= 0.47259E-02 EMIS= 0.13047E-00
      GRAD= 0.52011E-03 GRADS= 0.67268E-02
      J= 16
      XDI(J)= 0.20000E 01
      BLEB= 0.89273E 01 AVTEM= 0.20220E 04 PH20= 0.49105E-01 SSF= 0.51991E-02 EMIS= 0.13739E-00
      GRAD= 0.51740E-03 GRADS= 0.72442E-02
      J= 17
      XDI(J)= 0.21000E 01
      BLEB= 0.98796E 01 AVTEM= 0.20077E 04 PH20= 0.48284E-01 SSF= 0.56736E-02 EMIS= 0.14466E-00
      GRAD= 0.53100E-03 GRADS= 0.77752E-02
      J= 18
      XDI(J)= 0.22000E 01
      BLEB= 0.10873E 02 AVTEM= 0.19965E 04 PH20= 0.47631E-01 SSF= 0.61481E-02 EMIS= 0.15178E-00
      GRAD= 0.54486E-03 GRADS= 0.83200E-02
      J= 19
      XDI(J)= 0.23000E 01
      BLEB= 0.11416E 02 AVTEM= 0.19899E 04 PH20= 0.47242E-01 SSF= 0.66217E-02 EMIS= 0.15543E-00
      GRAD= 0.54935E-03 GRADS= 0.88694E-02
      J= 20
      XDI(J)= 0.24000E 01
      BLEB= 0.12484E 02 AVTEM= 0.19849E 04 PH20= 0.46950E-01 SSF= 0.75410E-02 EMIS= 0.16260E-00
      GRAD= 0.11045E-02 GRADS= 0.99739E-02
      J= 21
      XDI(J)= 0.26000E 01
      BLEB= 0.13963E 02 AVTEM= 0.19775E 04 PH20= 0.46925E-01 SSF= 0.84485E-02 EMIS= 0.17187E-00
      GRAD= 0.11356E-02 GRADS= 0.11110E-01
      J= 22
      XDI(J)= 0.28000E 01
      BLEB= 0.15271E 02 AVTEM= 0.19722E 04 PH20= 0.46218E-01 SSF= 0.93393E-02 EMIS= 0.17942E-00
      GRAD= 0.11526E-02 GRADS= 0.12262E-01
      J= 23
      XDI(J)= 0.30000E 01
      BLEB= 0.16665E 02 AVTEM= 0.19718E 04 PH20= 0.46195E-01 SSF= 0.10210E-01 EMIS= 0.18767E-00
      GRAD= 0.11759E-02 GRADS= 0.13438E-01
      J= 24
      XDI(J)= 0.32000E 01
      BLEB= 0.18150E 02 AVTEM= 0.19737E 04 PH20= 0.46307E-01 SSF= 0.10644E-01 EMIS= 0.19583E-00
      GRAD= 0.61364E-03 GRADS= 0.14052E-01
      J= 25
      XDI(J)= 0.33000E 01
      BLEB= 0.18930E 02 AVTEM= 0.20013E 04 PH20= 0.48922E-01 SSF= 0.11280E-01 EMIS= 0.20287E-00
      GRAD= 0.98517E-03 GRADS= 0.15037E-01
      Q BY AVT + AVP METHOD
      TOTAL RADIANT HEAT FLUX IS 0.15036862E-01 BTU/SEC-SQ FT

```

FIGURE 11. RADIATION PROGRAM, SAMPLE PRINT OUT (Continued)

```

CHAIN (X)
HEAT FLUX BY ABSORPTION METHOD
J= 1
XD(IJ)= 0.56000E 00

ORD= 0.74689E-07   ORDA= 0.74689E-07
J= 2
XD(IJ)= 0.60000E 00

ORD= 0.50860E-05   ORDA= 0.51607E-05
J= 3
XD(IJ)= 0.70000E 00

ORD= 0.36463E-04   ORDA= 0.41623E-04
J= 4
XD(IJ)= 0.80000E 00

ORD= 0.64390E-04   ORDA= 0.10601E-03
J= 5
XD(IJ)= 0.90000E 00

ORD= 0.80574E-04   ORDA= 0.18659E-03
J= 6
XD(IJ)= 0.10000E 01

ORD= 0.93671E-04   ORDA= 0.28026E-03
J= 7
XD(IJ)= 0.11000E 01

ORD= 0.95493E-04   ORDA= 0.37575E-03
J= 8
XD(IJ)= 0.12000E 01

ORD= 0.94769E-04   ORDA= 0.47052E-03
J= 9
XD(IJ)= 0.13000E 01

ORD= 0.95205E-04   ORDA= 0.56573E-03
J= 10
XD(IJ)= 0.14000E 01

ORD= 0.92091E-04   ORDA= 0.64782E-03
J= 11
XD(IJ)= 0.15000E 01

ORD= 0.91110E-04   ORDA= 0.74893E-03
J= 12
XD(IJ)= 0.16000E 01

ORD= 0.88668E-04   ORDA= 0.83759E-03
J= 13
XD(IJ)= 0.17000E 01

ORD= 0.88632E-04   ORDA= 0.92623E-03
J= 14
XD(IJ)= 0.18000E 01

ORD= 0.90721E-04   ORDA= 0.10169E-02
J= 15
XD(IJ)= 0.19000E 01

ORD= 0.91227E-04   ORDA= 0.11082E-02
J= 16
XD(IJ)= 0.20000E 01

ORD= 0.94834E-04   ORDA= 0.12030E-02
J= 17
XD(IJ)= 0.21000E 01

ORD= 0.10179E-03   ORDA= 0.13048E-02
J= 18
XD(IJ)= 0.22000E 01

ORD= 0.11091E-03   ORDA= 0.14157E-02
J= 19
XD(IJ)= 0.23000E 01

ORD= 0.11598E-03   ORDA= 0.15317E-02
J= 20
XD(IJ)= 0.24000E 01

ORD= 0.25169E-03   ORDA= 0.17836E-02
J= 21
XD(IJ)= 0.26000E 01

ORD= 0.28808E-03   ORDA= 0.20724E-02
J= 22
XD(IJ)= 0.28000E 01

ORD= 0.32669E-03   ORDA= 0.23991E-02
J= 23
XD(IJ)= 0.30000E 01

ORD= 0.37396E-03   ORDA= 0.27731E-02
J= 24
XD(IJ)= 0.32000E 01

ORD= 0.22030E-03   ORDA= 0.29934E-02
J= 25
XD(IJ)= 0.33000E 01

ORD= 0.35214E-03   ORDA= 0.33455E-02
HEAT FLUX BY ABSORPTION METHOD
TOTAL RADIANT HEAT FLUX IS 0.3345245E-02 BTU/SFC-SQ FT

```

FIGURE 11. RADIATION PROGRAM, SAMPLE PRINT OUT (Continued)

CHAIN (4)  
BLOCKAGE CORRECTION FACTORS  
J= 1

LEFT SIDE OF REGION  
X0= 0.7588651E 01 Y0= 0.20282232E 01  
MIDDLE OF REGION  
X0= 0.75851804E 01 Y0= 0.20222274E 01  
RIGHT SIDE OF REGION  
X0= 0.75811755E 01 Y0= 0.20187571E 01  
ORDA= 0. GRAS= 0.  
ORDA= 0. GRAS= 0.

J= 2

LEFT SIDE OF REGION  
X0= 0.74491021E 01 Y0= 0.2024404E 01  
MIDDLE OF REGION  
X0= 0.74460084E 01 Y0= 0.19851234E 01  
RIGHT SIDE OF REGION  
X0= 0.74457769E 01 Y0= 0.19422639E 01  
ORDA= 0. GRAS= 0.  
ORDA= 0. GRAS= 0.

J= 3

LEFT SIDE OF REGION  
X0= 0.71862355E 01 Y0= 0.20167705E 01  
MIDDLE OF REGION  
X0= 0.71455962E 01 Y0= 0.18970352E 01  
RIGHT SIDE OF REGION  
X0= 0.72363222E 01 Y0= 0.18289298E 01  
ORDA= 0. GRAS= 0.  
ORDA= 0. GRAS= 0.

J= 4

LEFT SIDE OF REGION  
X0= 0.69531841E 01 Y0= 0.20147374E 01  
MIDDLE OF REGION  
X0= 0.6982874E 01 Y0= 0.18136639E 01  
RIGHT SIDE OF REGION  
X0= 0.7086913E 01 Y0= 0.17008274E 01  
ORDA= 0. GRAS= 0.  
ORDA= 0. GRAS= 0.

J= 5

LEFT SIDE OF REGION  
X0= 0.6680077E 01 Y0= 0.20083375E 01  
MIDDLE OF REGION  
X0= 0.6558676E 01 Y0= 0.17371461E 01  
RIGHT SIDE OF REGION  
X0= 0.67825644E 01 Y0= 0.1586796E 01  
ORDA= 0. GRAS= 0.  
ORDA= 0. GRAS= 0.

J= 6

LEFT SIDE OF REGION  
X0= 0.64544931E 01 Y0= 0.19988914E 01  
MIDDLE OF REGION  
X0= 0.62511654E 01 Y0= 0.16665759E 01  
RIGHT SIDE OF REGION  
X0= 0.6501867E 01 Y0= 0.14843652E 01  
ORDA= 0. GRAS= 0.  
ORDA= 0. GRAS= 0.

J= 7

LEFT SIDE OF REGION  
X0= 0.62443241E 01 Y0= 0.19881179E 01  
MIDDLE OF REGION  
X0= 0.60853352E 01 Y0= 0.16810349E 01  
RIGHT SIDE OF REGION  
X0= 0.64638663E 01 Y0= 0.1390950E 01  
ORDA= 0. GRAS= 0.  
ORDA= 0. GRAS= 0.

J= 8

LEFT SIDE OF REGION  
X0= 0.60479784E 01 Y0= 0.19766014E 01  
MIDDLE OF REGION  
X0= 0.57760537E 01 Y0= 0.15399899E 01  
RIGHT SIDE OF REGION  
X0= 0.6257472E 01 Y0= 0.1305218E 01  
ORDA= 0. GRAS= 0.  
ORDA= 0. GRAS= 0.

J= 9

LEFT SIDE OF REGION  
X0= 0.59640474E 01 Y0= 0.19649947E 01  
MIDDLE OF REGION  
X0= 0.59813224E 01 Y0= 0.14826620E 01  
RIGHT SIDE OF REGION  
X0= 0.60618074E 01 Y0= 0.12258724E 01  
ORDA= 0. GRAS= 0.  
ORDA= 0. GRAS= 0.

J= 10

LEFT SIDE OF REGION  
X0= 0.5861386E 01 Y0= 0.19534531E 01  
MIDDLE OF REGION  
X0= 0.53497952E 01 Y0= 0.14269344E 01  
RIGHT SIDE OF REGION  
X0= 0.59859941E 01 Y0= 0.11522011E 01  
ORDA= 0. GRAS= 0.  
ORDA= 0. GRAS= 0.

J= 11

LEFT SIDE OF REGION  
X0= 0.5589732E 01 Y0= 0.1942259E 01  
MIDDLE OF REGION  
X0= 0.51901034E 01 Y0= 0.13783621E 01  
RIGHT SIDE OF REGION  
X0= 0.57491714E 01 Y0= 0.10834343E 01  
ORDA= 0. GRAS= 0.  
ORDA= 0. GRAS= 0.

J= 12

LEFT SIDE OF REGION  
X0= 0.53759314E 01 Y0= 0.19313853E 01  
MIDDLE OF REGION  
X0= 0.49811991E 01 Y0= 0.13306658E 01  
RIGHT SIDE OF REGION  
X0= 0.56206989E 01 Y0= 0.10191351E 01  
ORDA= 0. GRAS= 0.  
ORDA= 0. GRAS= 0.

J= 13

LEFT SIDE OF REGION  
X0= 0.5231476E 01 Y0= 0.19289437E 01  
MIDDLE OF REGION  
X0= 0.4822130E 01 Y0= 0.12555917E 01  
RIGHT SIDE OF REGION  
X0= 0.54499831E 01 Y0= 0.99881701E 00  
ORDA= 0. GRAS= 0.  
ORDA= 0. GRAS= 0.

J= 14

LEFT SIDE OF REGION  
X0= 0.50849895E 01 Y0= 0.19109638E 01  
MIDDLE OF REGION  
X0= 0.46620671E 01 Y0= 0.1242914E 01  
RIGHT SIDE OF REGION  
X0= 0.53452005E 01 Y0= 0.90209607E 00  
ORDA= 0. GRAS= 0.  
ORDA= 0. GRAS= 0.

FIGURE 11. RADIATION PROGRAM, SAMPLE PRINT OUT (Continued)

LEFT SIDE OF REGION

XO= 0.49656897E 01 YO= 0.19014793E 01  
MIDDLE OF REGION  
XO= 0.45103020E 01 YO= 0.12024574E 01  
RIGHT SIDE OF REGION  
XO= 0.52490699E 01 YO= 0.84862743E 00  
GRAD= 0. GRADS= 0.  
ORDA= 0. ORDAS= 0.  
J= 16

LEFT SIDE OF REGION

XO= 0.48430112E 01 YO= 0.18927591E 01  
MIDDLE OF REGION  
XO= 0.43661194E 01 YO= 0.11640190E 01  
RIGHT SIDE OF REGION  
XO= 0.51781540E 01 YO= 0.79791483E 00  
GRAD= 0. GRADS= 0.  
ORDA= 0. ORDAS= 0.  
J= 17

LEFT SIDE OF REGION

XO= 0.47266354E 01 YO= 0.18840611E 01  
MIDDLE OF REGION  
XO= 0.42289710E 01 YO= 0.11274539E 01  
RIGHT SIDE OF REGION  
XO= 0.50326767E 01 YO= 0.75029042E 00  
GRAD= 0. GRADS= 0.  
ORDA= 0. ORDAS= 0.  
J= 18

LEFT SIDE OF REGION

XO= 0.46460071E 01 YO= 0.18761410E 01  
MIDDLE OF REGION  
XO= 0.40983284E 01 YO= 0.10926243E 01  
RIGHT SIDE OF REGION  
XO= 0.49325959E 01 YO= 0.70492824E 00  
GRAD= 0. GRADS= 0.  
ORDA= 0. ORDAS= 0.  
J= 19

LEFT SIDE OF REGION

XO= 0.45107235E 01 YO= 0.18687663E 01  
MIDDLE OF REGION  
XO= 0.39737075E 01 YO= 0.10594000E 01  
RIGHT SIDE OF REGION  
XO= 0.48774504E 01 YO= 0.66180626E 00  
GRAD= 0. GRADS= 0.  
ORDA= 0. ORDAS= 0.  
WITH BLOCKAGE CORRECTION, THE RADIATIVE FLUX BY THE AVT. AND AVP. METHOD IS 0.  
BY THE ABSORPTION METHOD, IT IS 0.

J= 20

LEFT SIDE OF REGION

XO= 0.44104131E 01 YO= 0.18618354E 01  
MIDDLE OF REGION  
XO= 0.38546720E 01 YO= 0.10276649E 01  
RIGHT SIDE OF REGION  
XO= 0.47468689E 01 YO= 0.62081493E 00  
GRAD= 0. GRADS= 0.  
ORDA= 0. ORDAS= 0.

J= 21

LEFT SIDE OF REGION

XO= 0.42233904E 01 YO= 0.18497644E 01  
MIDDLE OF REGION  
XO= 0.36317123E 01 YO= 0.96822379E 00  
RIGHT SIDE OF REGION  
XO= 0.45784804E 01 YO= 0.54421668E 00  
GRAD= 0. GRADS= 0.  
ORDA= 0. ORDAS= 0.

J= 22

LEFT SIDE OF REGION

XO= 0.40925614E 01 YO= 0.18394075E 01  
MIDDLE OF REGION  
XO= 0.34270603E 01 YO= 0.91366258E 00  
RIGHT SIDE OF REGION  
XO= 0.44251189E 01 YO= 0.47433939E 00  
GRAD= 0. GRADS= 0.  
ORDA= 0. ORDAS= 0.

J= 23

LEFT SIDE OF REGION

XO= 0.38659210E 01 YO= 0.18305240E 01  
MIDDLE OF REGION  
XO= 0.32786282E 01 YO= 0.86342612E 00  
RIGHT SIDE OF REGION  
XO= 0.42849297E 01 YO= 0.41036099E 00  
GRAD= 0. GRADS= 0.  
ORDA= 0. ORDAS= 0.

J= 24

LEFT SIDE OF REGION

XO= 0.37517649E 01 YO= 0.18228347E 01  
MIDDLE OF REGION  
XO= 0.30645020E 01 YO= 0.81700345E 00  
RIGHT SIDE OF REGION  
XO= 0.41562980E 01 YO= 0.35163417E 00  
GRAD= 0. GRADS= 0.  
ORDA= 0. ORDAS= 0.

J= 25

LEFT SIDE OF REGION

XO= 0.36839194E 01 YO= 0.18196413E 01  
MIDDLE OF REGION  
XO= 0.2922514E 01 YO= 0.79507545E 00  
RIGHT SIDE OF REGION  
XO= 0.40960303E 01 YO= 0.32387894E 00  
GRAD= 0. GRADS= 0.  
ORDA= 0. ORDAS= 0.

BTU/SEC-SQ FT

FIGURE 11. RADIATION PROGRAM, SAMPLE PRINT OUT (Concluded)

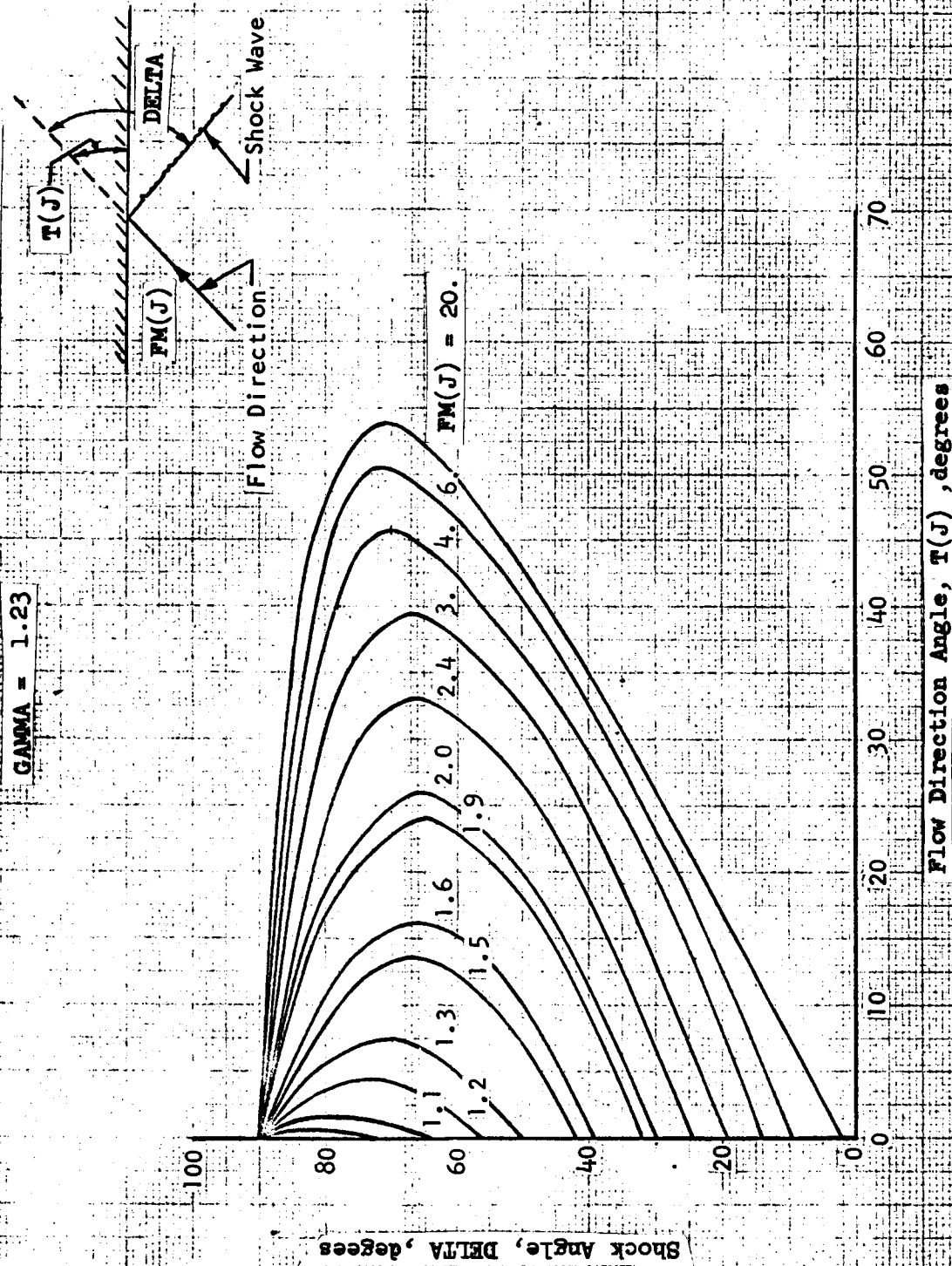


FIGURE 12. SHOCK ANGLE, DELTA, VERSUS FLOW DIRECTION,  $T(J)$ , FOR SELECTED MACH NUMBERS,  $FM(J)$ , USING OBLIQUE SHOCK THEORY

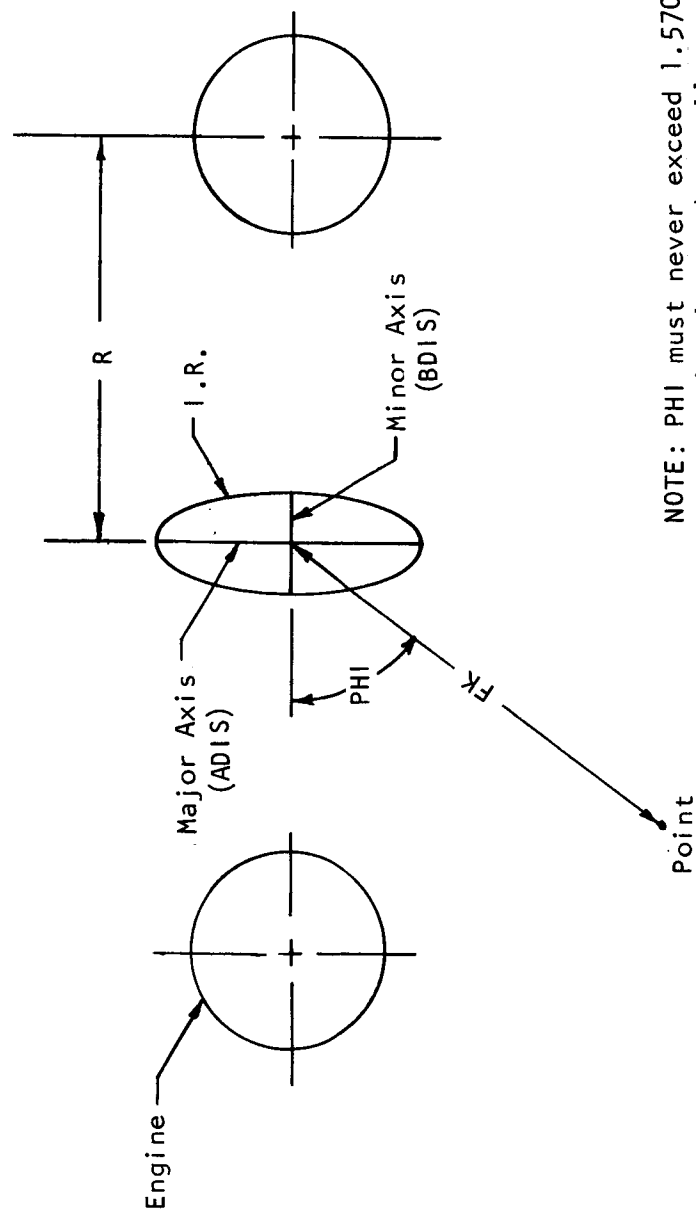


Mach Number (FM(J))	Theta (Radians)	Theta (Degrees)
1.1	.02827	1.62
1.4	.18325	10.5
1.6	.28796	16.5
1.8	.38045	21.8
2.0	.45724	26.2
2.4	.57417	32.9
3.0	.68935	39.5
4.0	.79232	45.4
5.0	.84293	48.3
10.0	.91972	52.7

NOTE: Values at 1.4, 1.8, 5.0, and 10.0 are interpolated from Figure 12. Notice that because of the purpose of the table our values for the maximum Theta at any given Mach number are on the low side of the actual maximum.

FIGURE 13. MAXIMUM VALUES OF THETA FOR SELECTED MACH NUMBERS

NOTE: This is a typical intersection region (I.R.). The region minor axis is on a line joining the rocket engine centers and the major axis is perpendicular to it as shown.



NOTE: PHI must never exceed 1.57079 radians.  
It is always the smallest angle between  
FK and BDIS.

FIGURE 14. GEOMETRY OF INTERSECTION REGION LOCATION

NOTE:  $-X_2 > -X_1$  but  $-X_2 < 0$  and  $-X_2 < X_3$ .

Thus  $-X_2$  must be input to analyze

I.R. (1) but not to analyze I.R. (2),

I.R. (3), or I.R. (4).

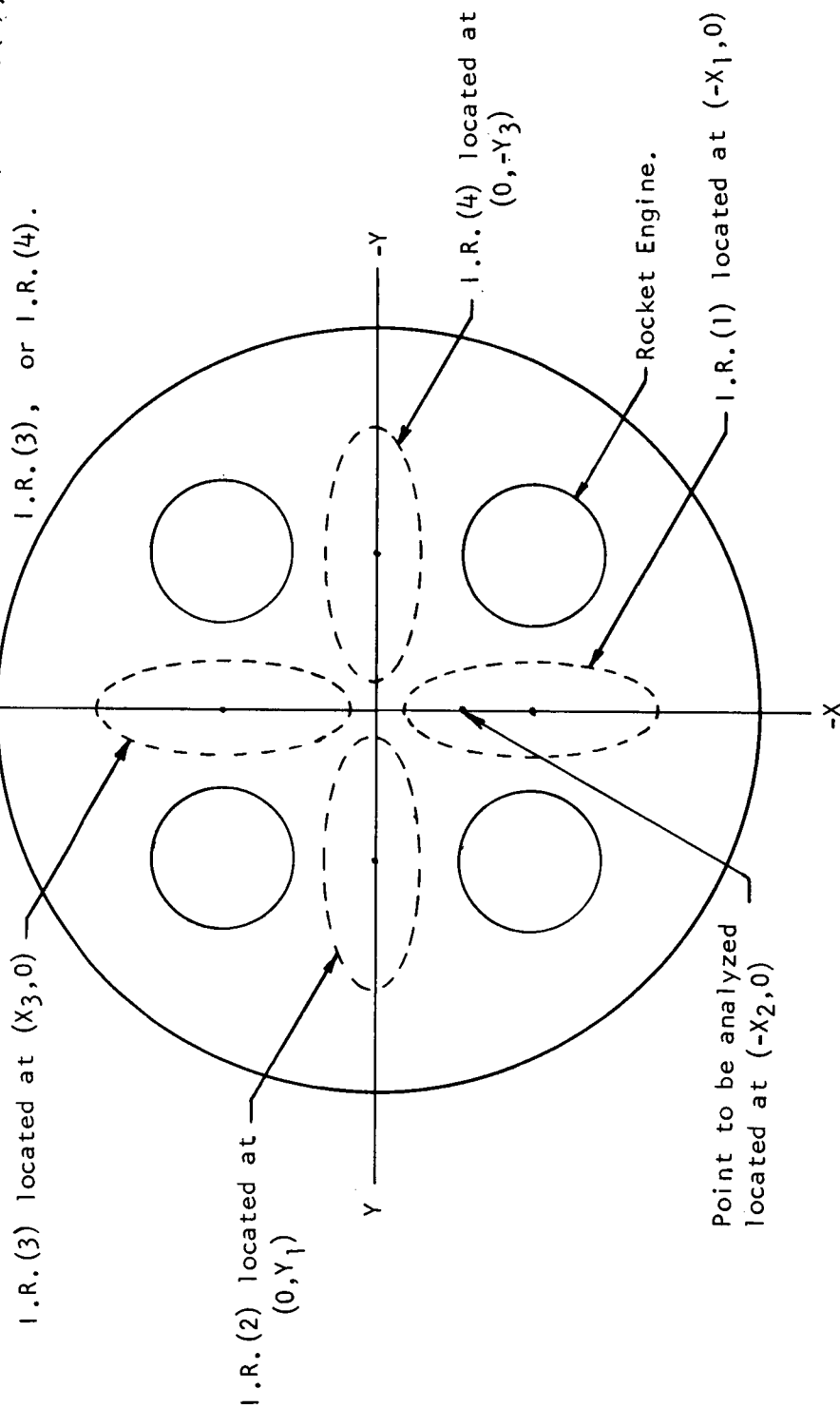
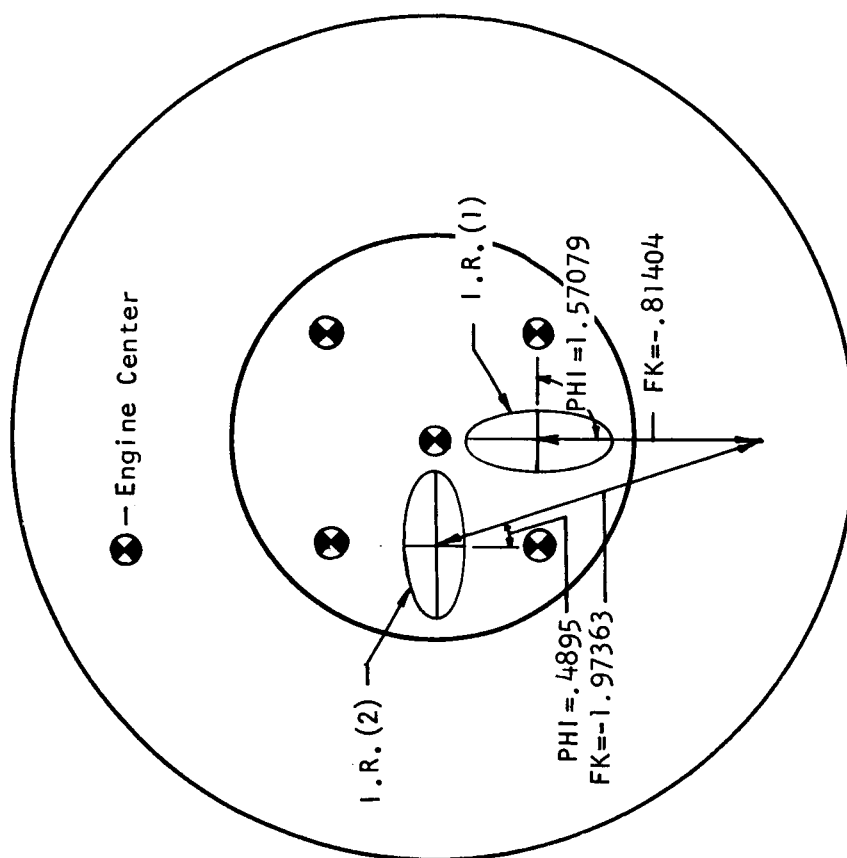


FIGURE 15. BASE GEOMETRY FOR SAMPLE PROBLEM ~ CASE IN WHICH THE X-COORDINATE MUST BE INPUT



NOTE: The heat shield and engines are not pictured here to avoid confusion.

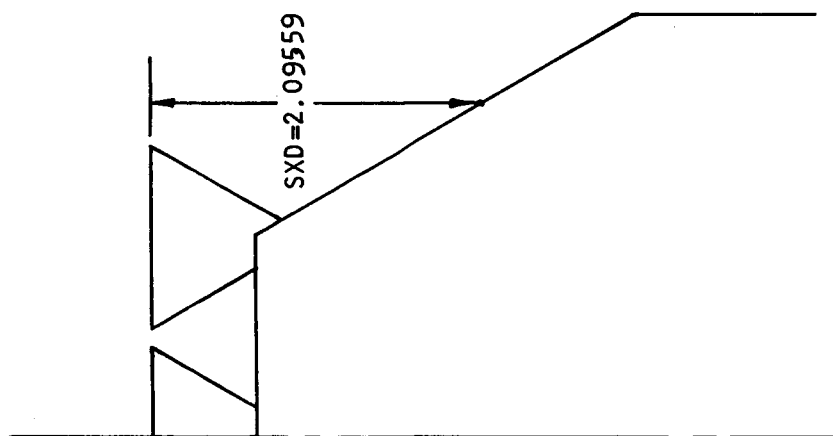


FIGURE 16. BASE GEOMETRY FOR SAMPLE PROBLEM

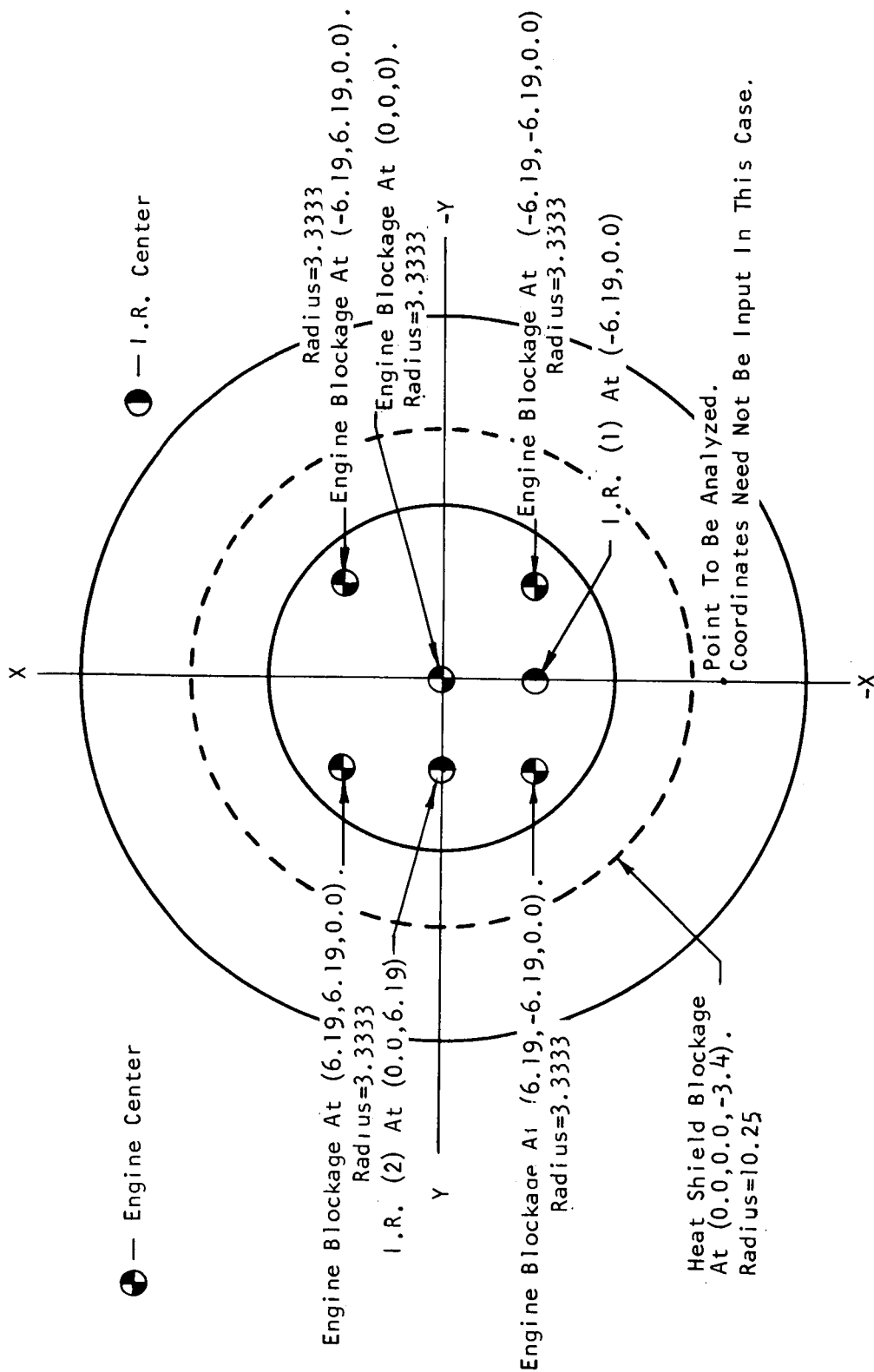


FIGURE 17. BASE GEOMETRY WITH COORDINATE LOCATIONS OF INTERSECTION AND BLOCKAGE REGIONS

CHAIN 1 INPUT	
*Block 1	X32,X25,X+1,.92773,43.004899,5760.0,1.23*
*Block 2	.0185*
*Block 3	*.55300,.60577,.68793,.75213,.82400,.87308,.91254,.96408,1.05794,1.09118* 1.14699,1.20885,1.27162,1.33487,1.43185,1.52983,1.68460,1.79133,1.90591* 2.00453,2.10755,2.20516,2.31099,2.39077,2.40765,2.51795,2.6743,2.82225* *2.96077,3.08055,3.19207,3.35044*
*Block 4	*5.55,5.678,6.121,6.027,6.01,5.89,5.874,5.840,5.80,5.78,5.75,5.723,5.715* 5.710,5.69,5.69,5.69,5.70,5.705,5.705,5.715,5.718,5.718,5.716,5.701* *5.705,5.717,5.72,5.722,5.725,5.719,5.685*
*Block 5	*0.59932,0.61166,0.69823,0.65766,0.63600,0.60129,0.58471,0.56404,0.53164* 0.51986,0.50391,0.48549,0.46950,0.45436,0.43380,0.41471,0.38945,0.37429* 0.36038,0.34923,0.33942,0.33107,0.32418,0.32047,0.32655,0.32794,0.31689* *0.30810,0.30217,0.29927,0.29961,0.291006*
*Block 6	*0.932,0.971,1.022,1.062,1.103,1.131,1.156,1.182,1.242,1.260,1.292* 1.323,1.355,1.388,1.437,1.488,1.561,1.609,1.660,1.710,1.743,1.783,1.825* *1.851,1.862,1.902,1.955,2.005,2.050,2.086,2.117,2.165*
*Block 7	*0.56,0.60,0.70,0.80,0.90,1.00,1.10,1.20,1.30,1.40,1.50,1.60,1.70,1.80* *1.90,2.00,2.10,2.20,2.30,2.40,2.60,2.80,3.00,3.20,3.30*
*Block 8	1.1,1.4,1.6,1.8,2.0,2.4,3.0,4.0,5.0,10.0*
*Block 9	.02827,.18325,.28796,.38045,.45724,.57417,.68955,.79232,.84293,.91972*
CHAIN 3 INPUT	
*Block 10	6.666,.63,3.45044*
*Block 11	-.81404,1.57079,2.09559*
CHAIN 4 INPUT	
*Block 12	X6,-6.19,0.0*
*Block 13	0.0,-6.19,6.19,6.19,-6.19,0.0*
*Block 14	0.0,6.19,6.19,-6.19,-6.19,0.0*
*Block 15	-3.4,0.0,0.0,0.0,0.0,0.0*
*Block 16	10.25,3.33,3.33,3.33,3.33,3.33*
*Block 17	1.0,1.0*

FIGURE 18. CHAIN INPUT DATA FOR INTERSECTION REGIONS

CHAIN 2 INPUT  
SECOND INTERSECTION REGION

\*Block 10 6.666,.63,3.45044\*

\*Block 11 -1.97363,.4895,2.09559\*

CHAIN 4 INPUT

\*Block 12 X6,0.0,6.19\*

\*Block 13 0.0,-6.19,6.19,6.19,-6.19,0.0\*

\*Block 14 0.0,6.19,6.19,-6.19,-6.19,0.0\*

\*Block 15 -3.4,0.0,0.0,0.0,0.0,0.0\*

\*Block 16 10.25,3.33,3.33,3.33,3.33,3.33\*

\*Block 17 1.0,1.0\*

FIGURE 18. CHAIN INPUT DATA FOR INTERSECTION REGIONS  
(Concluded)

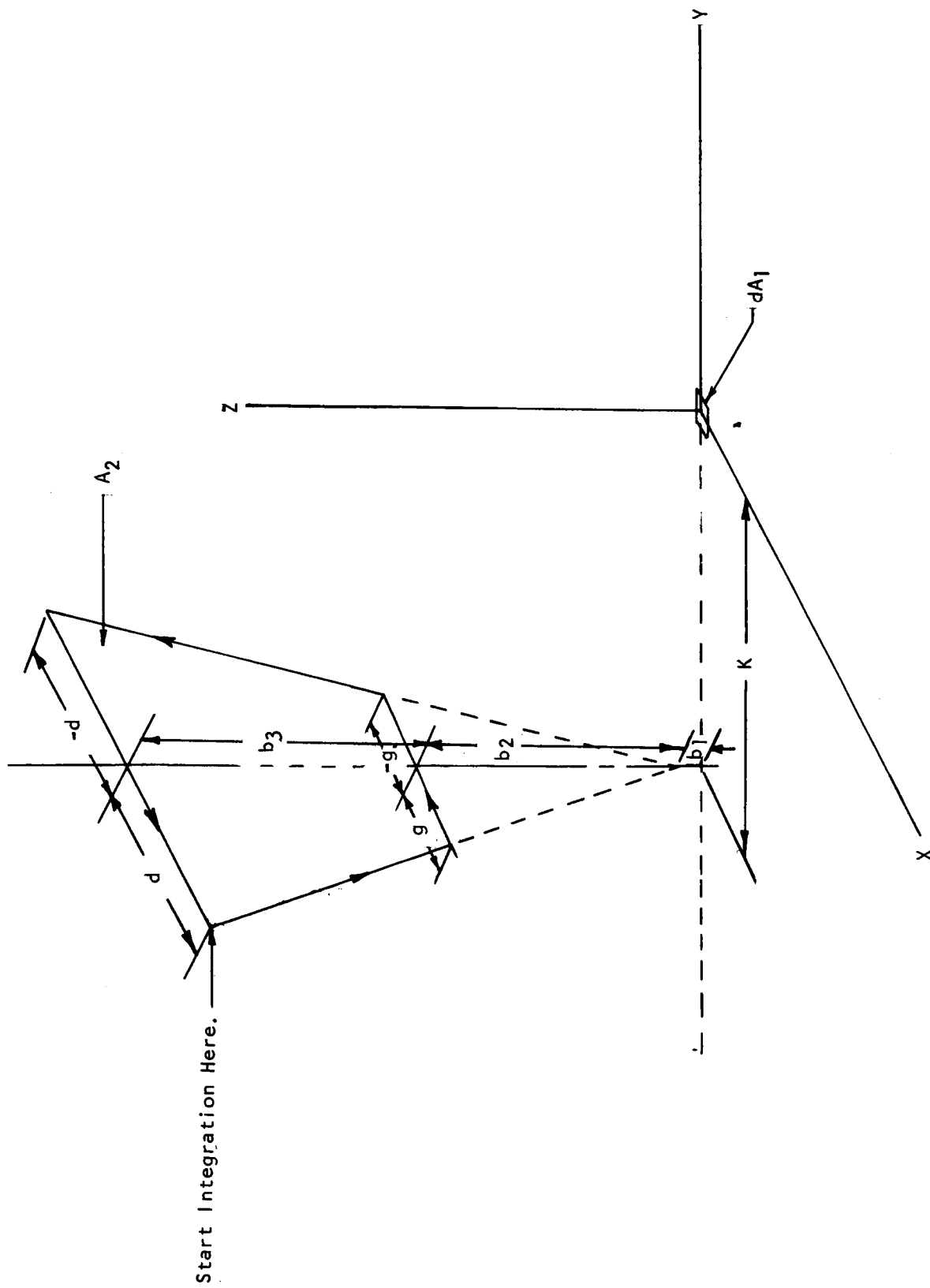


FIGURE 19. GEOMETRY OF SEGMENTED INTERSECTION REGION USED TO DETERMINE FORM FACTOR (SEE APPENDIX A)



## APPENDIX A

With reference to Figure 19, the form factor  $F$  from the region to area  $dA_1$  is given by Reference 2 to be

$$F_{dA_1-A_2} = \oint_c \frac{(y_2 - y_1) dx_2 - (x_2 - x_1) dy_2}{2\pi r^2}. \quad (33)$$

Since  $A_2$  is assumed parallel to the  $xz$  plane then  $dy_2 = 0$  and

$$F_{dA_1-A_2} = \oint_c \frac{(y_2 - y_1) dx_2}{2\pi r^2}. \quad (34)$$

By choosing  $dA_1$  at the origin

$$y_1 = x_1 = z_1 = 0. \quad (35)$$

Then,

$$F_{dA_1-A_2} = \frac{K}{2\pi} \oint_c \frac{dx_2}{r^2} \quad (36)$$

where

$$K = y_2. \quad (37)$$

Now the magnitude of the radius vector,  $r$ , is defined by

$$r^2 = x_2^2 + y_2^2 + z_2^2 = x_2^2 + K^2 + z_2^2 \quad (38)$$

but

$$z_2 = m x_2 + b. \quad (39)$$

Therefore,

$$r^2 = (1 + m^2) x_2^2 + (2mb)x_2 + (K^2 + b^2) \quad (40)$$

and

$$F_{dA_1-A_2} = \frac{K}{2\pi} \oint_c \frac{dx_2}{(1 + m^2) x_2^2 + (2mb)x_2 + (K^2 + b^2)}. \quad (41)$$

Integrating and proceeding around the trapezoid in the direction indicated yields

$$I_2 = \frac{K}{2\pi} \left( \frac{1}{\sqrt{K^2 + (b_1 + b_2)^2}} \right) \tan^{-1} \left( x \sqrt{\frac{1}{K^2 + (b_1 + b_2)^2}} \right) \Bigg|_{+g}^{-g} \quad (42)$$

$$I_4 = \frac{K}{2\pi} \left( \frac{1}{\sqrt{K^2 + (b_1 + b_2 + b_3)^2}} \right) \tan^{-1} \left( x \sqrt{\frac{1}{K^2 + (b_1 + b_2 + b_3)^2}} \right) \Bigg|_{-d}^{+d} \quad (43)$$

and

$$F_{dA_1-A_2} = I_2 + I_4. \quad (44)$$

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APPROVAL

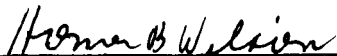
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A FORTRAN PROGRAM TO CALCULATE THE THERMAL RADIATION  
TO THE BASE OF A MULTI-ENGINE SPACE VEHICLE

By E. R. Heatherly, M. J. Dash, G. R. Davidson and C. A. Rafferty

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